Comparison between the non orographic gravity wave drag schemes used in global climate models to simulate a quasi-biennial oscillation and constant level balloons

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14	Key Points:
15	• Temptative, but somethink like:
16	• The non-orographic parameterization tuned to produce a realistic tropical quasi-
17	biennial oscillation in global climate models are used to predict in-situ observa-
18	tions.
19	• Parameterized gravity waves needed in large-scale models have realistic amplitudes
20	in the tropical lower stratosphere.
21	• Day-to-day variations of the estimated gravity wave momentum fluxes correlate
22	in some cases with observations, except when launching level are near the tropopause.
23	• The probability density distribution of the parameterized momentum fluxes are
24	better reproduced when the schemes are not related to their convective sources
25	and/or the launching level in the lower and middle troposphere.
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27 Abstract

Gravity Waves (GWs) parameterization schemes in 14 General Circulation Models (GCMs) 28 participating to the Quasi-Biennial Oscillation initiative (QBOi) are directly compared 20 to Strateole-2 balloon observations made in the lower tropical stratosphere from Novem-30 ber 2019 to February 2020 (phase 1) and from October 2021 and January 2022 (phase 31 2). The parameterizations used span the 3 state of the arts techniques used in GCMs 32 to represent subgrid scale non-orographic GWs, the two globally spectral techniques de-33 velopet by (Hines, 1997) and (Warner & McIntyre, 1999) respectively and the "multi-34 waves" approaches following (Lindzen, 1981). The input meteorological fields necessary 35 to run the parameterizations offline are extracted from the ERA5 reanalysis and corre-36 spond to the instantaneous meteorological conditions found underneath the balloons. In 37 general, the amplitudes are in fair agreement between measurements of the momentum 38 fluxes due to waves with periods less than 1 hr and the parameterizations. The corre-39 lation of the daily values between the observations and the results of the parameteriza-40 tion can be around 0.4, which is statistically elevated considering that we analyse around 41 1200 days of data and sometime good considering that the parameterizations have not 42 been tuned: the schemes used are just the standard ones that help producing a Quasi-43 Biennial Oscillation in the corresponding model. These correlations nevertheless vary 44 considerably between schemes and depend little on their formulation (globally spectral 45 versue multiwaves for instance). We therefore attribute it to dynamical filtering all schemes 46 taking good care of it, whereas only few relate the gravity waves to their sources. Ex-47 cept for one model, significant correlations are mostly gound for eastwrd propagating 48 waves, which may be due to the fact that during both Strateolo 2 phases the QBO phase 49 is eastely at the altitude of the balloon flights. On the other hand, statistical properties, 50 like pdf of momentum fluxes seem better represented in spectral schemes with constant 51 sources than in schemes ("spectral" or "multiwaves") that relate GWs to their convec-52 tive sources. 53

54 Plain Language Summary

In most large-scale atmospheric models, gravity wave parameterizations are based 55 on well understood but simplified theories and parameters which are keyed to reduce sys-56 tematic errors on the planetary scale winds. In the equatorial regions, the most challeng-57 ing errors concern the Quasi Biennial Oscillation. Although it has never been verified 58 directly, it is expected that the parameterizations tuned this way should transport a re-59 alistic amount of momentum flux in both the eastward and westward directions when 60 compared to direct observations. Here we show that it is the case, to a certain extent, 61 using constant-level balloon observations at 20 km altitude. The method consists in com-62 paring directly, each day and at the location of the balloon the measured momentum fluxes 63 and the estimations from the gravity wave parameterizations used in the global mod-64 els that participate to the Quasi-Biennal Oscillation intiative and when using observed 65 values of the large-scale meteorological conditions of wind, temperature, precipitation, 66 and diabatic heating. 67

68 1 Introduction

It is well known that the large scale circulation in the middle atmosphere is in good 69 part driven by gravity waves (GWs) that propagate in the stratosphere (Andrews et al., 70 1987). These waves carry horizontal momentum vertically and interact with the large 71 scale flow when they break. The horizontal scale of these waves can be quite short, much 72 shorter than the horizontal scale of General Circulation Models (GCMs) so they need 73 to be parameterized (Alexander & Dunkerton, 1999). In the tropics, the convective GWs 74 are believed to dominate largely (Fovell et al., 1992; Alexander et al., 2000; Lane & Mon-75 76 crieff, 2008), they contribute significantly to the forcing of the Quasi-Biennial Oscillation (QBO), a near 28-month oscillation of the zonal mean zonal winds that occurs in 77 the lower part of the equatorial stratosphere (Baldwin et al., 2001). For these reasons, 78 the parameterization of convective GWs is necessary for most GCMs to explicitly real-79 ize the QBO. 80

Although gravity wave parameterizations are now used in many models with suc-81 cess including in the tropics (Anstey et al., 2016; Scinocca, 2003; Orr et al., 2010; Chris-82 tiansen et al., 2016) (Serva et al., 2018)(Beres et al., 2005; Song & Chun, 2005; Lott & 83 Guez, 2013; Bushell et al., 2015), their validation using direct in situ observations remains 84 a challenge. There exist observations of GWs using global satellite observations (Geller 85 et al., 2013) but the GWs identified this way still have quite large horizontal scales, and 86 some important quantities like the Momentum Fluxes (MFs) are often deduced indirectly, 87 for instance from temperature measurements using polarization relations (Alexander et 88 al., 2010; Ern et al., 2014). For these two reasons, in situ observations are essential, and 89 the most precise ones are provided by constant-level long-duration balloons, like those 90 made in the Antarctic region during Strateole-Vorcore (Hertzog, 2007) and Concordiasi 91 (Rabier et al., 2010), or in the deep tropics during PreConcordiasi (Jewtoukoff et al., 2013) 92 and more recently Strateole 2 (Haase et al., 2018). Among many important results, these 93 balloon observations have shown that the momentum flux entering in the stratosphere 94 is extremely intermittent (Hertzog et al., 2012). This intermittency implies that the mean 95 momentum flux is mostly transported by few large-amplitude waves that potentially break 96 at lower altitudes than when the GW field is more uniform. This property, when repro-97 duced by a parameterization (de la Cámara et al., 2014; Kang et al., 2017; Alexander 98 et al., 2021), can help reduce systematic errors in the midlatitudes, for instance on the 99 timing of the final warming in the Southern Hemisphere polar stratosphere (de la Cámara 100 et al., 2016), or on the QBO (Lott, Guez, & Maury, 2012). Balloon observations have 101 also been used to characterize the dynamical filtering by the large scale winds (Plougonven 102 et al., 2017), and to validate the average statistical properties of the GW momentum flux 103 predicted offline using reanalysis data (Kang et al., 2017; Alexander et al., 2021). How-104 ever, the evaluation of parameterizations using balloon observations have have often been 105 quite indirect so far, with the common belief that the best a parameterization can do 106 is to reproduce a realistic statistical behaviour (Jewtoukoff et al., 2015; Kang et al., 2017; 107 Alexander et al., 2021). and there are few good reasons for that. For example, param-108 eterizations are often based on simplified quasi-linear wave theory, they assume spectral 109 distributions that are loosely constrained, and they ignore lateral propagation almost 110 entirely (some attempt to include it can be found in Amemiya and Sato (2016)). Nev-111 ertheless, some factors could mitigate these weaknesses. One is that in most parameter-112 izations the wave amplitude is systematically limited by a breaking criterion that encap-113 sulates nonlinear effects. An other is that some parameterizations explicitly relate launched 114 waves to sources, and there is constant effort to improve the realism of the convective 115 ones (Liu et al., 2022). Also, observations systematically suggest that dynamical filter-116 ing by the large scale wind is extremely strong for upward propagating GWs (Plougonven 117 et al., 2017), and this central property is represented in most GW parameterizations. For 118 all these reasons, it may well be that GW parameterizations keyed to the large scale con-119 ditions found at a given place and time gives MFs that can be directly compared to the 120 MFs measured by a balloon at the same place. 121

Based on the relative success of the offline calculations done in the past using re-122 analysis data (Jewtoukoff et al., 2015; Kang et al., 2017; Alexander et al., 2021), (Lott 123 et al., 2023) have shown that such a direct comparison gives result of interest. The first 124 is that a state of the art convective gravity wave drag scheme, predicts momentum fluxes 125 in the low equatorial stratosphere which amplitude can be directly compared with those 126 measured during the Strateole-2 balloon flights. It gives a direct in-situ observational 127 confirmation that the theories and modelling of the QBOs developed over the last 50 years 128 were in good part correct about the significance of the GWs to the QBO forcing. Also 129 interesting, the comparison showed a good level of correlation between the day to day 130 variability in momentum fluxes between measured and observed fluxes, a correlation that 131 is much better for waves carrying momentum fluxes in the eastward direction than in 132 the westward direction. It was suggested that such a good correlation was due to the 133 fact that the (Lott & Guez, 2013) scheme analysed relate the gravity waves to their con-134 vective sources (not all schemes do) and that the GWs experience significant dynami-135 cal filtering in the middle troposphere and lower stratosphere. (Lott et al., 2023) nev-136 ertheless revealed that a scheme that relates gravity waves to convection only somehow 137 failed in predicting the right statistical behaviour of the momentum fluxes, the pdfs show-138 ing a long tail for low values of the MFs, suggeting missing processes like lateral prop-139 agation or the presence of a background of waves which origin remains a challenge to pre-140 141 dict.

The purpose of this paper is to continue such a direct comparison using the most 142 recent observations and near all the gravity wave parameterization schemes used by the 143 modelling groups participating to the Quasi-Biennial Oscillation initiative (QBOi, (Butchart 144 et al., 2018)). We will follow for that (Lott et al., 2023) and use the 8 balloons of the 145 first phase of the Strateole 2 campaign that flew in the lower tropical stratosphere be-146 tween November 2019 and February 2020 and extent it to the 15 balloons that flew more 147 than one day during the second phase of the Strateole 2 campaign, between October 2021 148 and January 2022. For each of the flights and each time, we have identified the grid point 149 in the ERA5 reanalysis (Hersbach et al., 2020) that is the nearest and used the verti-150 cal profiles of wind and temperature as well as the surface value of precipitation to em-151 ulate the parameterization of GWs used in the global models that participated to the 152 Quasi-Biennial Oscillation initiative (QBOi). We also extract from the analysis and short 153 range forecast, diabatic heatings and the cloud base and top altitudes needed in some 154 schemes to predict gravity waves. 155

¹⁵⁶ 2 Data and method

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2.1 Parameterizations of non orographic gravity wave schemes

The parameterizations schemes used to predict orographic gravity waves belongs 158 to two well separated families, dating back from the 1980's when it becomes evident that 159 a goood simulation of the middle atmosphere by global atmospheric models could not 160 be done without taking into account non-orographic gravity waves. The first family roots 161 in the formulation by (Lindzen, 1981), where the gravity wave field field is represented 162 by gravity waves monochromatic in the horizontal space and time. It was extended to 163 treat a large ensemble of waves by (Alexander & Dunkerton, 1999) making the asump-164 tion that the breaking of each waves could be made independent from the others. An 165 advantage of such schemes is that it roots in linear theories where sources like convec-166 tion and/or fronts can be introduced using closed form theories (Beres et al., 2005; Song 167 & Chun, 2005; Richter et al., 2010; Lott & Guez, 2013; de la Cámara & Lott, 2015). In 168 the following we will refer to such schemes as "multiwave", they are expensive because 169 they request a large amount of waves to represent well a realistic wave field, but this limit 170 can easily be circumvented by using stochastic approaches (Eckermann, 2011; Lott, Plougonven, 171 & Vanneste, 2012). As an alternative, but also to better represent breaking, many cen-172 ters developed globally spectral schemes. These schemes uses the observationnal fact that 173

	p_l	F_{LT}	$2\pi/m_*$	$ C_{\min}$
CMAM IFS ECEarth	100hPa 450hPa 450hPa	1.3mPa 5mPa 3.75mPa	1km 3km 2km	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
UKMO	1000hPa	Precip	4.3km	2

Table 1. WMI Parameters changing between CMAM, IFS, ECEarth, and UKMO. UKMO is shown distinctly because it is based on (Warner & McIntyre, 1999) simplified version of WMI rather than on (Scinocca, 2003)'s and realte launched MF to precipitations.

in observations the vertical shape of the spectra have a quite universal character. In the 174 early 1990's (Hines, 1991) developed a theory where GW breaking is represented by im-175 posing an upper limit to the range of vertical wavenumber, the limit being calculated 176 according to the large scale wind and including a Doppler spreading by the other grav-177 ity waves (see also (Hines, 1997)). The scheme has been implemented with success in var-178 ious GCMs (see for instance (Manzini et al., 1997)), and will be referred to as "HDS" 179 in the following. As an alternative, the theory in (Warner & McIntyre, 1996) imposes 180 gravity wave saturation according to an empirical spectra but treat vertical changes in 181 the spectra following GWs propagation invariant character. The theory has been sim-182 plified and/or optimized to permit implementation, for instance in the UKMO model (Warner 183 & McIntyre, 1999; Scaife et al., 2002) and in the CMAM model (Scinocca, 2003) respec-184 tively, and will be referred to has "WMI" in the following. To a certain extent, the spec-185 tral schemes can also take into account the relation with sources, for instance the HDS 186 scheme has been related to fronts in (Charron & Manzini, 2002), and the UKMO ver-187 sion of the WMI scheme to precipitations in (Bushell et al., 2015). 188

In the present paper, we are going to compare the GWs schemes used in 14 of the models that participate to QBOi, all belonging to one of the three type of schemes described above (WMI, HDS, and Multiwave), all the multiwave schemes relating GWs to their convective sources, only one of the spectral scheme doing so, the UKMOgws WMI scheme in (Bushell et al., 2015), its results will be discussed with the source-related multiwave scheme.

Among the 14 models, three use the (Scinocca, 2003)'s version of the WMI: CMAM, IFS and ECEarth. Their version for QBOi and further detailed in (Anstey et al., 2016; Orr et al., 2010; Davini et al., 2017), they essentially differ by four parameters, the launch level pressure p_l , the launched momentum flux F_{LT} , the characteristic vertical wavenumber m_* and a minimum intrinsic phase speed in the launched spectra Note that for EC-Earth the exact value of the parameters are from J. Garcia Serrano (private communication).

Still among the 14 models, 5 uses the (Hines, 1997)'s parameterization schemes pre-202 sented in (Manzini et al., 1997). Between the five models, and in the Hines scheme, only 203 changes between models the launching level p_l , the root mean square of the horizontal 204 wind variability due to GWs at launch level σ , as well as an effective horizontal wavenum-205 ber K^* . There are also more numerical parameters that eventually changes, a minimum 206 value for the the cutoff vertical wavenumber m_{\min} , and two parameters that control smooth-207 ing in the vertical of the GWs root mean square variance and cut-off vertical wavenum-208 ber, the coefficient $C_{\rm SMO}$ and the number of time the smoothing is applied $N_{\rm SMO}$. 209

	$ p_l$	σ_s	$2\pi/K^*$	m_{\min}	$ C_{\rm smo} $	N _{smo}
	4501 D	1	1051			
ECnam5 MIROC	450nPa 650hPa	1.0.95	250km	$\begin{bmatrix} 0 \\ 6.5 \ 10^{-5} \end{bmatrix}$	$\begin{vmatrix} 2\\ 2 \end{vmatrix}$	$\frac{5}{2}$
MPIM	650hPa	1.2	125km	0	2	2
MRI-ESM	700hPa	1.9	1250km	$3.3\ 10^{-4}$	$\begin{vmatrix} 4\\ 2 \end{vmatrix}$	$\begin{vmatrix} 2\\ 2 \end{vmatrix}$
EMAC	050111 a	1.	125KIII	0		<u> </u>

Table 2. HDS Parameters changing between ECHam5, MIROC, MPIM, MRI-ESM, andEMAC.

	p_l	Phase Speed	Δz	Source
LMDz Yonsei WACCM	500hPa 900hPa-100hPa ?	-30m/s <intrinsic<30m s<br="">-100m/s<absolute<100m s<="" td=""><td>1km 100m-15km</td><td>Precip Heating rate Heating rate</td></absolute<100m></intrinsic<30m>	1km 100m-15km	Precip Heating rate Heating rate

 Table 3.
 Some parameters changing between LMDz, YONSEI and WACCM, for information only the schemes being extremely distinct

Finally the last 4 schemes we consider all links GWs to sources (convection or pre-210 cipitation), 3 are multiwaves and have been developed independently one from the oth-211 ers, LMDz, YONSEI, and WACCM and 1 uses the ultra simple version of the WMI schemes 212 presented in (Warner & McIntyre, 1999; Bushell et al., 2015) rather than the (Scinocca, 213 2003)'s version. The differences between these schemes are numerous it is impossible to 214 details them, the reader is referred to the corresponding papers. The most salient dif-215 ferences are in the source term. In LMDz is made the choice to relate the launched MF 216 to square precipitation P_r^2 consistent with linear theory before breaking (Lott & Guez, 217 2013) whereas in (Bushell et al., 2015) it is related to $\sqrt{P_r}$. In the Yonsei's scheme (Song 218 & Chun, 2005; Choi & Chun, 2011), the launched momentum flux is directly related to 219 convective heating distributed in the vertical between the cloud bottom and cloud top, 220 the launch altitude being at the cloud top. In this case the launching level can vary be-221 tween 2km and 15km typically and the depth of the heating between 100m and 15km. 222 Also, the absolute phase speed cover the ranges $100 \text{m/s} < C_{abs} < 100 \text{m/s}$. 223

2.2 Offline parameterization runs

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To activate the schemes in offline mode we will use ERA-5 hourly data of precip-225 itation and 3-hourly data of winds, surface pressure, temperature, cloud liquid and ice 226 water content at $1^{\circ} \times 1^{\circ}$ horizontal grid to mimic a large scale climate model resolution. 227 Winds, surface pressure, temperature, and water contents are then linearly interpolated 228 on 1hr time step to be synchronised with precipitation. In the vertical we use data at 229 67 model levels, taking one every two ERA5 levels, to speed up calculations. To estimate 230 convective heating rates vertical profiles, we follow (Fueglistaler et al., 2009) and eval-231 uate diabatic heating using ERA5 hourly data from short range forecast and as a resid-232 ual between the parameterized temperature tendency and the radiative heatings (long-233 wave plus shortwave). When needed, we also evaluate the cloud bottom height and top 234 height using the cloud water content (liquid+ice) from ERA5 reanalysis. 235



Figure 1. Strateole 2, Phase 2 balloon trajectories taking place between October 2021 and January 2022. Shading presents the precipitation field from ERA5 averaged over the period.

2.3 Strateole 2 balloon observations

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The in situ observations we use are from the 8 balloons of the first phase of the Stra-237 teole 2 campaign that flew in the lower tropical stratosphere between November 2019 238 and February 2020 and from the 15 balloons that flew more than one day during the sec-239 ond phase of the Strateole 2 campaign, between October 2021 and January 2022. The 240 trajectories during phase 2 are shown in Figure 1, superimposed upon the averaged pre-241 cipitation (the same Figure but fir phase 1 is in (Lott et al., 2023)). In the MFs calcu-242 lated from observations Corcos et al. (2021) distinguish the waves with short periods (1hr-243 15mn) from the waves with period up to one day (1d-15mn). They also distinguish the 244 eastward waves giving positive MF in the zonal direction from the westward waves giv-245 ing negative MF. As shows Fig. ??, it is coincidental that the phase 1 flights took place 246 during the 2nd documented QBO disruption (Anstey et al., 2021), but the fact that the 247 measurements are below the altitude at which the disruption manifests makes us believe 248 that our comparison between gravity wave MFs over the period is not much affected by 249 the disruption (beyond the fact that the disruption potentially affects the large scale winds, 250 which is something that translates well in the parameterization). It is also important to 251 notice that during phase 2, the large scale winds conditions in the lower stratosphere are 252 almost as during phase one at balloons altitudes (end of eastward QBO phase). 253

In the following we will compare the momentum fluxes derived from the balloon 254 data, emphasize the intrinsic frequencies that the scheme represents (the intrinsic pe-255 riods below 1hr) and consider the ERA5 data at the points that are the nearest from 256 the balloon. The prediction is then made every hour and averaged over the day, again 257 because this is the time scale needed for our scheme to sample realistically a GW field, 258 and also because it takes around a day for a balloon flight to cover about a model grid-259 scale. We will discuss sensitivities to these choices in the first paragraph of the conclu-260 sion. 261



Figure 2. Time vertical sections of the zonal mean zonal wind (CI=10m/s, negative values are dashed and non-orographic gravity wave tendency averaged over the Equatorial band (-6S - +6N). Input data are from ERA5 reanalysis and GWs prediction from the LMDz scheme. The 2 green boxes indicate schematically the altitude and time ranges of the Strateole 2 phase 1 and 2 flights considered in this study.

262 3 Results

THIS SECTION IS UNDER PROGRESS, ONLY THE FIGURES SHOULD BE CONSULTED

Figure 3 shows time series of daily values of momentum fluxes predicted by the pa-265 rameterizations and measured during balloon flights 2 from strateole 2 phase 1. This is 266 also the flight shown in Fig. 3 in (Lott et al., 2023), and where was also shown the time 267 series of daily precipitation and zonal wind at flight altitude. The top panel is for the 268 WMI based schemes, the middle panel for the HDS schemes and the bottom panels for 269 the schemes relating the GWs fluxes to their sources. In all panels the black curves are 270 for the daily observations. For clarity we present results for the Eastward and westward 271 MF only. Overall ones sees that the schemes predict momentum flux values that some-272 how compare with the observed one, at least in terms of amplitude. In the globally spec-273 tral schemes (upper and middle panels), we also see that the parameterizations predict 274 peaks in MF which duration and amplitudes looks reasonable compared to the observed 275 ones. More specifically, and in the eastward direction there are pronounced peaks after 276 day sixty, peaks that (Lott et al., 2023) related to the fact that after this date the zonal 277 wind at balloon altitude is westward a situation that favors eastward waves. Of course 278 in terms of amplitude there are varibilities between the models schemes, but the qual-279 itative behaviours look reasonnable. There is nevertheless one exception, the CMAM scheme 280 predicts long lasting plateau, maybe for this scheme the fact that the launching altitude 281 is quite high, mitigate the dynamical filtering between the launching level and the bal-282 loon flight. 283

The fact that the parameterizations estimates fluxes of about the right amplitude is summarized in Figure 5, where the average of the fluxes over all strateole flights that last than a month (18 flight in total) are shown. It confirms systematically that the offline estimations are quite good on average and in the zonal direction, for the eastward



Figure 3. Comparison between daily averaged values of the eastward and westward MFs measured by the balloons during Strateole 2 Flight 1 and estimated by the GW schemes at the balloon location and altitude. Colored curves are for the GW schemes predictions using ERA5 and from different models, black curves are for the observed MFs due to the 15mn-1hr GWs.

and westward components again. The Figure 6 group the models averaging the eastward
and westward fluxes over all the balloon flights, confirming again that the parameterizations used fall around the observed values. There is varibilities between the models,
but there is no tendency for the models to vcollectively need much more or much less
gravity wave stress than needed.

The curves in Figure 3 and Figure 4 also suggest that observations and offline es-293 timations evolve quite similarly day after day, both measured and parameterized MFs 294 being sensitive to precipitation and dynamical filtering. To test more systematically this 295 relationship, we also calculated the correlations between measured and estimated MFs 296 and for each flight (Table ??). To test the significance, we measure the number of De-297 grees of Freedom (DoF) present in each dataset, and calculate for that the decorrelation 298 time scale, which we take as the lag in day beyond which the lag-autocorrelation of the 299 series falls below 0.2. As this time-lag varies from one series to the other, we give explic-300 itly in column 5, the number of DoF, which is the duration of the flight divided by the 301 decorrelation time scale. Note that for their decorrelation time, we consider for simplic-302 ity that evaluated with daily averaged observations, but found that it is not much dif-303 ferent from that evaluated with the offline estimates (not shown). In each case, we find 304



Figure 4. a) Same as Fig 3 but for Strateole 2 Phase 2 Flight 7.



Figure 5. Scatter plot of the momentum fluxes measured by the balloon versus parameterized using different models. Only considered here the 18 balloon flights that last more than a month (East: black; West: red; Cumulated: green). Also shown are the correlations between observations and predictions, 99% significant levels are bold underlined, 95% are bold. Non significant values are shown in italic for information. The number of DoF for Pearson test is 18, about the number of balloon flights that last more than a month.

positive correlations, they are often significant in the Eastward direction the estimated
westward being much more difficult to predict. In the eastward directions, differences
seems more related to the launching altitude than to the nature of the scheme, CMAM
lauching waves near the tropopause whereas YONSEI often does so when clouds extent
over the entire troposphere, in which case little dynamical filtering can occur between
the launching level and the quite nearby flights.

A major differences between the scheme, is that in some the GW activity is related 311 to convective heating or precipitation, whereas others consider uniform sources. In the 312 first case its means that momentum fluxes could be underestimated in many circumstances, 313 despite the fact that the amplitudes are realistic when considering long term averages. 314 To analyse better this difference and its potential consequences, the Figure ?? presents 315 PDFs of the distributions of the momentum fluxes considering all the daily data. For 316 the PDFs (solid line), one sees that the balloons almost systematically measure fluxes 317 with amplitude between 0.1mPa and 10mPa (see Figure ??a), whereas in the parame-318 terizations with convective/precipitation sources there are many more contributions from 319 the smaller amplitude momentum fluxes (solid red), not mentioning that the zero val-320 ues are excluded from PDFs when plotted versus the logarithm of MF amplitudes. 321

322 4 Conclusion



Figure 6. East, West and cumulated zonal momentum fluxes averaged over the Strateole 2 phase 1 and 2 period period and according to participating models.

East	Day	CM	IFS	ECE	Ech	MI	MPI	MRI	EM	LMD	UK	YON
	Dof	AM		ARTH	am5	ROC	Μ	ESM	AC	Z	MO	SEI
Phase 1	670-216	-0.07	0.53	0.52	0.52	0.48	0.49	0.44	0.48	0.49	0.34	0.32
Phase 2	621-322	-0.19	0.41	0.38	0.38	0.33	0.34	0.30	0.33	0.40	0.34	0.20
Phase 1+2	1291-538	-0.11	0.49	0.47	0.45	0.41	0.41	0.36	0.40	0.46	0.34	0.27
West	Day	CM	IFS	ECE	Ech	MI	MPI	MRI	EM	LMD	UK	YON
	Dof	AM		ARTH	am5	ROC	Μ	ESM	AC	z	MO	SEI
Phase 1	670-216	0.14	-0.07	-0.07	-0.13	-0.03	-0.04	-0.04	-0.04	0.30	-0.03	0.10
Phase 2	621-322	0.21	0.18	0.16	0.03	0.00	0.01	0.05	-0.01	0.40	0.04	0.13
Phase 1+2	1291-538	0.17	0.05	0.04	-0.05	-0.02	-0.02	0.01	-0.02	0.34	0.00	0.11

 Table 4.
 Correlation between observed and measured fluxes, strateole phases 1 and 2.



Figure 7. PDFs of daily values of Momentum flux distribution. The PDFs are calculated from histograms of 1291 MFs daily value within intervals of $\Delta \left(\log_{10} \rho \overline{u'w'}(\text{mPa}) \right) = 0.05$, thereafter smoothed by a 5 point non-recursive filter with weight (0.1, 0.2, 0.4, 0.2, 0.1). Measured values are in green, estimations using ERA5 data and the parameterizations are in black. Solid lines are for Eastward, dashed lines are for Westward.

³²³ 5 Open Research

- Balloon data presented in (Haase et al., 2018) can be extracted from the STRA-TEOLE 2 dedicated web site: https://webstr2.ipsl.polytechnique.fr
- ERA5 reanalysis data are described in (Hersbach et al., 2020) and can be extracted from the COPERNICUS access hub: https://scihub.copernicus.eu/
- The LMDz-6A GCM used for CMIP6 project is described in (Hourdin et al., 2020), it can be directly installed from the dedicated webpage: https://lmdz.lmd.jussieu.fr/utilisateurs/installationlmdz

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Appendix: Running the offline code

To run the models parameterizations in offline mode and compare with daily values of momentum fluxes measured during strateole 2, download the file offline_v9_Strateole_QBOi_Open.tar, on the web page:

337 wget https://web.lmd.jussieu.fr/~flott/DATA/offline_v9_Strateole_QBOi
338 _Open.tar.gz
339 Then gunzip and do tar -xvf offline_v9_Strateole_QBOi_Open.tar

- In the directory, offline_v9_Strateole_QBOi_Open:
- Run directory It basically contains a script that compile the programs, link to the in-341 put dataset and produce various outputs. The Makefile certainly needs to be adapted 342 to the computer. 343 To launch predictions for Strateole-2 phase 1, launch: ./laun_ph1ball_gwd_era5.sh 344 For phase 2, $ph1 \rightarrow ph2$. 345 Fortran Codes: all the fortran routines are located in prog. 346 laun_gwd_era5.f90: Main program loading input data in netcdf format and cal-347 culating drag and momentum fluxes at the balloon place. 348 preci_gwd_LMDz_QBOi.f90: LMDz Multiwaves routines predicting gwdrag from 349 precipitation 350
- **gwsat_Modnam.f90:** the globally spectral scheme using the (Warner & McIntyre, 1996)'s scheme version by J. Scinocca.
- ³⁵³ hinesgw6g_plus_subs.f HDS scheme
- gw_ussp_core.f90: The WMI scheme with amplitude keyed to precipitation used
 in some UKMO runs.

³⁵⁶ **cgwcalc.f90:** Multiwave scheme developped at Yonsei's university

- Input Data: All the input data are located in the directories hourly_ph1 and hourly_ph2 for phase 1 and 2 respectively. For instance, 1hr average of the strateole2 momentum fluxes are in
- 360 ALL_STRATEOLE2_Balloon_ph1_1day15min.nc
- and

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- 362 All_STRATEOLE2_Balloon_ph1_1hrs15min.nc
 - for the waves with periods between 1day and 15mn and between 1Hr and 15 mn respectively.
- 365 Still in this directory, the ERA5 reanalysis products, which include winds tem-
- $_{366}$ perature, cloud liquid water, and surface log pressure, over a 5°x5° domain cen-
- tered at the balloons drifting locations are in Input_ERA5_data_all_variables_balloons_ph1.nc.
- Precipitation every hours are also included. The diabatic heatings are from fore-

369	cast. All datas that are only provided every 3hr are linearly interpolated in time
370	to give hourly values.
371	Output data (Part 1)
372	All the ouputs are in the output_ph1 and output_ph2 directories:
373	Netcdf: contains the output of the schemes in netcdf format on the vertical col-
374	umn and over the $5^{\circ}x5^{\circ}$ domain over which the ER5 data are provided. There is
375	one netcdf dataset by balloons flight each contains output from all the schemes.
376	Balloon_alt After post processing by the python scripts launch_script_obs.py, are
377	extracted the MFs at balloon flight altitude.
378	Python Scripts
379	A serie of Python scripts, located into python_script are proposed to compare the
380	outputs of the scheme to the balloon data.
381	launch_script_obs.py: Reads the balloon flight data of MFs and averaged over
382	1day and writte them in text format (ending with '.dat') and stored in output/Balloon_alt/obs_output
383	launch_prediction_eachB_ysei.py : extract from the prediction the values of the
384	MFs at the balloons place and altitude. Results stored in text format (".dat" in
385	${f Balloon_alt/Pred_output_Balloon_altitude/.}$
386	The next python scripts are cosmetic in the sense that they use the above two datasets
387	to make plots of timeseries balloon averaged values, evaluate correlations, and his-
388	tograms.
389	timeseries_obs_pred_plot_all.py Produces a lot of time series for each model
390	and flights.
391	Output data (Part2) As a result, you can visualize timeseries of each flight here:
392	$\mathbf{output}_ph1/\mathbf{Balloon_alt}/\mathbf{figure_timeseries}$
393	Histograms here: output_ph1/histo
394	Scatter plots and correlations here output_ph1/correlation
395	For phase 2, change ph1 in ph2.
396	xmgrace Alternative to calculate these diagnostics using fortran programs and xmgrace,
397	the programs permit to combine statistics over the 2 phases of Strateole2.

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⁶⁰² Supplementary: Phase 1 flights and models



⁶⁰³ Supplementary: Phase 1 flights and models (continued)



⁶⁰⁴ Supplementary: Phase 2 flights and models



⁶⁰⁵ Supplementary: Phase 2 flights and models (continued)



⁶⁰⁶ Supplementary: Phase 2 flights and models (continued)



⁶⁰⁷ Supplementary: Phase 2 flights and models (continued)

