

# Mini-Projects ocean

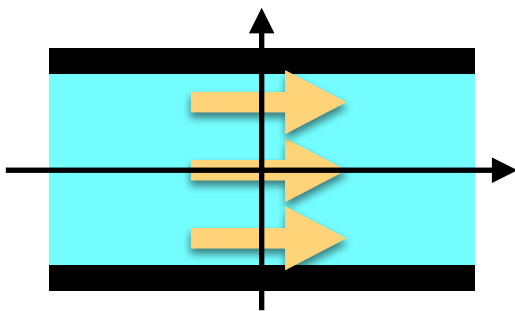
## 2. Formation of ocean eddies

The aim of this project is to characterize the destabilization of a barotropic jet in an east-west periodic channel, and the impact of the numerical schemes on the instabilities.

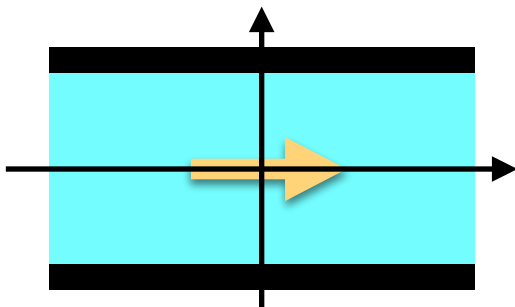
The basin has a flat bottom (no topographic obstacles) and is initially forced by a current in geostrophic balance, homogeneous in the along channel direction (x) and in vertical (z). For simplicity, Coriolis is either supposed to be constant (f-plane) or to vary linearly with latitude (beta plane) and the equation of state is linear in temperature. Density thus does not depend on salinity which can be used as a passive tracer for visualization purposes.

4 experiments will be designed by the students using the ocean model NEMO and the configuration called “CANAL”. The main idea is to find in which conditions a barotropic current can be destabilized

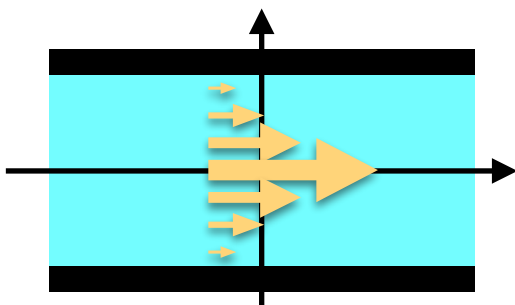
- 1) Uniform zonal current [f-plane and  $\beta$ -plane]



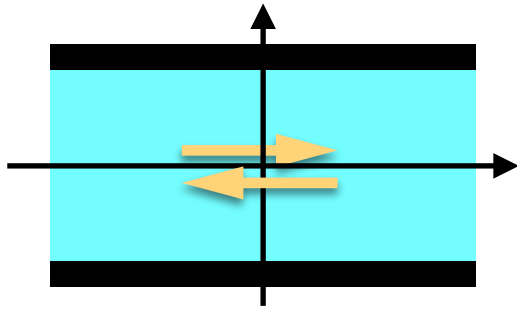
- 2) Zonal jet “uniform shape” (confined in between 2 latitudes) [f-plane and  $\beta$ -plane]



- 3) Zonal jet “gaussian shape” [beta-plane]



#### 4) Double jets “uniform shape” (high shear) [f-plane]



### Rappel: équilibre géostrophique

$$u_{\text{geostrophique}} = - \frac{1}{f\rho_0} \frac{\partial p}{\partial y}$$

$$v_{\text{geostrophique}} = + \frac{1}{f\rho_0} \frac{\partial p}{\partial x}$$

$$\frac{\partial p}{\partial z} = -\rho g$$

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$$

### le “plan f”

$$f = f_0 = 2\Omega \sin\varphi_0$$

### le “plan $\beta$ ”

$$f = f_0 + \beta y$$

$$\beta = 2\Omega \cos\varphi_0 / R_{\text{earth}}$$

To do:

- Design experiment (1) and show that the current stays in geostrophic equilibrium (in theory and in the model). tip: Find the expression of  $\eta$ , the height of the ocean surface above the reference  $z=0$ . Start with f-plane.

$$u = u_0$$

$$v = 0$$

$$\rho = \rho_0$$

- Design experiment (2)

- Run it. Do you see eddies forming? Why?
- Add a random noise to the background sea surface height. Do you see eddies? Why?
- Do we need the North-South walls?
- Design experiment (3)
  - Calculate (theoretically) which shape is unstable/stable depending on the latitude
  - Verify with the model's behavior
  - Characterize the instabilities (do they depend on the shape?)
  - Do we need the North-South walls?

Tips:

- the gaussian shape for the zonal current takes this form:  $u(x, y, z) = u_0 e^{-\frac{y^2}{2\lambda^2}}$

- the condition of instability (stabilizing effect of beta) is

$$\frac{\partial^2 u}{\partial y^2} - \beta \text{ change de signe} \Rightarrow \frac{\partial^2 u}{\partial y^2} = \beta$$

