

# Feedback and Sensitivity in Climate

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# Outline

- 1 Boundary layer processes in climate
  - Boundary layer as a boundary condition
  - Boundary layer and clouds
  - Boundary layer in the "Earth System"
- 2 Approaches to the parametrization of the boundary layer
  - Scale decomposition
  - Diffusive approaches and their limitations
  - Alternatives to diffusive approaches
- 3 Boundary layer, clouds and convection
  - Cloud schemes in climate models
  - Cumulus clouds and mass flux parametrisations
  - Boundary layer and deep convection

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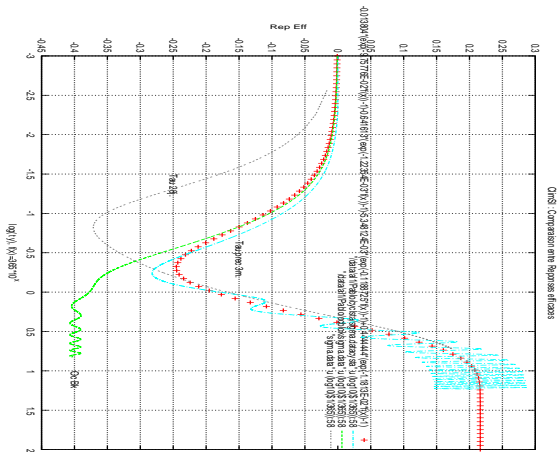


Figure: ClimSI WV feedback model responses.

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# Scale decomposition of the conservation equation

## Conservation equation

$\mathbf{v}$  : wind field

$c$  : conserved quantity ( $dc/dt = 0$ ),

$$\text{Advective form : } \frac{\partial c}{\partial t} + \mathbf{v} \cdot \text{grad} c = 0 \quad (1)$$

$$\text{Flux form : } \frac{\partial \rho c}{\partial t} + \text{div} (\rho \mathbf{v} c) = 0 \quad (2)$$

## Scale decomposition

$\bar{X}$  : "average" or "large scale" variable

$X' = X - \bar{X}$  : turbulent fluctuation

$$\overline{\mathbf{v}c} = \bar{\mathbf{v}}\bar{c} + \overline{\mathbf{v}'c'}$$

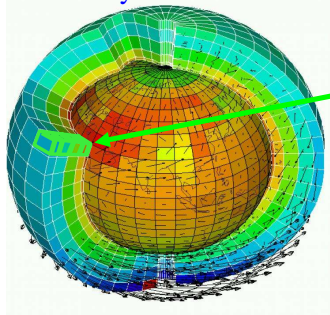
$$\frac{\partial \bar{q}}{\partial t} + \bar{\mathbf{V}} \cdot \text{grad} \bar{q} + \frac{1}{\rho} \text{div} (\overline{\rho \mathbf{v}'c'}) = 0 \quad (3)$$



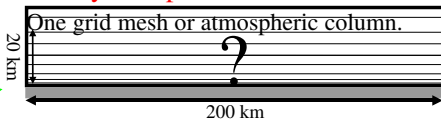
**Under boundary layer approximations ( $\partial/\partial x \ll \partial/\partial z$ ) :**

$$\frac{\partial c}{\partial t} + \mathbf{v} \cdot \mathbf{grad} \, c = S_c + \frac{1}{\rho} \frac{\partial}{\partial z} \overline{w'c'} \quad (4)$$

3D Dynamical core



Physical parametrizations



$c : \theta, u, v, \text{ water (vapor and others), chemical compounds ...}$

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# Diffusive or local formulations for the PBL

$$\overline{w'c'} = -K_z \frac{\partial c}{\partial z} \quad \longrightarrow \quad \frac{\partial c}{\partial t} = \frac{\partial}{\partial z} \left( K_z \frac{\partial c}{\partial z} \right) \quad (5)$$

- Analogy with molecular viscosity.
- Down-gradient fluxes.
- Turbulence acts as a "mixing"

# Turbulent diffusivity $K_z$

- Prandtl (1925) mixing length :  $K_z = l|\overline{w'}|$  or  $K_z = l^2 \frac{\partial ||\mathbf{v}||}{\partial z}$
- Accounting for static stability (Ex. Louis 1979)

$$K_z = f(Ri)l^2 \left| \frac{\partial \mathbf{v}}{\partial z} \right|, \quad \text{with } Ri = \frac{g}{\theta} \frac{\frac{\partial \theta}{\partial z}}{\left( \frac{\partial \mathbf{v}}{\partial z} \right)^2} \quad (6)$$

- Turbulent kinetic energy  $\overline{w'^2} \simeq e = \frac{1}{2} \left[ \overline{u'^2} + \overline{v'^2} + \overline{w'^2} \right]$

$$\frac{\partial e}{\partial t} = -\overline{w'u'} \frac{\partial u}{\partial z} - \overline{w'v'} \frac{\partial v}{\partial z} - \frac{g}{\theta} \overline{w'\theta'} - \frac{1}{\rho} \frac{\partial \overline{w'p'}}{\partial z} - \frac{\partial \overline{w'e}}{\partial z} - \epsilon \quad (7)$$

Ex : Mellor and Yamada  $\overline{w'\phi'} = -K_\phi \frac{\partial \phi}{\partial z}$  with  $K_\phi = l\sqrt{2e}S_\phi(Ri)$

Note : Imposing  $\frac{\partial e}{\partial t}$  gives a coefficient of the form Eq. 6

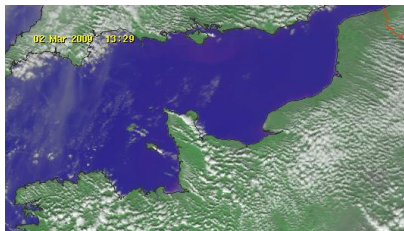
# Limitations of turbulent diffusion

## Diffusive approach :

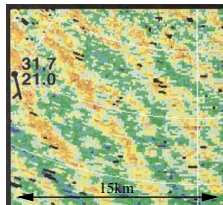
- Random process
- Small scale turbulence of size  $l \ll h$  with  $h = \left[ \frac{1}{c} \frac{\partial c}{\partial z} \right]^{-1}$

## Real turbulence

- Long range vertical transport (from the bottom to PBL top)
- Organized structures



Cloud streets on North of France  
(March 2009, MSG)

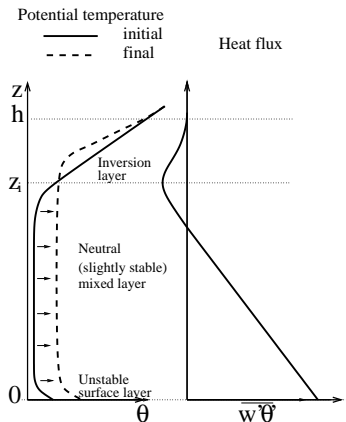


Radar echoes in a dry convective  
boundary layer

# Limitations of turbulent diffusion

Idealized view of the dry convective boundary layer.

## In the mixed layer



- Diffusive formulation

$$\overline{w'\theta'} = -K_z \frac{\partial \theta}{\partial z} = 0 \quad \text{or slightly } < 0 \quad (8)$$

- Uniform heating by the surface

$$\frac{\partial \theta}{\partial t} \simeq \frac{\overline{w'\theta'}_0}{z_i} (\text{Cste} > 0) \quad (9)$$

$$\overline{w'\theta'} \simeq \frac{z - z_i}{z_i} \overline{w'\theta'}_0 > 0 \quad (10)$$

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# Extension of diffusive formulations

- **Introduction of a countergradient term**

$$\overline{w'\theta'} = -K_z \left[ \Gamma - \frac{\partial \theta}{\partial z} \right] = 0 \quad \text{with } \Gamma \simeq -1K/km \quad (11)$$

Imposed countergradient Deardorf, 1966

Revisited by Troen & Mart, 1986, Holtzlag & Boville, 1993,  
based on a similarity approach.

- **Higher order closures**

Abdella & Mc Farlane, 1997, Randall et al., 1992, Lapen &  
Ransall, 2002

(12)



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