Wakes tbd

July 3, 2025

1 Abstract

Pas de citations dans l'abstract Cold pools, formed under clouds by the evaporation of precipitation, play a central role in maintaining and organizing atmospheric convection~~(Rotunno et al., 1988; Weisman and Rotunno, 2004; Jeevanjee and Romps, 2013)~~. Their absence in climate models leads to significant errors in the representation of convection, such as premature convection onset~~, and underestimation of precipitation rates (Randall et al., 2003; Gu~~ . The introduction of ~~the~~ a cold pools parameterization proposed by ~~Grandpeix and Lafore (2010)~~ into the LMDZ climate model has significantly improved the representation of convection~~(Rio et al., 2009)~~, in particular with regard to its diurnal cycle. However, this parameterization had never been finely evaluated before in terms of representation of the cold pools themselves. This work provides ~~a detailed evaluation of this parameterization in LMDZ,~~ for the first time such an evaluation based on Large Eddy Simulation (LES)~~, an approach that had never been explored before. We evaluated~~ . We evaluate the underlying physics of the model, its internal variables as well as those used in the coupling with the deep convection scheme. The LES analyses demonstrate the relevance of the assumptions underlying the parameterization. We also show that its initial version represents well, at first order, the characteristics of the cold pools, although some biases were identified. These were corrected thanks to substantial modifications made to the cold pools scheme and a readjustment of some free parameters. Persistent defects can be corrected by adding thermal-related mixing in the cold pools and by considering evolution of their density in a more physical way.

2 Introduction

During thunderstorms, a significant amount of precipitation evaporates before reaching the ground, generating cold air masses in the layers below the clouds. This cooled air, denser than its surroundings, collapses and then spreads horizontally across the surface, forming what are called cold pools. These are often associated with a gust front, capable of lifting the surrounding warm air and thus promoting the development of new convective cells. In organized propagative systems such as squall lines, convective columns are permanently generated by cold pool fronts at the front of the system (Rotunno et al., 1988; Weisman and Rotunno, 2004). When the cold pools is accompanied by a gust front, it is called a density current. These density currents are fueled by precipitating downdrafts, which is their main dynamic driver. Although present over both continents and oceans, density currents are generally deeper, colder, and propagate more rapidly over continents. They play a key role in the self-aggregation of tropical convection (Jeevanjee and Romps, 2013), as well as in the transition between shallow and deep convection (Khairoutdinov and Randall, 2006; Böing et al., 2012).

In atmospheric Global Circulation Models (GCMs), as those used for climate change studies, convection has to parameterized due to the coarse horizontal resolution (30 to 300 km). Simulating convective rainfall with parameterized physics is challenging (Randall et al., 2003). GCMs often underestimate rainfall rates (Kendon et al., 2012; Pantillon et al., 2015; Tan et al., 2018) and produce peak precipitation at noon, in phase with insolation, while the maximum precipitation is generally observed in late afternoon or during night (Randall et al., 2003; Guichard et al., 2004; Stephens et al., 2010; Dirmeyer et al., 2012). Density currents probably play a key role in this timing, by self-maintaining convection (Pantillon et al., 2015; Grant et al., 2018). One of the first attempts to parameterize density currents was proposed by ~~(Qian et al., 1998)~~Qian et al. (1998). Later on, ~~(Grandpeix and Lafore, 2010)~~ Grandpeix and Lafore (2010) proposed a parameterization based on a population of identical circular density currents that are cooled by convective precipitation. The coupling of the ~~(Emanuel, 1991)~~ Emanuel (1991) parameterization of deep convection with this cold pool parameterization and with the thermal plume model of Rio and Hourdin (2008) in the LMDZ climate model significantly improved the simulation of the diurnal cycle of precipitation in the tropics (Rio et al., 2009), shifting its maximum from noon to mid afternoon. A further improvement was brought by the introduction of the stochastic triggering of deep convection Rochetin et al. (2014) which made the simulated convection more intermittent. Despite this success, and the use of the cold pool model in the standard version of the LMDZ atmospheric and IPSL (Institut Pierre Siméon Laplace) coupled models (Hourdin et al., 2020; Boucher et al., 2020), it was not evaluated in details so far. This is explained not only by a lack of observational data but also by the fact that the internal variables of parameterizations are not directly accessible from observations.

Large Eddy Simulations (LES) are a useful complement to observations. Their fine horizontal resolution enables them to simulate explicitly turbulent and convective motions in the boundary layer (Brown et al., 2002; Siebesma et al., 2003). One advantage of

LES compared to observations is that they provide full three-dimensional information. They have been used extensively to develop and evaluate boundary layer and convection parameterizations (Rio et al., 2010; Dorrestijn et al., 2013; Strauss et al., 2019; Legay et al., 2025). LES have been used also to simulate, understand and develop parameterizations of cold pool parameterizations (Tompkins, 2001; Khairoutdinov and Randall, 2006; Couvreux et al., 2012; Feng et al., 2015; Kurowski et al., 2018). However, their use for a cold pool parameterization assessment remains unexplored.

Here we propose to use LES to evaluate in details the parameterization of cold pools of LMDZ (Grandpeix and Lafore, 2010; Grandpeix et al., 2010). We first use LES to evaluate some of the fundamental relationships between large scale state variables (for LES, the horizontal average over the domain) and internal variables which are at the basis of the parameterization. We then propose improvements which are further assessed in simulations with a Single-Column-Model (SCM) version of LMDZ against LES. In such simulations, the parameterization interact with all the other parameterizations and depend on the values of a number of free parameters. To explore the sensitivity of the results to those free parameters and retune the model after improvement of its physical consent, we use a tool for automatic calibration, High-Tune-Explorer, developed recently (Couvreux et al., 2021; Hourdin et al., 2021). This tool, based on history matching, can be used to characterize the subspace of parameter values for which the model is in agreement with LES, given a series of target metrics and associated tolerance to error (Couvreux et al., 2021). It is used here to explore the sensitivity of the agreement between SCM simulations and LES to the model free parameters.

The paper starts by ~~a presentation of~~ presenting in the section 1 the tools used ~~, including~~ : the LMDZ model, the cold pool parameterization by ~~Grandpeix and Lafore (2010),~~ Grandpeix and Lafore (2010) (referred to as the GL10 ~~model, and LES~~hereafter), and the LES used for evaluation. The presentation of the tuning tool (largely published) and the setup of its use is let to an appendix to concentrate on model physics and improvement in the core of the paper. In section 2, we detail the ~~sampling of cold pools carried out in LESand used~~ cold pool sampling in LES, designed to assess the physical laws internal to the cold pool parameterization and its coupling with deep convection. Section 3 is devoted to a comparison of cold pool model variables simulated by LMDZ in SCM mode and those calculated in LES, in order to identify the model's limitations. These results will then be discussed, and proposed improvements will be detailed in section 4. Finally, we conclude with a synthesis and discussion of prospects in section 5.

3 Tools and methods

3.1 LMDZ and its single-column version

LMDZ is the General Circulation Model (GCM) used in this work. Developed in the 1970s at the Laboratoire de Meteorologie Dynamique (Sadourny, 1984; Hourdin et al., 2006), the "Z" in LMDZ refers to the model's ability to refine its horizontal grid over a specific region.

This climate model is based on simplified Navier-Stokes equations for fluid mechanics, as well as transport equations. It represents the second generation (Hourdin et al., 2013) of a climate model initially described by Sadourny and Laval (1984). LMDZ is the atmospheric component of the IPSL coupled model. The latter is one of around twenty coupled models taking part in major international model intercomparison exercises, such as those of the CMIP (Coupled Model Intercomparison Project), the results of which are used in IPCC (Intergovernmental Panel on Climate Change) reports.

LMDZ consists of two main parts, from a physical, mathematical and computational point of view. The first part, called "the dynamics", concerns the numerical resolution of the atmospheric general circulation equations. This component manages horizontal exchanges between the model's grid cells. The second part, called "physics", calculates the impact of radiation, small-scale processes (subgrid) and phase changes of water on dynamic variables via "physical parameterizations". This "physical" part is made up of juxtaposed atmospheric columns, which do not interact with each other. Within each column, the variables are assumed to be statistically homogeneous in the horizontal plane. **Le 1D/LES n'est pas une obligation et n'est vraiment utilisé que pour les paramétrisations de la convection et des nuages**

The SCM version of LMDZ is built by extracting an atmospheric column from the GCM, incorporating all subgrid-scale parameterizations, and running it in a large-scale constrained environment. This ~~tool is essential for~~ approach has become central in the development and tuning of ~~physical parameterizations in climate models~~parameterizations of convection and associated clouds in several climate modeling groups. Parameterizations are often developed and evaluated within this single-column framework by comparing them with LES of the same atmospheric column. The SCM/LES approach was ~~developed within the framework of the~~ promoted in particular by GCSS (GEWEX Cloud Systems Study), a program aimed at improving the parameterization of cloud systems in climate models ~~((*ref*))~~**ref**. A major advantage of the SCM is its low computational cost, which allows a large number of simulations, even on a laptop, making it particularly useful in the development phase, where extensive testing is required.

Pas possible de partir à ce point bille en tête je trouve, sans avoir un peu dressé le portrait des paramétrisations de la convection dans le modèle.

The parameterization of turbulence, convection and clouds in LMDZ is based on a multi-scale, or object view. The small scale turbulence, mainly active near the surface, is accounted for following Yamada (1983) scheme, with an eddy diffusive approach in which the eddy diffusivity relies on a prognostic equation for the turbulent kinetic energy. A specific mass flux parameterization, the thermal plume model, accounts for the vertical transport by organised thermal plume, cells or rolls in the convective boundary layer Hourdin et al. (2002); Rio and Hourdin (2008). It was later on coupled to a bigaussian statistical representation of the subgrid distribution of humidity, leading to a strong improvement in the representation of cumulus and stratocumulus clouds Jam et al. (2013); Hourdin et al. (2019) . Deep convection is represented with a modified version of the Emanuel (1991) scheme.

En mettre suffisamment ici pour introduire déjà les thermes Q1 et Q2, unsat n'co. Pour les avoir sous la main plus loin

The main modification of the deep convection scheme concerns the triggering and closure ... **Compléter Les phrases ci-dessous sont reprises de l'introduction. Il faut peut être les enlever plus haut ? Introduire Strig puisqu'on l'utilise plus loin** proposed a parameterization based on a population of identical circular density currents that are cooled by convective precipitation. Later on, Grandpeix and Lafore (2010) model of Rio and Hourdin (2008) in the LMDZ climate model significantly improved the simulation of the diurnal cycle of precipitation in the tropics (Rio et al., 2009), shifting its maximum from noon to mid afternoon. A further improvement was brought by the introduction of the stochastic triggering of deep convection Rochetin et al. (2014) which made the simulated convection more intermittent.

3.2 The cold pool model

The cold pool model represents a population of identical circular cold pools (the wakes) over an infinite plane containing the grid cell. All the wakes have the same height, radius, and vertical profiles of thermodynamic variables. Their centers are statistically distributed with a uniform density D_{wk}. Cold pools divide the space into two parts : (i) the interior of cold pools (w) is where convective precipitating downdrafts are located; in these downdrafts, the re- evaporation of precipitation generates intense cooling and strong negative buoyancy; (ii) the exterior of cold pools (x) contains the warm air that fuels the saturated convective currents (Fig. 1). The top height of the cold pool (h_{wk}) is defined as the altitude where the temperature difference between (w) and (x) becomes zero. Below this level cold pools are cooler than their exterior: they collapse and spread out as they are denser than ~~their surrounding~~ the surrounding air. The boundary between the cold pool and the environment is considered to be infinitely thin, and at each point on this boundary, the cold pool spreads at a rate C. C is considered to be a random variable whose mean ~~C_*~~ C_* will give the rate at which the cold pool spreads. In the GL10 model, ~~C_*~~ C_* scales with the square root of the potential energy available in the cold pools, i.e the cold pool's collapse energy, $WAPE$ (Wake Available Potential Energy), given by:

$$WAPE = g \int \frac{\delta\rho}{\overline{\rho}} = -g \int_0^{h_{wk}} \frac{\delta\theta_v}{\overline{\theta_v}} dz \tag{1}$$

so that:

$$C_* C_* = k\sqrt{2WAPE} \tag{2}$$

where ρ is the air density; θ_v is the virtual potential temperature.

~~δX~~ For any variable X, $\delta X = X_w - X_x$ is the difference ~~in the variable X between (w) and (x) ($\delta X = \delta X_w - \delta X_x$)~~ of its mean value in the two subdomain and $\overline{X}$ ~~is the mean of the variable X in the domain.~~ the average over the horizontal domain.

~~The coefficient~~ **Il faut faire attention. Ici on décrit le model. Dans le modèle, k ne dépend pas de la structure des poches. Il est fixé. C'est important de faire la distinction pour bien que le lecteur comprenne le modèle. On impose une**

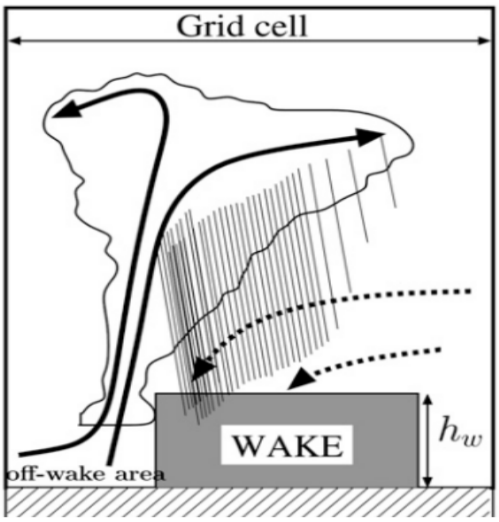

Figure 1: Conceptual diagram of a density current (Grandpeix and Lafore, 2010).

proportionalité entre deux choses. On ne peut même pas dire que ce coefficient dépend de quelque chose. C'est un modèle. Dans des développement ultérieur, on peut imaginer ... So far, k in equation (2) ~~, generally~~ is fixed, to a value between 0 and ~~1, depends~~ 1. This coefficient should probably depend on the structure of cold pools. Based on 3D CRM (Cloud Resolving Models) simulations, Lafore (2000) (oral communication) estimated this coefficient at 0.33 in the case of a linear structure such as squall grain. This is the value used in the GL10 model.

The spread rate of cold pools ~~is given by C_*~~ C_* is deduced from the following relationship :

$$\partial_t \sigma_{wk} = 2\pi r C_* r C_* D_{wk} = 2C_* 2C_* \sqrt{\pi D_{wk} \sigma_{wk}} \tag{3}$$

where σ_{wk} is the surface fraction covered by cold pools ($\sigma_{wk} = D_{wk}\pi r^2$). Due to the complex life cycle of cold pools (including birth, death, collisions and mergers), calculating their ~~evolution~~ number density requires an other parameterization. In GL10 model, so far in its LMDZ implementation, and in this study, ~~their~~ the value of the cold pool number density is imposed. In ~~the GL10 model,~~ standard configurations of LMDZ, **C'est dans LMDZ ou vraiment dans GL10 ?** this density is ~~imposed at~~ fixed to a different value over ocean (10.10^{-10} m^{-2}, i.e. 10 cold pools over 100 km×100 km~~over the ocean, while~~) and over the continent ~~it is imposed at~~ (8.10^{-12} m^{-2}, i.e. around 8 cold pools over 1000 km×1000 km). In the GL10 model, cold pools initially appear with a surface fraction of 2% and evolve over time according to equation 3. The evolution of σ_{wk} is arbitrarily limited to a maximum of 40% ($\sigma_{wk} \leq 0.4$).

les 2% et 40% sont des paramètres ajustables fondamentalement.

It is assumed that below the top of cold pool (h_{wk}), the vertical velocity profile associated with the subsidence of the cold pool results solely from the spreading ~~of cold pool~~ at the surface, without lateral entrainment (e_w) or detrainment (d_w) between the

cold pool and its environment. Above ~~cold pool, there is the existence of a meso-scale subsidence initiated below the stratiform cloud (at altitude h_m fixed at 600hPa in GL10 model) driven by~~ this level, the ~~evaporation of precipitation and that brings θ_e from the mid-troposphere above~~ subsidence is driven both by the need to fed the subsidence in the cold pool ~~top. h_m is considered the altitude above which the thermodynamic differences between the cold pools and their exterior become negligible, except within convective currents (saturated currents in (x), unsaturated descending currents in (w)) . In the GL10 model, the~~ (air mass continuity equation) and by the additional reevaporation of rainfall bellow stratiform clouds. The shape of the vertical ~~velocity difference profile ($\delta\omega$(P))~~ profile of the velocity difference $\delta\omega$ is imposed as ~~piecewise linear~~a piecewise linear function of pressure: $\delta\omega$ increases linearly from zero at the surface up to a maximum value at h_{wk} ~~. Between~~ and then decreases linearly between h_{wk} and a maximum height at which it vanishes : h_m. The vertical subsidence which thus increases downward between h_m and h_{wk} is fed by lateral entrainment ($e_w > 0$) without detrainment. This lateral entrainment accounts for the horizontal component of the meso-scale circulation known to entrain air from low- or mid- tropospheric air into the cold pool. **Pour moi il est très importants qu'on se mette d'accord sur le paragraphe ci dessus, et que Lamine comprenne l'importance des ces discussions**

At h_m, ~~$\delta\omega$ decreases linearly.~~ the top of the cold pool model, δ_X, cancels for all cold pool state variables.

In GL10 model, h_m was set to 600 hPa and there was also a nonzero velocity difference ($\delta\omega^{cv}$) at h_m, accounting for the difference of the convective mass fluxes between (w) and (x). In the version use on the paper, this difference is now zero ($\delta\omega^{cv} = 0$) above this level.

The evolution of the potential temperature difference ($\delta\theta$) between (w) and (x) is controlled by differential heating (δQ_1^{cv}, δQ_1^{wk}) due to deep convection and cold pools, as well as by damping due to gravity waves (τ_{gw}). The humidity difference (δq) follows a similar pattern, but without the damping effect of gravity waves. Heat sources are replaced by moisture sources (δQ_2^{cv} for convection and δQ_2^{wk} for cold pools).

$$\begin{cases} \partial_t \delta\theta = -\overline{\omega}\partial_p \delta\theta + \frac{\delta Q_1^{wk} + \delta Q_1^{cv}}{C_p} - \frac{K_{gw}}{\tau_{gw}}\delta\theta, \\ \\ \partial_t \delta q = -\overline{\omega}\partial_p \delta q + \frac{\delta Q_2^{wk} + \delta Q_2^{cv}}{L_v}. \end{cases} \tag{4}$$

where ~~$\tau_{gw} = \frac{\sqrt{\sqrt{\sigma_{wk}} - (1 - \sqrt{\sigma_{wk}})}}{4Nz\sqrt{D_{wk}}}$~~

~~τ_{gw} represents~~

$$\tau_{gw} = \frac{\sqrt{\sqrt{\sigma_{wk}} - (1 - \sqrt{\sigma_{wk}})}}{4Nz\sqrt{D_{wk}}} \tag{5}$$

is estimated as the time required for a wave with speed Nz to travel a distance equal to the geometric mean of the cold pool size and the interval between cold pools. C_p is the heat capacity of dry air, N is the Brunt-Väisälä frequency, and z is altitude. K_{gw} is an efficiency of gravity waves. Finally, L_v is the latent heat of vaporization of water.

δQ_1^{wk} (respectively δQ_2^{wk}) depend on the entrainment (e_w) of dry air, the differential advection of $\overline{\theta}$ (respectively $\overline{q}$) and $\delta\theta$ (respectively δq). :

$$\begin{cases} \frac{\delta Q_1^{wk}}{C_p} = \frac{e_w}{\sigma_{wk}}\delta\theta - \delta\omega\partial_p\overline{\theta} - (1-2\sigma_{wk})\delta\omega\partial_p\delta\theta \\ \frac{\delta Q_2^{wk}}{L_v} = \frac{e_w}{\sigma_{wk}}\delta q - \delta\omega\partial_p\overline{q} - (1-2\sigma_{wk})\delta\omega\partial_p\delta q \end{cases} \tag{6}$$

Similarly, δQ_1^{cv} (respectively δQ_2^{cv}) are ~~influenced by heating trends~~ computed from the by heating tendencies associated with unsaturated currents ($Q_{cv}^{1,unsat}$, or $Q_{cv}^{2,unsat}$ for humidity) and saturated currents ($Q_{cv}^{1,sat}$, or $Q_{cv}^{2,sat}$ for humidity).

$$\begin{cases} \frac{\delta Q_1^{wk}}{C_p} = \frac{e_w}{\sigma_{wk}}\delta\theta - \delta\omega\partial_p\overline{\theta} - (1-2\sigma_{wk})\delta\omega\partial_p\delta\theta \\ \frac{\delta Q_2^{wk}}{L_v} = \frac{e_w}{\sigma_{wk}}\delta q - \delta\omega\partial_p\overline{q} - (1-2\sigma_{wk})\delta\omega\partial_p\delta q \end{cases}$$

:

$$\begin{cases} \delta Q_1^{cv} = \frac{Q_{cv}^{1,unsat}}{\sigma_{wk}} - \frac{Q_{cv}^{1,sat}}{1-\sigma_{wk}} \\ \\ \delta Q_2^{cv} = \frac{Q_{cv}^{2,unsat}}{\sigma_{wk}} - \frac{Q_{cv}^{2,sat}}{1-\sigma_{wk}} \end{cases} \tag{7}$$

$Q_{cv}^{x,unsat}$ and $Q_{cv}^{x,sat}$ ($x = 1, 2$) are given by the deep convection scheme but we will not go into details here.

Entrainment is determined from the vertical gradient of $\delta\omega$ and the cold pool spreading rate, according to the following relationship:

Bien vérifier la formule ci dessous. Elle ne me saute pas aux yeux

$$e_w = \sigma_{wk}(1-\sigma_{wk})\partial_p\delta\omega + \partial_t\sigma_{wk} \tag{8}$$

Equation 4, via the variables δQ_1^{cv} and δQ_2^{cv}, describes the impact of deep convection on cold pools which results in their cooling due to precipitating descents, as discussed above.

The cold pool model is now fully described. It includes:

- three prognostic variables, derived directly from the model equations: the profiles of $\delta\theta$ and δq and σ_{wk}.
- two diagnostic variables, evaluated from the profile of $\delta\theta$: h_{wk}, C_* and $WAPE$
- three main free parameters: the coefficient k, the density D_{wk} and τ_{gw} **Est-ce qu'on ne veut pas mettre les surfaces min et max ? Et d'autres peut être ?**

3.3 ~~The~~ Coupling with deep convection model

In LMDZ, the deep convection scheme used is based on that of Emanuel (1991), with modifications made by Grandpeix et al. (2004). The main modifications concern the conditions under which deep convection is triggered and closed.

Deep convection is triggered when the Available Lifting Energy (ALE) exceeds the convective inhibition (CIN) threshold. This can be caused either by uplift energy from the convective boundary layer (ALE_{bl}), provided by the thermals model (Rio and Hourdin, 2008), or by energy generated by cold pools (ALE_{wk}).

$$\max(ALE_{bl}, ALE_{wk}) > |CIN| \tag{9}$$

Deep convection triggering occurs when For deep convection triggering by thermal plumes, an additional condition is required: at least one cumulus cloud in a mesh exceeds a given size, specified by S_{trig}. For this, a probability of non-triggering is estimated, based on the characteristics of the spectrum of type 2 thermals (N_2, S_2) derived from the original thermal plume model (Rio and Hourdin, 2008)$and S_{trig}$, according to the relationship proposed by Rochetin et al. (2014).

$$P_{\Delta t} = ([1 - exp(\frac{-S_{trig}}{S_2})]^{N_2})^{\frac{\Delta t}{\tau}} \tag{10}$$

where Δt is the model time step; τ is the decorrelation time between cloud scenes. $S2$, representing the mean effective cross-sectional area of cloud base thermal currents, is determined by the following relation:

$$S_2 = [a(\overline{Z_{top}} - \overline{Z_{lcl}}) + b\overline{Z_{lcl}}]^2 \tag{11}$$

where Z_{top} is the mean cloud depth; Z_{lcl} is the mean cloud base altitude; a and b are free parameters

$N2$ is the corresponding thermal population in the mesh and is calculated from the following relation:

$$N_2 = \frac{(1-\epsilon)\alpha_{tot} S_d}{S_2} \tag{12}$$

where α_{tot} is the surface covered by thermals; S_d is the surface of the domain

In this framework, deep convection is triggered by thermals whenever a uniform random number R, between 0 and 1, exceeds the non-trigger probability.

$$R > P_{\Delta t} \tag{13}$$

The intensity of the convection depends on the mass flux (M_b) at the cloud base, determined by ALP, provided by thermals (ALP_{bl}) and cold pools (ALP_{wk}).

$$M_b = k\frac{ALP_{bl} + ALP_{wk}}{(2w_b^2 + |CIN|)} \tag{14}$$

where k and w_b are free parameters.

The two variables ALE_{wk} and ALP_{wk}, to take account of the effect of cold pools on convection, have been introduced into the cold pools model by Grandpeix et al. (2010).

To calculate ALE_{wk}, the model assumes that the maximum speed (C_{max}Cmax) on the cold pool contour will trigger convection. This is assumed to be proportional to the square

root of $WAPE$, with a higher coefficient of proportionality here (arbitrarily estimated at 1), leading to the following relationship:

$$C_{max} C_{\max} = k' \sqrt{2 WAPE} \tag{15}$$

where $k' = 1$

Il faut peut etre mieux dire ce qu'on a en tête en distinguant C* et Cmax. Et on aura un joli modèle de ca avec la distribution sous maille du vent. J'avais pas complètement réalisé ... Cmax sort tout seul du modèle de vent.

The Available Lifting Energy associated with cold pools is thus expressed by the following relationship :

$$ALE_{wk} = \frac{1}{2} C_{max} C_{\max}^2 \tag{16}$$

Combining equations (16) and (15) gives the expression for ALE_{wk} below:

$$ALE_{wk} = k'^2 WAPE \tag{17}$$

With $k' = 1$, this equation says that, in the cold pool model, the Available Lifting Energy associated with cold pools is equal to the collapse energy.

ALP_{wk} is calculated ~~by~~ assuming that cold pools exert a horizontal power on the surrounding air during its spreading. This horizontal power is then converted into vertical power. During this conversion, the model assumes that a large part of the horizontal power is dissipated, and that only 25% contributes to increasing the intensity of convection.

Each cold pool generates its own lifting power, depending on its spreading speed (C_*), height (h_{wk}) and the length (L_g) of its gust front. The total power (ALP_{wk}) of the cold pools is the product of the power supplied by each pool ~~and their~~ times the cold pool number density (D_{wk}).

$$ALP_{wk} = \epsilon \frac{1}{2} \rho C_*^3 h_{wk} L_g D_{wk} \tag{18}$$

where $\epsilon = 0.25$ is the lifting efficiency with

$$L_g = 2\pi r \tag{19}$$

$$\sigma_{wk} = D_{wk} \pi r^2 \tag{20}$$

Then, the lifting power ALP_{wk} reads :

$$ALP_{wk} = \epsilon \rho C_* {C_*}^3 h_{wk} \sqrt{\sigma_{wk} D_{wk} \pi} \tag{21}$$

3.4 Large Eddy Simulations

Large Eddy Simulations (LES) are numerical tools for simulating atmospheric phenomena with a horizontal resolution of tens to hundreds of meters. They are particularly well suited to the study of the thermodynamic structure of the boundary layer, as they resolve the eddies that form there. They offer an explicit and detailed representation of turbulent and convective movements within the boundary layer and associated clouds (Brown et al., 2002; Siebesma et al., 2003). ~~While they are able to reproduce atmospheric thermodynamics and structure satisfactorily, the representation of cloud characteristics remains more delicate. They enable fairly direct simulation of turbulent and convective movements.~~ **Les phrases barrées n'ajoutent rien** In the presence of water phase changes, however, these simulations can become ~~highly dependent their~~ more dependent on the microphysical schemes used. One of the major strengths of LES lies in its ability to provide three-dimensional information not available from observations, making then an indispensable complement to the latter for understanding processes. In addition, LES can be used to validate the internal variables of parameterizations, enabling their physical realism to be assessed. They have been used to evaluate boundary layer and convection parameterizations (Rio et al., 2010). In recent years, they are increasingly used to document the characteristics of cold pools and guide their parameterization (Couvreux et al., 2012; Feng et al., 2015).

In this study, we use the outputs of two oceanic LES and one continental LES.

Both oceanic LES were carried out in Radiative-Convective Equilibrium (RCE) mode. RCE is a concept in which equilibrium is achieved between convective heating and radiative cooling of the atmosphere. A detailed description of RCE simulation protocols is provided in Daleu et al. (2015). In the RCE simulations used here, radiative computation is replaced by a constant cooling of -1.5 K per day, while the surface temperature is imposed. The destabilization leads to convection. The associated heating rate, largely corresponding to the release of latent ~~heat~~heatby cloud condensation in convective towers, compensates for the cooling once quasi-equilibrium has been reached. Two oceanic LES of this RCE are used here, one is performed with the SAM model (Khairoutdinov and Randall, 2003) and the other one with MesoNH (Lac et al., 2018). Both simulations cover an oceanic domain of 200 km×200 km with horizontal resolution of 25 m. The lateral boundary conditions are cyclic for both models. The sea surface temperature is set at 300 K. These two RCE simulations run for 44 days, with ~~equilibrium reached on simulation day 40.~~ quasi steady-state regime reached after about 40 days. Output frequency for LES SAM is set to every 3 hours, while that for LES MesoNH is set to every 24 hours.

The continental LES is based on the AMMA (African Monsoon Multidisciplinary Analysis) case. This case is derived from observations made on July 10, 2006 during the AMMA field campaign (Redelsperger et al., 2006), during which a relatively small, short-lived convective system formed over Niamey (Couvreux et al., 2012; Lothon et al., 2011). This system, with a lifetime of around 6 hours, was observed by various instruments (radar and atmospheric soundings), supplemented by satellite data. This case study represents a typical example of deep convection in the Sahel regions. LES for this continental case is carried out with the MesoNH model over a 100 km × 100 km domain, with a horizontal

resolution of 200 m. Lateral boundary conditions are cyclic and surface fluxes are imposed. Outputs are generated at a frequency of 10 minutes.

4 Assessment of the cold pool model internal equations from LES

4.1 Sampling of cold pools

In order to use LES for the assessment of the cold pool parameterization, the first challenge is to separate cold pools from their environment. Indeed, there is no a priori established framework for objectively identifying cold pools in observations and numerical models (Rochetin et al., 2021), and choices may depend in part on the physical picture one has of cold pools, and also, for the purpose at hand, on the picture underlying the parameterization. The first method for identifying cold pools proposed by Young et al. (1995) was based on surface precipitation rates. In more recent studies, such as those by ~~Provod et al. (2016); Zuidema et al. (2017); Vogel et al. (2021); Rochetin et al. (2021); Touzé-Peiffer e~~ (Provod et al., 2016; Zuidema et al., 2017; Vogel et al., 2021; Rochetin et al., 2021; Touzé-Peiffer et al , the detection of cold pools is closer to a density current oriented detection, in which variations in temperature, pressure and wind are taken into account.

In the present study, the aim is not to isolate individual "cold pools objects", but only to know whether a grid box is inside or outside a cold pool. Also the boundary conditions are idealized targeting the statistical homogeneity assumption that is at the basis of the Reynolds decomposition between dynamical core and physics parameterizations. In this idealized case with uniform surface temperature, cold pools can be identified fairly immediately using a threshold on the anomaly (after removing the domain average) of temperature at 10 m above surface~~(T_{10m}, first model layer)~~, $T_{10\mathrm{m}}$, i.e. at the first model mid layer.

~~The map of divergence of~~ Fig. 2 and Fig. 3 show a horizontal sliding average with a box of 3.25 km×3.25 km of the divergence of the wind at 10 m ~~, smoothed on a 3.25 km×3.25 km box, enables us to visually identify~~ above surface, $\overrightarrow{V_{10\mathrm{m}}}$. From these maps, the centers and gust fronts of cold pools ~~, represented respectively by~~ can be easily identified, corresponding respectively to the maximum and minimum of divergence values~~(and)~~. Maxima of divergence of surface wind indicate the center of cold pools where cold air masses collapse. Precipitation is generally co-located with these divergence maxima (not shown). The fairly strong wind convergence observed around cold pools centers corresponds to the strong lift of air masses created upstream of the gust front at the cold pool's periphery.

Both the ~~LES in RCE~~ two LES of the RCE case and the LES ~~in~~ of the AMMA case show cold pools groupings (or very close cold pools centers) forming a common gust front. This can be explained by the fact that, during propagation, cold pools can merge to create a single, larger cold pools. We can also observe that wind convergence is generally more intense between the centers of grouped cold pools, indicating that updrafts of air masses associated with gust fronts is more pronounced when these cold pools meet. This is in line

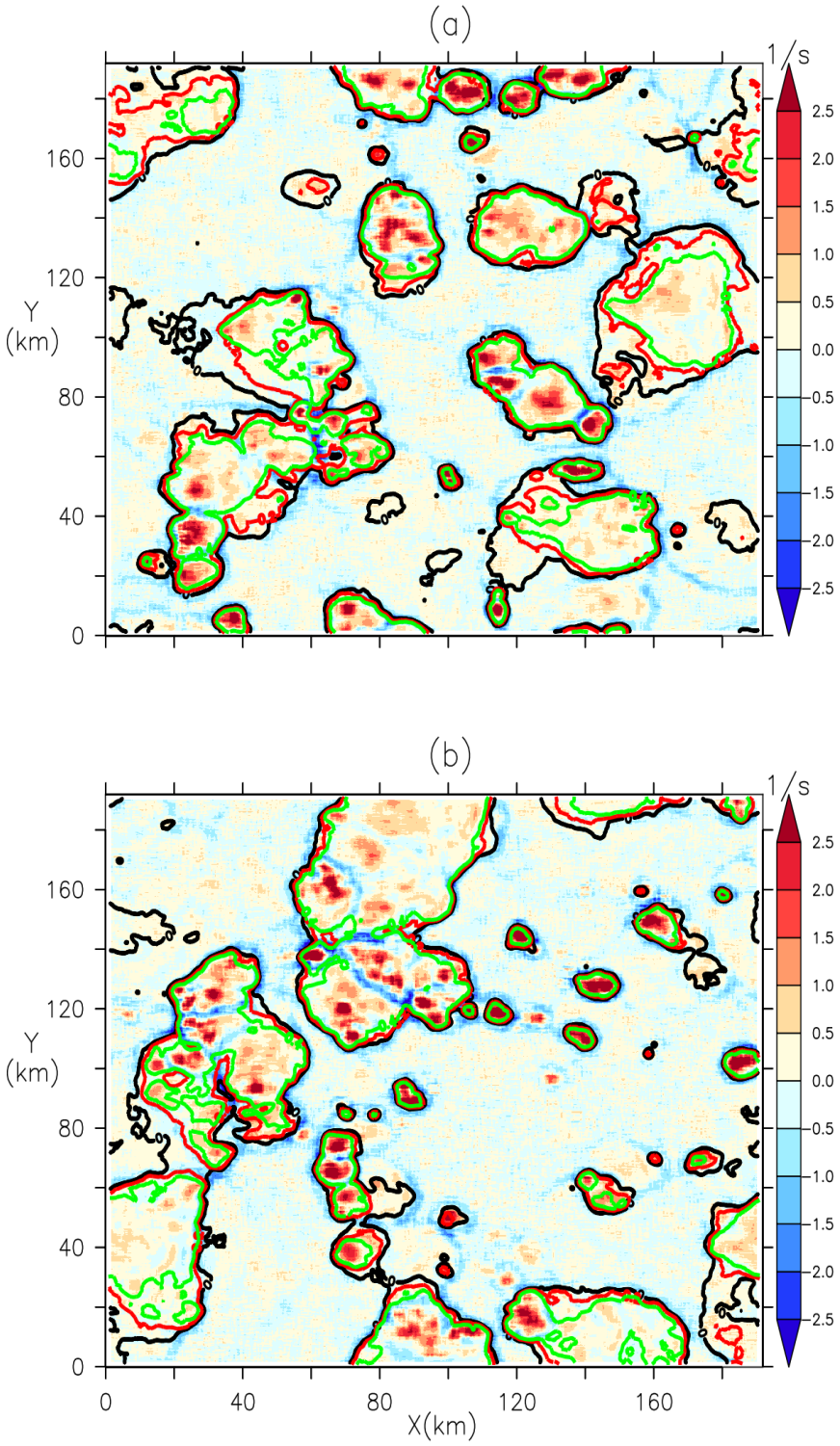

Figure 2: ~~Map~~ Sliding average (with a box of 3.25 km × 3.25 km) of the divergence of wind at 10 m $\overrightarrow{V_{10m}}$ (in ~~s^{-1}~~$10^{-3}s^{-1}$)~~multiplied by 1000 and smoothed horizontally over 3.25~~. **Changer l'unité 1/s sur les figures ou l'enlevers** With this unit, a value of 1 corresponds to a change of wind intensity of 1 ~~km × 3.25~~ms^{-1} for 1 km~~represented on two instants (~~). Panels a and b ~~)~~ correspond to two different states of the LES SAM carried out on the oceanic RCE case~~and superimposed with the contours~~. Contours of temperature anomalies at 10 m at -0.4 K (green), -0.2 K (red) and 0 K (black) are superimposed on the smoothed divergence field.

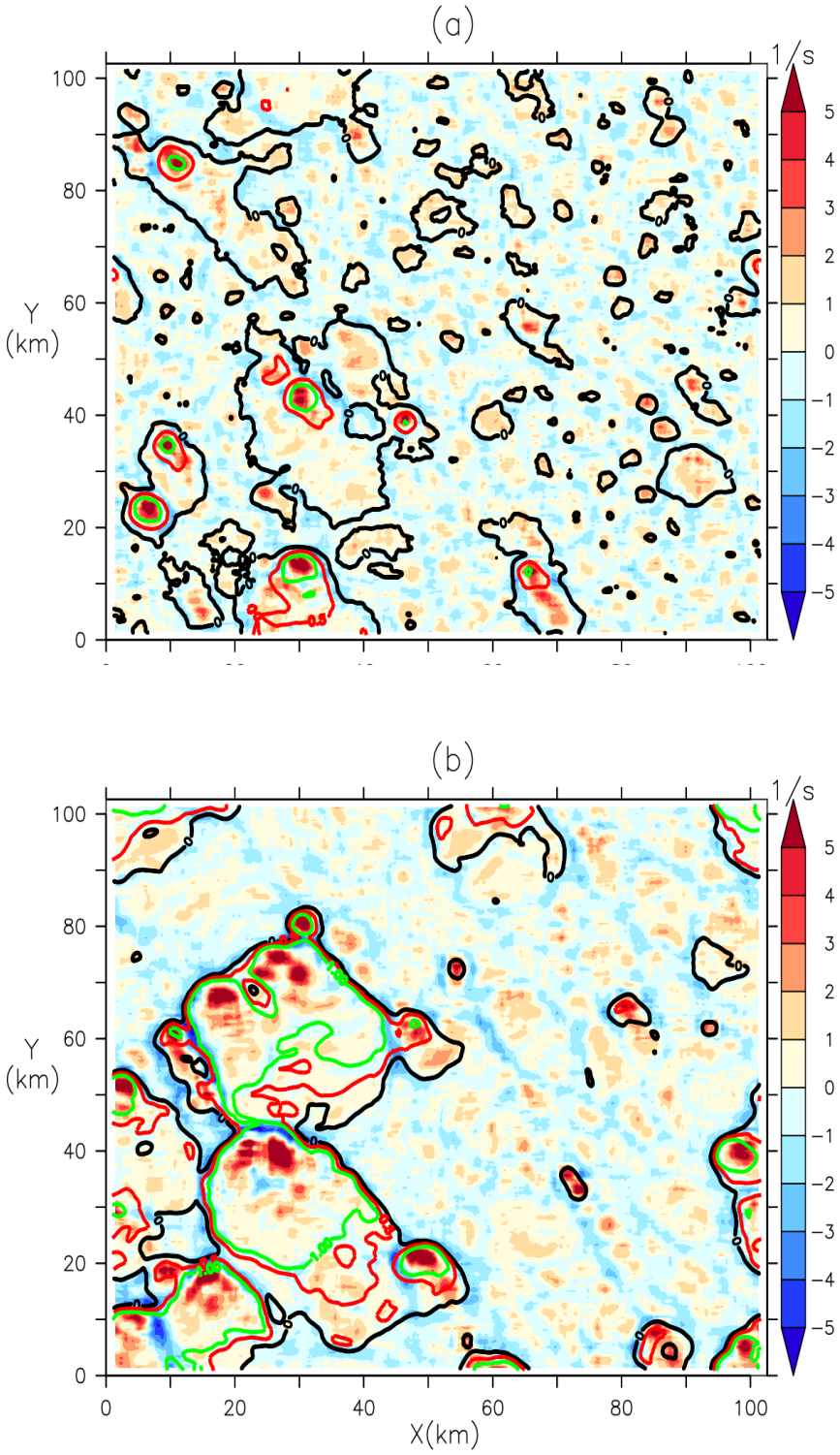

Figure 3: ~~Map of divergence of wind at 10 m (in s^{-1}) multiplied by 1000 and smoothed horizontally over 3.25 km × 3.25 km represented on the~~ Same as Fig. 2 for two successive instants, 17:10 (a) and 18:00 (b)~~instants~~, of the LES MESONH carried out on the AMMA case~~and superimposed with the~~. The contours ~~of~~ superimposed corresponds to T_{10m} anomalies of ~~temperature at 10 m at~~ -1 K (green), -0.5 K (red) and 0 K (black).

with some studies that indicate that convection initiation on gust fronts is more efficient when two or more cold pools collide (Meyer and Haerter, 2020; Torri and Kuang, 2019; Haerter and Schlemmer, 2018; Feng et al., 2015).

We superimpose on this map ~~T_{10m}~~ the $T_{10\mathrm{m}}$ anomaly contours with different values to determine an optimal threshold for this anomaly. In the RCE case, the ~~T_{10m}~~ $Tnearsrf$ anomaly at 0 K sometimes includes regions without cold pools centers, where divergence of surface wind is low (Fig. 2a and Fig. 2b) while anomaly contours -0.2 K and -0.4 K surround the centers of cold pools quite well. In the AMMA case, figure 3a clearly shows that the 0 K threshold is too high to identify cold pools. Figure 3b, on the other hand, shows that the -1 K threshold follows gust fronts of cold pools better than the -0.5 K threshold. On the basis of these analyses, we retain the ~~T_{10m}~~ $T_{10\mathrm{m}}$ anomaly thresholds at -0.2 K and -1 K to identify cold pools in the RCE and AMMA cases respectively.

~~After selecting values for the T_{10m} anomalyto separate the inside and outside of cold pools in the RCE and AMMA cases, we carry out sampling to calculate certain variables of cold pool model in the LES. We first determine~~

4.2 Computing cold pool anomalies vertical profiles

Once the threshold value is fixed for the $T_{10\mathrm{m}}$ anomaly, we separate the full 3-dimensional LES domain between cold pool region (w) and the rest of the domain (x) form which we can compute the horizontal averages on each subdomain, X_{W} inside cold pools and X_{X} outside, and then the cold pool anomaly $\delta X = X_{\mathrm{W}} - X_{\mathrm{X}}$. This sampling allows to compute the vertical profiles of cold pools anomaly for temperature (δT), humidity (δq) and vertical velocity (δw)~~differences between (w) and (x). To do this,~~ . Examples of temperature anomalies are shown in Fig. 4.

Note that we apply the same surface mask to the entire column to determine the vertical profiles. This simple vision of vertical cylinders, which matches the view underlying the parameterization, is obviously open to question. ~~But it does seem to apply, at least to the idealized cases studied here~~It was not seen as a limitation in the analysis presented below but this of course could be put into question.

~~**Calculation of the spreading speed, C_***~~

4.3 Computing the spreading speed, C_*, from sampled wind divergence

It is assumed in the parameterization that cold pools are identical disks of the ~~same radius (r)~~radius r. This assumption makes it easy to determine ~~C_*~~ C_* by of the divergence theorem.

$$\int\int \underline{div(\overrightarrow{V_{10}})}\mathrm{div}\left(\overrightarrow{V_{10\mathrm{m}}}\right) dS_{wk} = \underline{C_*} C_* L_g \tag{22}$$

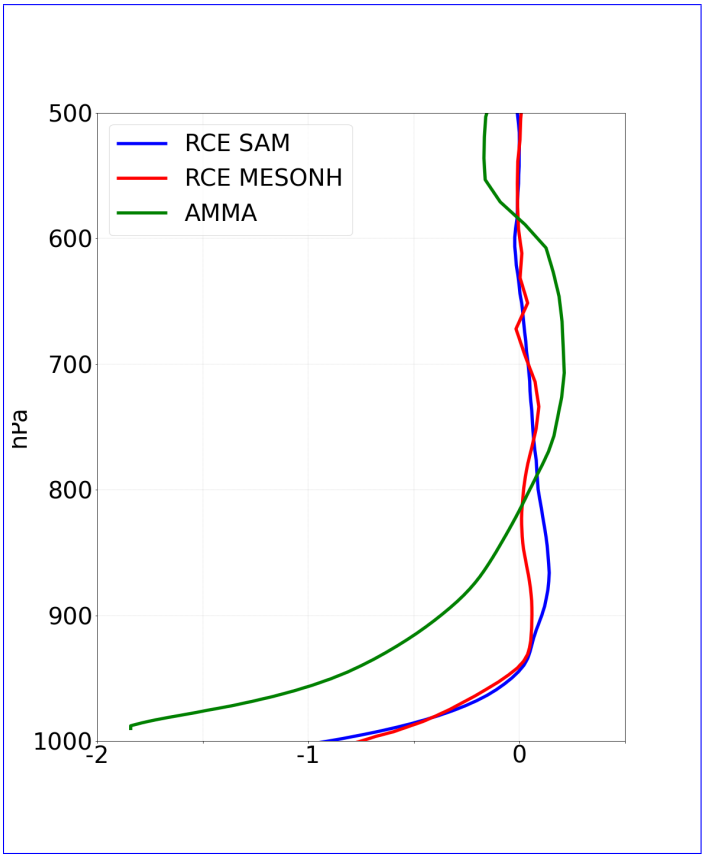

Figure 4: Vertical profiles of the temperature difference between the inside and the outside of cold pools calculated at an instant of the LES (SAM and MESONH) of the RCE case and an instant of the LES MESONH of the AMMA case.**Ajouter l'heure et peut être mettre les deux heures ? Peut être mettre aussi plusieurs courbes pour les RCE. Une dizaine chacune ?**

$$C_* C_* = \frac{\overline{div(\overrightarrow{V_{10}})} S_{wk}}{L_g} \frac{\overline{\text{div}\left(\overrightarrow{V_{10\text{m}}}\right)} S_{wk}}{L_g} \tag{23}$$

where S_{wk} is the surface of cold pools

$$S_{wk} = \pi r^2 \tag{24}$$

Equations 19, 20 and 24 allow us to express C_* as a function of the mean divergence of wind at 10 m, the surface fraction (σ_{wk}) and the density (D_{wk}) of cold pools by the relation :

$$C_* = \frac{1}{2} \overline{\text{div}\left(\overrightarrow{V_{10\text{m}}}\right)} \sqrt{\frac{\sigma_{wk}}{D_{wk}\pi}} \tag{25}$$

To apply this calculation of C_* in the LES, we take the horizontal average of the surface wind divergence inside cold pools. The surface fraction (σ_{wk}) of cold pools calculated in the LES is 0.12 for the AMMA case and 0.25 for the RCE case. To determine D_{wk}, we manually counted the centers of cold pools visible on the surface wind divergence maps (Fig. 2 and 3), as we did not use automated detection methods in this study that could generate their number automatically. We find an approximate density, D_{wk}, of 5 cold pools per 100 km × 100 km for both the RCE and AMMA cases.

~~Calculation of collapse energy~~

4.4 Computing the collapse energy, WAPE, from the virtual temperature anomaly

We finally calculate the collapse energy ($WAPE$) of cold pools in the LES using equation (1) proposed by Grandpeix et al. (2010). The task consists of determining $\overline{\theta_v}$, as well as the profiles of $\delta\theta_v$ and h_{wk} in the LES. To do this, we first computed δT in the LES, then derived $\overline{\theta_v}$ and the profile of $\delta\theta_v$. Regarding the determination of h_{wk}, as suggested by Grandpeix et al. (2010), we take this height at the altitude where the δT profile cancels out. This altitude is around 950 hPa (approximately 600 m) in the oceanic RCE case and around 800 hPa (approximately 2 km) in the AMMA case (Fig. 4). ~~Vertical profiles of the temperature difference between the inside and the outside of cold pools calculated at an instant of the LES (SAM and MESONH) of the RCE case and an instant of the LES MESONH of the AMMA case.~~

4.5 Computing ALP and ALE form gust front vertical velocities

Here we ~~compute the variables of~~ derive a direct estimation of the Available Lifting Energy (ALE_{wk}) and Power (ALP_{wk}) ~~associated with cold pools~~ in the LES ~~.~~ from a sampling of the vertical wind at cloud base.

To do this, we ~~proceed in several steps:~~

~~We~~ first determine an average cloud-base height at which we extract vertical velocities $w_b(x,y)$. This height corresponds to the altitude at which the average profile of condensed water reaches its first non-zero value. It is observed at around 950 hPa on the two oceanic LES (SAM and MesoNH) and at around 750 hPa on the LES for the AMMA case (MESONH) (Fig. 5).

We then separate the updrafts on gust fronts from those associated with thermal plumes. Since the updrafts on gust fronts are both stronger and more coherent horizontally than the thermals observed in the environment of cold pools, we ~~defined~~ define a mask based on a threshold an ~~horizontal smoothed~~ horizontally smoothed vertical veolcity at cloud based w_b (sliding average over 1.25 km×1.25 km ~~(RCE) et~~ for the RCE case and 2 km×2 km ~~(AMMA). The smoothed w_b values are denoted as $\tilde{w}_b(x,y)$~~ for AMMA), denoted as $\tilde{w}_b(x,y)$ in the rest of the text. After several analyses, we selected ~~$\tilde{w}_b(x,y)$ a~~ $\tilde{w}_b(x,y)$ thresholds of 0.6 m/s for the RCE case and 2 m/s for the AMMA case to identify gust fronts.

On ne peut pas dire moothed horizontally on a 2.5 km×2.5 km grid. Il n'y a pas de grille. La moyenne est glissante Figure 6 presents maps of T_{10m} anomaly, smoothed horizontally ~~on a~~ applying a sliding average on a box of 2.5 km×2.5 km~~grid~~, for the RCE and AMMA cases. On these maps, we have overlaid the contours of the T_{10m} anomalies used to identify cold pools (-0.2 K for RCE and -1 K for AMMA), as well as the updrafts on gust fronts (in red) and thermals (in green). Visually, the gust fronts computed with $\tilde{w}_b(x,y)$ thresholds of 0.6 m/s (RCE) and 2 m/s (AMMA) align well with the contours of cold pools identified using these T_{10m} anomaly thresholds. It also appears that most thermals are located in the environment of cold pools for both the RCE and AMMA cases (Fig. 6). This retrospectively validates a choice made in version 6A of ~~the model~~LMDZ, where the effect of thermals was only computed outside cold pools. Finally, to determine ALE_{wk}, we take the maximum kinetic energy in the domain, considering only $w_b(x,y)$ in the gust fronts mask ($w_{bgust}(x,y)$), as it is the maximum vertical velocity on the gust front that triggers convection. As for ALP_{wk}, which represents the average updrafts power provided by all cold pools in the domain, it is calculated from the horizontal average of the cube of w_{bgust}, weighted by the surface fraction (σ_{gust}) covered by gust fronts. The mask applied to gust fronts was used to calculate σ_{gust}, which is 0.017 for the RCE case and 0.067 for the AMMA case, for the times shown in figure. 6.

$$ALE_{wk} = max(\frac{1}{2}w_{bgust}^2) \tag{26}$$

$$ALP_{wk} = \sigma_{gust}\frac{1}{2}\rho\overline{w_{bgust}^3} \tag{27}$$

.

On aurait pu se poser la question de calculer ALE comme le max d'une vitesse verticale lissée horizontalement

Fin de relecture detaillee par Fredho

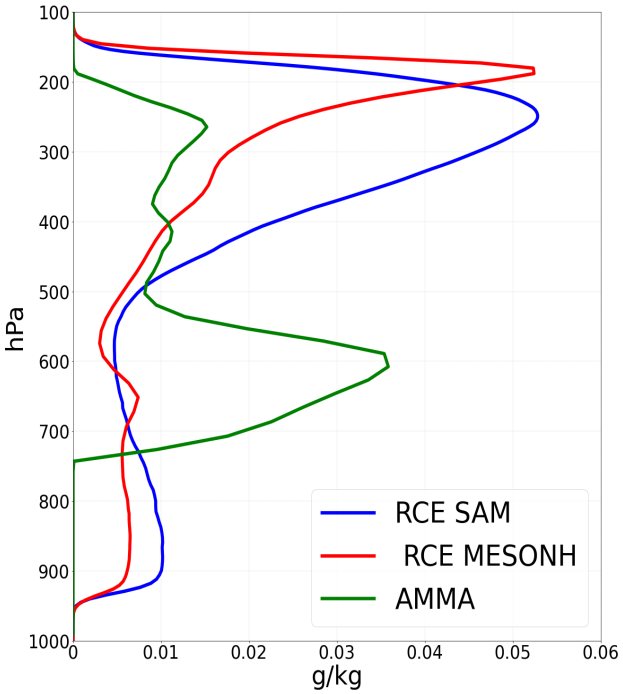

Figure 5: Vertical profile of condensed water averaged horizontally on the LES in oceanic RCE carried out with the SAM and MésoNH models and the continental LES of the AMMA case carried out with MésoNH.

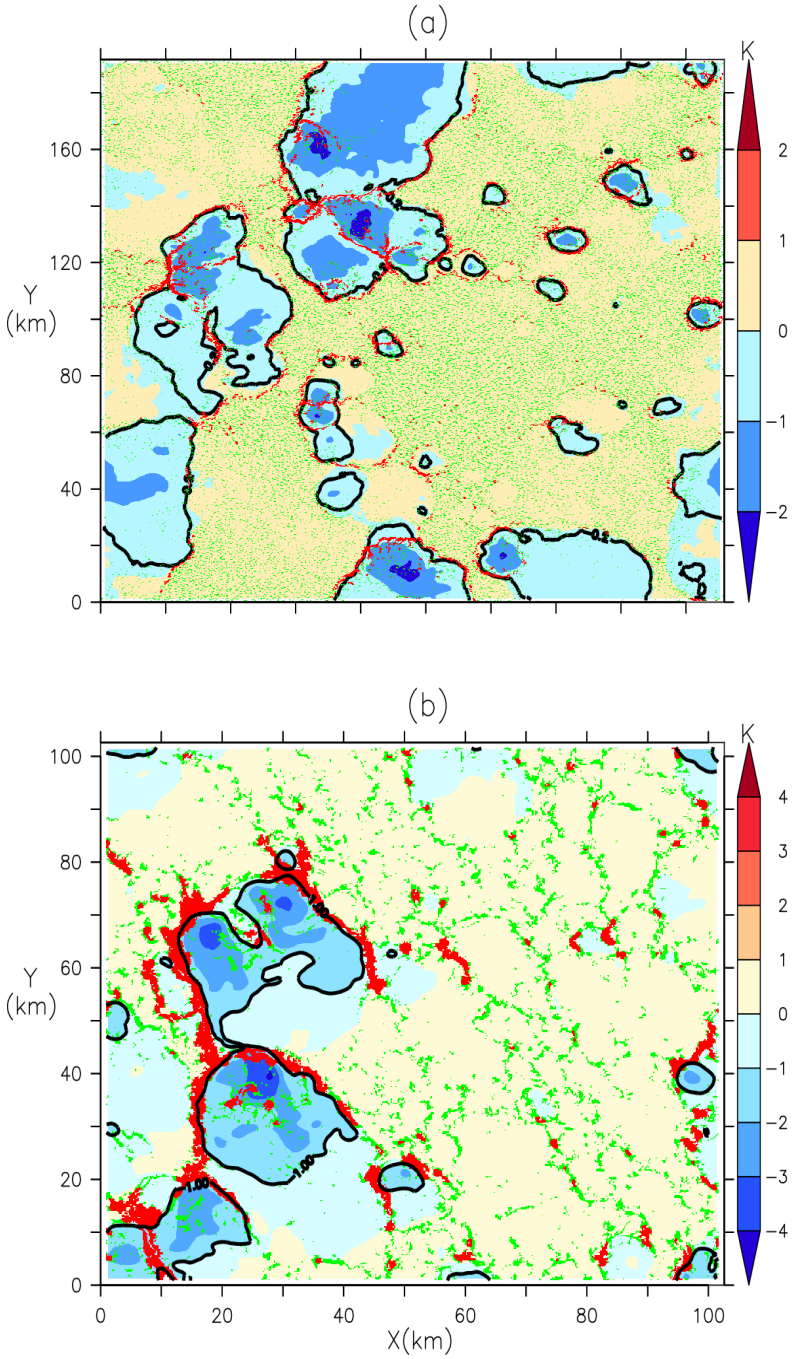

Figure 6: Maps of T_{10m} anomaly~~of temperature at 10 m~~, ~~smoothed horizontally over~~ with a sliding average with a horizontal box of 2.5 km×2.5 km, ~~represented on~~ at an instant of the LES SAM of the RCE case (a) and on the instant 6:00 PM of the LES of the AMMA case with black contours indicating thresholds of temperature at 10 m anomaly of -0.2 K (RCE) and -1 K (AMMA). The red color indicates the updrafts on the gust fronts given by the vertical velocities at cloud base (w_b) in the gust fronts mask~~, which~~. This mask is ~~determined by~~ defined from a threshold value applied to the sliding average of w_b~~smoothed horizontally over~~. For the RCE case, the average is done with a box of 1.25 km×1.25 km and ~~exceeding 0.6~~values of $\tilde{w}_b > 0.6$ m~~/~~ s^{-1} are retained (~~RCE) and over~~ respectively 2 km×2 km ~~with a value greater than 2~~and $\tilde{w}_b > 2$ m~~/~~ s^{-1} for AMMA). **il manque les valeurs de wb au dessus des quelles on trace les ponints de grille rouge et vert.** The green dots represent thermals, defined by w_b outside the gust front mask.

4.6 Validation of Phenomenological Laws

Physical parameterizations are defined by sets of mathematical equations intended to represent the subgrid process within a column of the model. The formulation of these equations is based on both a phenomenological understanding of the processes concerned and fundamental principles of physics. These parameterizations can be assessed in bulk, or piecewise, by isolating certain equations or relations between internal variables, or between internal variables and state variables of the GCM. LES offer the possibility of performing a priori validation and adjustment of these laws.

In the cold pool model, variables ALE_{wk}, ALP_{wk} and C_* are determined from the collapse energy~~(, $WAPE$)~~(see equations (2), (17) and (21))~~, based on assumptions derived from physical laws.~~

~~Here, we compare the values of ALE_{wk}, ALP_{wk} and C_* computed from~~ . We compare in Table 1 the values obtained this way, using the $WAPE$ deduced from $\delta\theta_v$, with those obtained directly from the vertical speed at cloud base ~~near the gust fronts (w_{bgust}~~(w_b) for ALE_{wk} and ALP_{wk}, and from the mean divergence of wind at 10 m in cold pools for C_*.

~~Table 1 shows such comparison for the three LES available.~~ The values of ALE_{wk} calculated ~~from w_{bgust} and $WAPE$ from the $\delta\theta_v$ profiles~~ by both methods are very close ~~. In the LES of the RCE case made with SAM, ALE_{wk} calculated from w_{bgust} is slightly higher than the $WAPE$ from the $\delta\theta_v$ profile (table 1). However, even in this case,~~ to each other. The largest error is an overestimation by about 30% of the ALE_{wk} ~~determined~~ computed from from w_{bgust} ~~remains comparable~~ compared to the $WAPE$ ~~derived from the $\delta\theta_v$ profile~~estimate. These results for the three LES are compatible with the hypothesis of equality between ALE_{wk} and $WAPE$, as estimated by the parameterization.

Table 1: Comparison of the variables of $WAPE$, ALE_{wk}, C_* and ALP_{wk} calculated in the samplings (E) and those calculated with the formulas of the parameterization (FP) for the coefficient $k = 0.33$ and $k = 0.66$ in the oceanic LES in RCE carried out with SAM and MESONH and in the continental LES of the AMMA case carried out with MESONH

	$WAPE$ (J/Kg)	ALE_{wk} (J/kg) (E)	C_* (m/s) (FP) k=0.33	C_* (m/s) (E)	C_* (m/s) (FP) k=0.66	ALP_{wk} (J/kg) (FP) k=0.33	ALP_{wk} (W/m^2) (E)	ALP_{wk} (W/m^2) (FP) k=0.66
RCE SAM	7.962	10.460	1.315	2.228	2.630	0.008	0.054	0.071
RCE MESO	7.912	6.965	1.313	2.264	2.625	0.008	0.020	0.071
AMMA MESO	34.250	33.480	2.727	4.939	5.454	0.104	0.982	0.831

C'est bizarre ce choix des lettres E et FP pour désinger les deux estimations... Pas très intuitif. Ca pourrait être WIND et WAPE ? Autre ? Ca serait pas mal d'utiliser le mot en question dans le texte. We compare the WIND

estimate with the WAPE estimate. S sampled and P parameterized ? Avec l'idée que les estimations à partir de la divergence du vent ou de wb sont ce qu'on vise et les estimations à partir de WAPE la version paramétrée. C'est le choix qui était fait avec FP. J'aime bien ce choix : S et P. Même si le P lui même repose sur un échantillonage de T. Mais justement. C'est sans doute l'occasion de bien dire ça en début de section.

Table 1 shows that, C_* values calculated from the $WAPE$ are systematically lower than those coming from the mean divergence of wind at 10 m in cold pools. This difference could be due to an underestimation of the coefficient k, imposed here at 0.33. ~~By setting k to 0.66~~With $k = 0.6$, the calculation of C_* based on the $WAPE$ becomes comparable to those obtained from the mean divergence of wind at 10 m in cold pools ~~, notably for the RCE and AMMA cases~~ (table 1). As discussed above, the value of 0.33 was retained following an oral communication by Lafore (2000). But other studies propose different values: Lafore and Moncrieff (1989) estimate k at 0.68 based on CRM simulations of 2D squall grain, Bryan (2005) estimate it at 0.5 from observations of cold pools during the BAMEX experiment in the American Great Plains. ~~These~~ Our results are thus compatible with the hypothesis of the model which postulates that the kinetic energy of cold pools results from the transformation of $WAPE$ into kinetic energy with a coefficient k compatible with the published estimates.

Table 1 also shows that, for the three LES cases, the values of ALP_{wk} calculated with $C*$ from $WAPE$ are at least three times lower than those obtained from w_{bgust}. Two coefficients are involved in the calculation of ALP_{wk} with the parameterization formula: the coefficient k and the lifting efficiency ϵ, imposed respectively at 0.33 and 0.25. Using k=0.66 however in the calculation of C_*, and keeping ϵ at is nominal value of 0.25 allows to reconcile the various estimates. This is compatible with the hypothesis of the parameterization according to which 25% of the horizontal power provided by the cold pools during its propagation would be used to reinforce the intensity of the convection while a large part dissipates.

5 ~~Comparison between LES and standard~~ Evaluation in the single column configuration of LMDZ

5.1 ~~Vertical profiles of δT, δq and δw~~

In this section, we evaluate the ~~profiles of δT, δq and δw computed by LMDZversus LES ones. In SCM mode, the~~ cold pool parameterization in the SCM configuration of LMDZ. The comparison is more demanding ~~than those previously discussed~~here, since all parameterizations interact with each other ~~to arrive at the simulated values several~~ and because the state of the atmosphere at the time of evaluation depends on the interaction of all those parameterizations during the preceeding hours (AMMA) or days (RCE)~~after initialization~~. The SCM simulations are performed with exactly the same initial and boundary conditions as the corresponding LES for both cases.

For the RCE case, we represent ~~the profiles~~ diagnostics once a quasi-steady state has been reached ~~. Regarding~~ by averaging results between day 40 and 44.

For the AMMA case, ~~intermediate analyses show that~~ the LMDZ CTRL simulations are performed over the day of July 10, 2006, from 6:00 AM to midnight. In the AMMA LES, cold pools appear in the afternoon around 5:00 PM with relatively low temperatures~~and develop during the day~~. Due to the variations in cold pools characteristics ~~at different times on the continent~~in the following hours, we average the results over the 7 available times between 5:00 PM and 6:00 PM to simplify our analyses. ~~To compare with the model, we perform a single-column LMDZ control simulation (LMDZ CTRL) for the RCE and AMMA cases. These LMDZ simulations are performed with exactly the same initial and boundary conditions as the corresponding LES. For the RCE case , we perform a 44-day LMDZ CTRL simulation to reach a quasi-equilibrium. For the AMMA case, the LMDZ CTRL simulations are performed over the day of July 10, 2006, from 6:00 AM to midnight.~~

~~For the AMMA~~ For this case case, the cloud size threshold (S_{trig}, a model free parameter with large uncertainty) controlling the triggering of deep convection in LMDZ is adjusted so that convection triggers at the same time as in the LES in order to allow a precise comparison. Indeed, convection triggers before 2:00 PM in the AMMA case with the standard LMDZ configuration, while in the LES, it appears around 5:00 PM. To obtain a triggering simultaneous with that of the LES, we performed tests by modifying the value of S_{trig}. These tests made it possible to obtain the triggering of convection in the LMDZ simulation of the AMMA case at 4:50 PM by setting S_{trig} at 24 km^2.

In order to facilitate comparisons between LMDZ and LES, we also impose in the LMDZ simulations the density of cold pools estimated in the LES. We thus set a density of 5 cold pools per 100 km×100 km, both for the RCE and AMMA cases. To represent the profiles of δT, δq and δw in LMDZ CTRL for the RCE case, we perform a time average between the 41st and 43rd day of simulation, in order to compare with the LES at the same times. For the AMMA case, we perform an average between 5:00 PM and 6:00 PM, as in the LES.

5.1 Vertical profiles of δT, δq and δw

The analysis of the δT profiles in the LES confirms that cold pools are colder at the surface with temperatures increasing towards the top for the three LES. The cold pools are about three times deeper in AMMA (Fig. 7a) than for the RCE case (Fig. 7d). In the LES, we observe that the temperatures of cold pools for the AMMA case (around –2 K) are relatively close to those of the RCE case (around –1.2 K). However, observations indicate that cold pools are significantly more intense over continents than over oceans. The results obtained with the LES for the AMMA case could be explained by the fact that the analysis is carried out from the first moments following the formation of the cold pools. However, for this same case, observations reveal a temperature drop of around –5 K during the passage of cold pools (Lothon et al., 2011). It should also be noted that the AMMA case corresponds to a particularly weak and atypical episode of continental convection. The

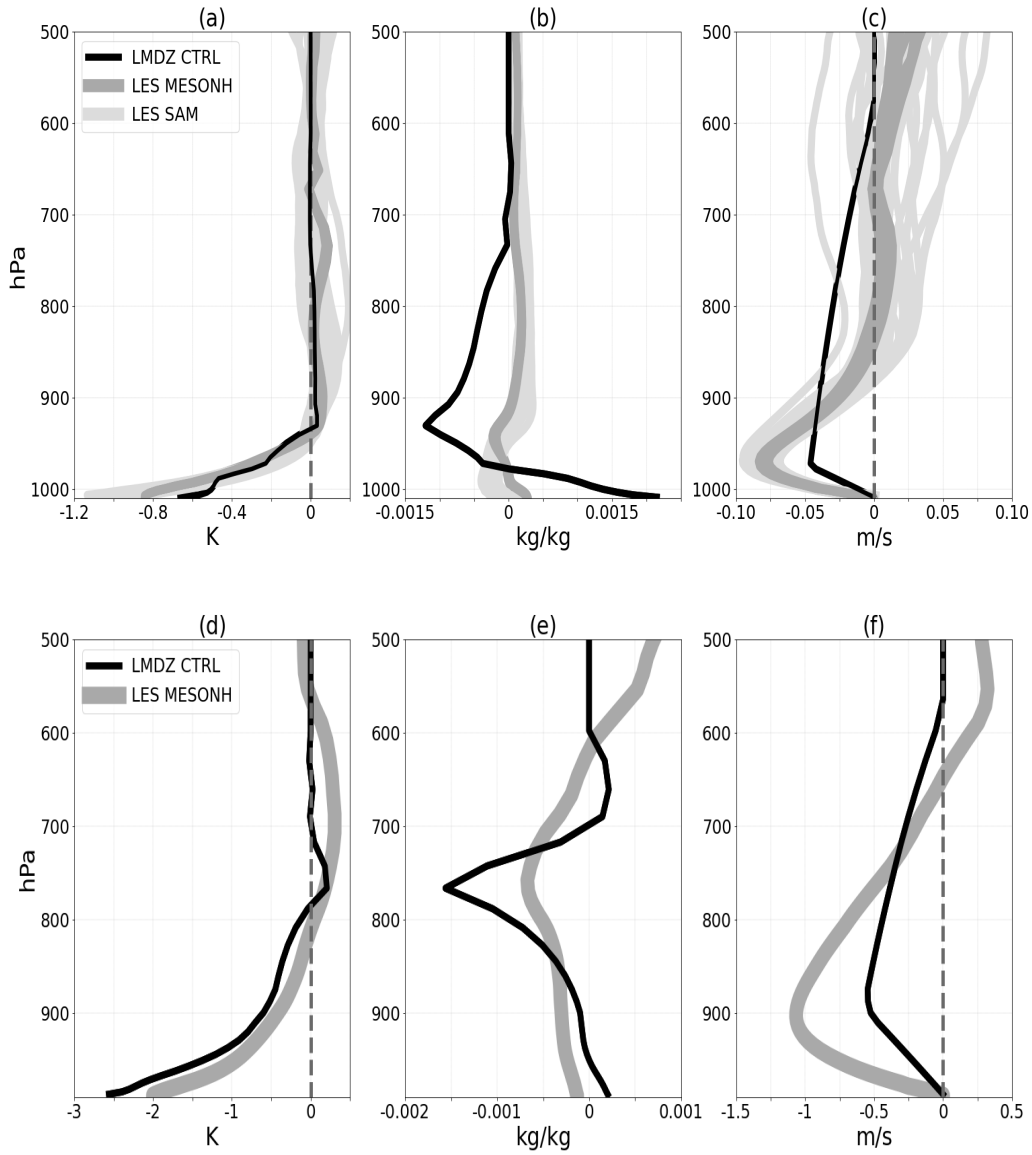

Figure 7: Vertical profiles of δT, δq and δw calculated in the LES and simulated by LMDZ control (LMDZ CTRL) on the RCE case (a, b, c) and on the AMMA case (d, e, f).

δq profiles indicate that at the surface, cold pools are wetter than ~~their surroundings~~ the surrounding air in the RCE case (Fig. 7b), while in the AMMA case, they are slightly drier (Fig. 7e). In both cases, the humidity within the cold pools decreases with altitude until they reach their summit, where they are dried by the subsidence of dry air masses into cold pools (Fig. 7c and 7f). On the RCE case, this subsidence vanishes below 800 hPa (Fig. 7c), while for the AMMA case, it vanishes at a higher level, around 600 hPa (Fig. 7f).

The δT profiles simulated with LMDZ CTRL are qualitatively consistent with LES, with a cold pool top (where δT cancelled) at about the right altitude. Cold pools simulated with LMDZ are however warmer than in the LES for the RCE case (Fig. 7a), and slightly colder at the surface than the LES for the AMMA case (Fig. 7d). Consistently with LES, cold pools are also wetter at the surface and drier close to their top top (Fig. 7b and Fig. 7e). However the variations of δq are much larger in LMDZ than in the corresponding LES. In particular, the cold pools are much too dry at their top in LMDZ. In both cases, cold pools are associated with subsidence. The height at which the subsidence of air masses in cold pools begins, fixed at 600 hPa in LMDZ CTRL, is too high compared to LES for the RCE case 7e).

The comparisons also reveal that the model simulates wetter cold pools at the surface than those in the LES in both cases, with a more pronounced difference for the RCE case.

5.2 WAPE, ALE and ALP

Table 2: Comparison of the $WAPE$, ALE_{wk}, C_* and ALP_{wk} computed from sampling of the LES and by LMDZ control (LMDZ CTRL) for the RCE AMMA cases. The results are averaged over the days following the achievement of equilibrium (days 41, 42 and 43) for RCE and over the available instants between 5:00 PM and 6:00 PM for AMMA.

	$WAPE$ (J/Kg)	ALE_{wk} (J/kg)	C_* (m/s)	ALP_{wk} (W/m^2)
RCE				
LES SAM	7.962	10.460	2.228	0.054
LES MESONH	7.912	6.965	2.264	0.020
LMDZ CTRL	2.957	2.957	0.802	0.001
AMMA				
LES MESONH	34.250	33.480	4.939	0.982
LMDZ CTRL	30.430	30.430	2.574	0.042

For the RCE case, the $WAPE$ is significanlty smaller in LMDZ CTRL than in the LES, with a difference of at least a factor of 2 (Table 2). These low values of $WAPE$ in LMDZ CTRL also translate into low ALE_{wk} values compared to LES (table 2).

Indeed, ALE_{wk} in the RCE case it at least twice as low in LMDZ CTRL as in the LES. On the other hand, for the AMMA case, the $WAPE$ simulated by the model are globally in agreement with the values calculated in the LES (table 2), which allows the model to obtain ALE_{wk} comparable to those of the LES for this case (table 2).

The value of C_* simulated by LMDZ CTRL is also at least three times smaller than in the LES for all the cases (table 2). This leads to a ALP_{wk} value ten times smaller than in the LES.

6 Improvements of cold pool model

Here, we start by correcting the observed discrepancies between the LES and the model concerning the value of the coefficient k and the altitude h_m, and by assessing the impact of these changes on the temperature and humidity difference between the cold pools and their environment, before exploring other avenues for improvement.

6.1 Coefficient k

We present here the impact of increasing the coefficient k from 0.33 to 0.66 (LMDZ V1 simulation) on the profiles of δT, δq, δw as well as on the variables C_*, $WAPE$, ALP_{wk} and ALE_{wk}. In the RCE case, this modification significantly improves the profile of δw below h_{wk} (Fig. 8c). This improvement is directly linked to an increase in C_* (Table 4), since the profile of δw below h_{wk} depends on the spreading of cold pools. The increase in C_* could be associated with a stronger air mass subsidence in the cold pool, which would contribute to a slight drying near the surface (Fig. 8b). Similar effects, although less marked, are observed for the profiles of δw and δq in the AMMA case (Fig. 8e,f). Nevertheless, the increase of k also leads to an improvement of C_* for this case (Table 4). The improvement of C_* in both cases, RCE and AMMA, is also at the origin of a better representation of ALP_{wk} (increase by a factor of 6 for RCE and by a factor of 10 for AMMA), even if this variable remains underestimated (Table 4). ~~However, despite this modification of k, cold pools remain~~ Cold pools remain however too dry at their top and wetter at the surface, in both cases (Fig. 8b,e). In the RCE case, they also remain less cold in LMDZ V1 than in the LES (Fig. 8a). For the AMMA case, a slight flattening of the δT profile is observed, which nevertheless remains globally consistent with the LES (Fig. 8d). The impact on the δT profiles in the AMMA and RCE cases is at the origin of the decrease in the values of $WAPE$ and ALE_{wk} for these two cases (Table 4).

Pour les profils moyens, est-ce qu'il ne faudrait pas tracer à la fois les profils (comme ici) et les biais par rapport à la LES ? Fig. 9 shows that the modification introduced in version V1 has a low impact on the θ and q_v mean profiles (Fig. 9), the black and blue curves being almost superimposed. Both CTRL and V1 simulations reproduce the θ profiles reasonably well. Both cases are too cold by 2-3 K in the boundary layer **to be checked**. Above 600 hPa, a slight warm bias is observed in the RCE case, and a cold bias for AMMA. The agreement is not as good for the humidity profiles. In the RCE case, a dry bias is clearly visible in the boundary layer, as well as between 800 and 400 hPa. For the AMMA case, a wet bias is observed in the boundary layer and above 600 hPa, while a dry bias is present between 700 and 600 hPa.

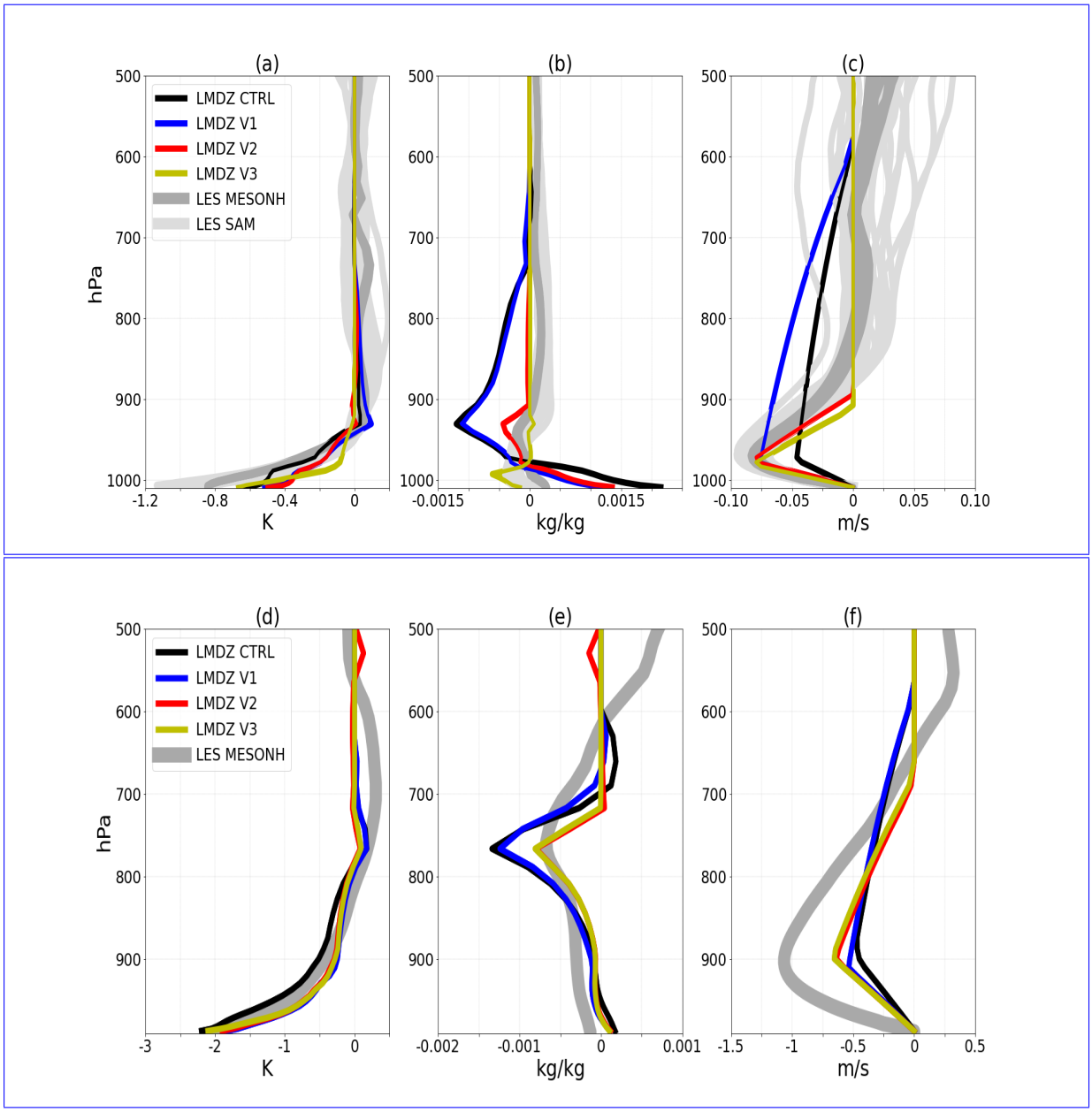

Figure 8: Vertical profiles of δT, δq and δw calculated in the LES and simulated in the control LMDZ (CTRL), LMDZ with the adjustment of the coefficient k to 0.66 (V1), LMDZ with the drop in altitude (h_m) at which the subsidence of the air masses in cold pools is zero (V2) and LMDZ with the activation of thermals in the entire domain (V3) on the RCE case (a, b, c) and on the AMMA case (d, e, f).

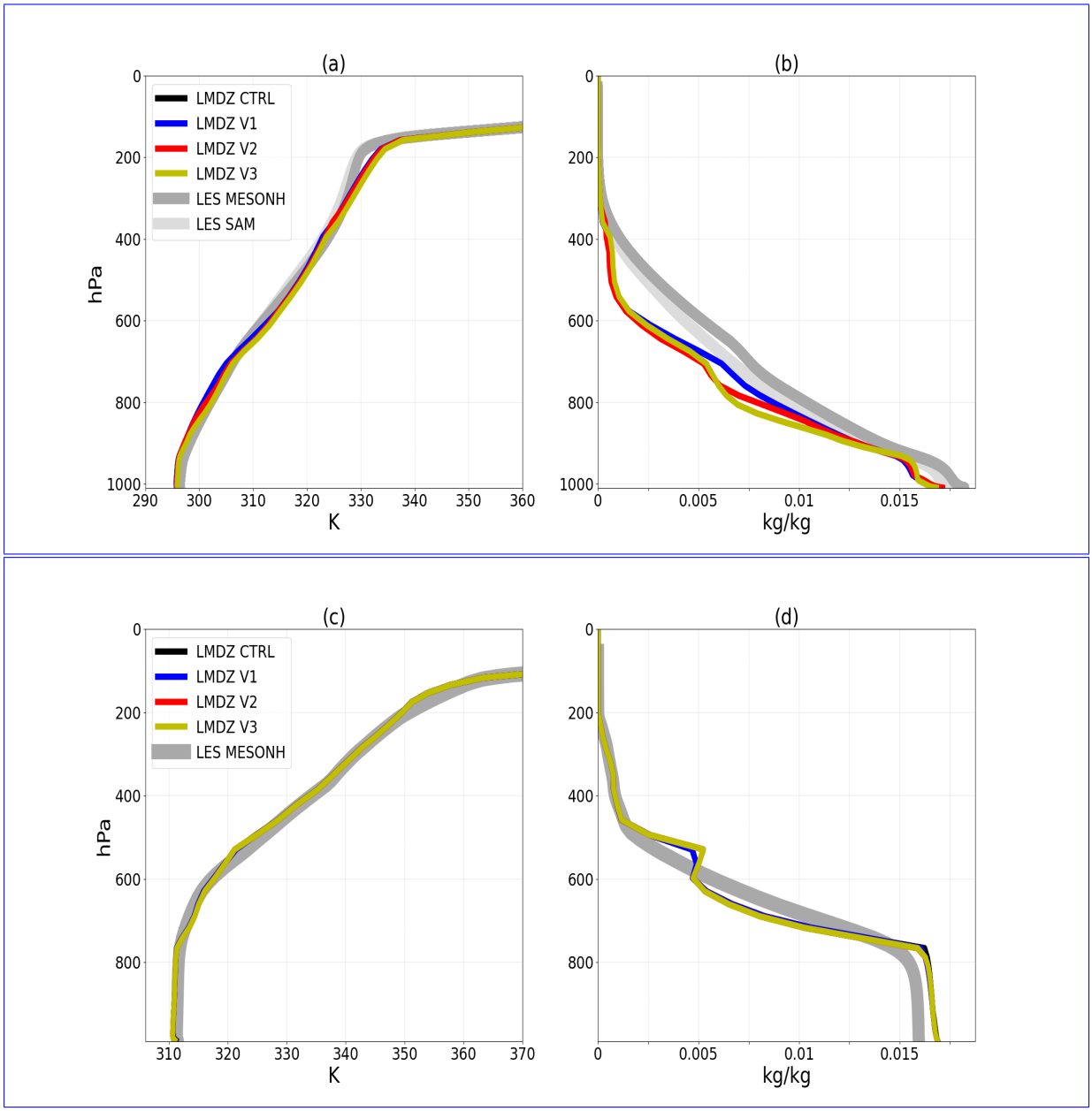

Figure 9: Vertical profiles of potential temperature (θ) and specific humidity (q_v) calculated in the LES and simulated in control LMDZ (LMDZ CTRL), LMDZ with the adjustment of the coefficient k to 0.66 (V1), LMDZ with the drop in altitude (h_m) at which the subsidence of the air masses in cold pools is zero (V2) and LMDZ with the activation of thermals in the entire domain (V3) on the RCE case (a, b) and on the AMMA case (c, d). The LES profiles correspond simply to horizontal averages over the full domain.

6.2 Altitude h_m

~~Vertical profiles of δT, δq and δw calculated in the LES and simulated in the control LMDZ (CTRL), LMDZ with the adjustment of the coefficient k to 0.66 (V1), LMDZ with the drop in altitude (h_m) at which the subsidence of the air masses in cold pools is zero (V2) and LMDZ with the activation of thermals in the entire domain (V3) on the RCE case (a, b, c) and on the AMMA case (d, e, f).~~ **C'est très bizarre d'utiliser hm pour une pression ... Pupper et Ptop c'est bien non ??? D'ailleurs ca serait bien de donner une fois les altitudes correspondantes dans le texte.**

In the previous sections, we found that the altitude at which the subsidence of dry air above cold pools initiate is observed in LES below 800 hPa for the RCE case and below 600 hPa for the AMMA case, while in LMDZ, this altitude h_m was arbitrarily set to 600 hPa in the original version of the parameterization. In version V2, in addition to the change of the value of k from 0.33 to 0.66, we compute h_m as αh_{wk} with $\alpha = 3$ (α is considered as a new free parameter in the following section).

Ce n'est pas ce qui est décrit dans l'annexe ??? A slight adjustment of h_{wk} was also made thanks to the new numerical scheme proposed for its calculation, although the details are not discussed here. This adjustment, however, has no impact on the vertical profiles of δT, δq.

Comparisons between LMDZ V2 simulations and LES show a better representation of the δq profiles at the top of cold pools in both the RCE and AMMA cases (Fig. 8b and Fig. 8e). These results show that the dry bias at the top of the cold pool in the original version was due to advection of dry air from too high an altitude. The fact that the model is able to reproduce consistently the vertical profile of vertical wind and the humidity at the top of cold pools when adjusting h_m validates the physics implemented in this cold pools scheme. ~~This reveals that a limitation of this scheme lays in the choice of the value of a parameter (the height above 600 hPa) rather than in the formulation themselves~~**Finalement je trouve la phrase suivante : "This reveals that a limitation of this scheme lays in the choice of the value of a parameter (the height above 600 hPa) rather than in the formulation themselves." Quelque part c'est un changement de paramétrisation. Petit mais quand même. Le paramètre dépend d'autre chose. Et je trouve que ca n'ajoute rien**. This modification also reduces slightly the humidity at the surface of cold pools in the RCE case. We however observe that cold pools always remain more humid at the surface in LMDZ V2 than in the LES. ~~Concerning the δT profiles, a and d indicate~~

Note finally that this modification has a very limited impact on the δT profiles~~in the AMMA and RCE cases.~~ **. C'est pas évident de savoir pourquoi et potentiellement intéressant.**

Table 4 shows that the decrease in h_m weakly affects the variables $WAPE$, C_*, ALE_{wk} and ALP_{wk} for these two cases.

Versions V2 does not modify much the mean vertical profiles except for a drying of the mid-troposphere in the RCE case (Fig. 9b), in a region where the CTRL simulation was already to dry. Although the time evolution of the mean profiles is the first target of

physics parameterizations, we think however that the improvement of the internal variables is so strong for this modification that it should be adopted in the future in LMDZ.

6.3 Activation of thermals throughout the domain

~~To understand the origin of the wet bias in surface of cold pools in LMDZ, we test to activate thermals throughout the domain.~~ In the standard LMDZ configuration, thermals only interact with temperature and humidity profiles outside cold pools. **Il me semble qu'il faut avoir expliqué plus haut qu'on a Q1th dans le delta Q1cv.** This choice was originally made to account for the fact that the atmosphere is more stable inside cold pools, ~~which would inhibit convection in these regions. In the version~~ and indeed the analysis above shows that the thermal plumes that reach cloud base are essentially outside cold pools. This this choice, the boundary layer convection is reinforced, and an additional term is added to the time evolution of the cold pool temperature and humidity anomalies. Version V3 ~~, we interact thermals with the grid-averaged temperature and humidity profiles, starting from the V2 configuration~~is identical to version V2, except that we consider that thermal plumes interact with the mean grid cell profiles, with no effect of thermal plumes on the temperature and humidity cold pool anomalies. For the RCE case, the LMDZ V3 simulations show a clear decrease in the surface humidity of cold pools, corresponding better to the results obtained with the LES (Fig. 8b). This result is expected because the vertical transport by thermals systematically dries the surface (Diallo et al., 2017). We also observe a slight modification of the profile at the top of cold pools. In the AMMA case, this modification has almost no effect (Fig. 8e), probably because the simulation duration is too short. In the 30-day 3D test **On a fait des tests, c'est ça ? On les montre ou pas ?**, cold pools also dry out significantly on the continent with this modification. ~~These results suggest a key role for thermals~~ This confirms the key role of boundary layer convection in regulating surface humidity on both continent (Diallo et al., 2017) and ocean (Hourdin et al., 2020), via the mixing of moist air with dry air above. ~~To represent this effect in the model, one could incorporate shallow ,~~

One way to improve the representation of humidity anomaly profile without activating the thermal plumes everywhere would be to add a simple parameterization of shallow and cloud-free ~~thermals that primarily serve to mix the air~~boundary layer convection (a simplified version of the thermal plume model) within the cold pool.

~~Intermediate tests have allow~~ Tests not shown allowed to assess the impact of surface evaporation flux on cold pool moisture by activating splitting, which differentiates this flux between (w) and (x). In the standard configuration, this flux is treated uniformly for both regions. The tests showed a limited effect of this flux on cold pools moisture for RCE. This test was not carried out for AMMA, as LMDZ does not yet allow it on the continent. However, it would be relevant to explore it.

~~LMDZ~~ In version V3~~simulations show a cooling of cold pools by thermals for the RCE case, although cold pools remain~~ , cold pools are colder than in version V2, but still less cold compared to the LES (Fig. 8a). This ~~cooling is at the cause of an increase in the variables~~ induced in turn a slight increase of $WAPE$, C_*, ALE_{wk} and ALP_{wk} ~~in this case~~

(Table 4). For the AMMA case, the impact of this modification on the δT profile as well as on the associated variables remains very limited (Fig. 8e,Table 4). But 3D tests also indicate a cooling of cold pools on the continent when thermals are activated in the whole domain. **Attention : on parle à nouveau de ces résultats 3D**

Table 3: Description of simulations performed with LMDZ in the standard configuration and with various modifications

Simulations	**Protocols**
LMDZ CTRL	simulation of LMDZ with the standard configuration by imposing D_{wk} to 510^{-10}
LMDZ V1	LMDZ CTRL + change of k to 0.66
LMDZ V2	LMDZ V1 + drop of h_m
LMDZ V3	LMDZ V2 + activation of thermals throughout the domain

Table 4: Comparison of the variables $WAPE$, ALE_{wk}, C_* and ALP_{wk} calculated from the samplings in the LES, with those simulated in LMDZ control (LMDZ CTRL), LMDZ with the adjustment of the coefficient k to 0.66 (V1), LMDZ with the drop in altitude (h_m) at which the subsidence of the air masses in cold pools is zero (V2) and LMDZ with the activation of thermals in the entire domain (V3) on the RCE case and on the AMMA case.

	$WAPE$ (J/Kg)	ALE_{wk} (J/kg)	C_* (m/s)	ALP_{wk} (W/m^2)
RCE				
LES SAM	7.962	10.460	2.228	0.054
LES MESONH	7.912	6.965	2.264	0.020
LMDZ CTRL	2.957	2.957	0.802	0.001
LMDZ V1	2.528	2.528	1.484	0.006
LMDZ V2	2.465	2.465	1.465	0.006
LMDZ V3	3.408	3.408	1.723	0.009
AMMA				
LES MESONH	34.250	33.480	4.939	0.982
LMDZ CTRL	30.430	30.430	2.574	0.042
LMDZ V1	22.020	22.020	4.380	0.479
LMDZ V2	20.580	20.580	4.234	0.399
LMDZ V3	20.640	20.640	4.240	0.404

6.4 ~~Effect~~ Tuning of ~~changes on large-scale variables~~free parameters

~~Although the modifications presented above have improved the representation of cold pools in the model, it is also essential to examine their impact on large-scale variables. In this section, we analyze the effect of these adjustments on variables such as potential temperature (θ) and specific humidity (qv) profiles. For this, the same profiles are recalculated~~

~~in the LES for the RCE and AMMA cases and then compared with those obtained in each modified version of the LMDZ model. The profiles of θ and qv in the LES are calculated by a horizontal average of these variables over the domain. Vertical profiles of potential temperature (θ) and specific humidity (qv) calculated in the LES and simulated in control LMDZ (LMDZ CTRL), LMDZ with the adjustment of the coefficient k to 0.66 (V1), LMDZ with the drop in altitude (h_m) at which the subsidence of the air masses in cold pools is zero (V2) and LMDZ with the activation of thermals in the entire domain (V3) on the RCE case (a, b, c) and on the AMMA case (d, e, f).~~ The above tests show possible avenues for improving the cold pool parameterization. However all the test shown underestimate the cold anomaly inside cold pools and in turn $WAPE$, ALE_{wk} and ALP_{wk}.

~~shows that, in the RCE case, the modifications introduced in versions V1, V2 and V3 have a low impact on the θ profiles (a), while in the AMMA case, their influence remains negligible (c). Overall, all simulations (LMDZ CTRL, V1, V2 and V3) manage to reproduce the θ profiles well, both for RCE and for AMMA, although a slight warm bias is observed around 200 hPa in the RCE case. In contrast, versions V2 and V3 lead to a drying of the mid-troposphere in the RCE case (b), while for AMMA, the three modified versions have little effect on the humidity profiles (d). However , it appears that the LMDZ model insufficiently reproduces the humidity profiles in all simulations, both for RCE and AMMA. In the RCE case, a dry bias is clearly visible in the boundary layer, as well as between 800 and 400 hPa, for versions CTRL, V1, V2 and V3. For the AMMA case, a wet bias is observed in the boundary layer and above 600 hPa, while a dry bias is present between 700 and 600 hPa. To correct these biases observed in the model, as well as the simulated hot cold pools in RCE case, a tuning of parameter is performed~~ **Reprendre les tests de tuning et leur analyse, meme si je trouve la modification du RCE suffisamment importante et positive pour partir avec ça à la soumission**

7 ~~Tuning of free parameters~~

Mettre les fourchettes de valeurs obtenues pour les 10 meilleures simulations dans le tableau de WAPE, C*, ALE ...

Since the cold pool model is coupled to the deep convection model, the δT profile could be influenced by the latter. Thus, more than twenty free parameters were selected, including those related to the cold pool model as well as to the convection schemes. The metrics retained are the δT, q_v and θ profiles, evaluated through vertical averages at different levels and time averages (between 5 P.M. and 6 P.M. for the AMMA case, and between days 41 and 43 for RCE). In these tuning tests, only modifications affecting the k and h_m coefficients were integrated. Adjustments related to thermals are not taken into account here, because, in LMDZ v3, our objective is only to highlight their role in the drying of surface cold pools. We suggest that further parameterization work address this point.

The results obtained after tuning show a clear improvement in the representation of the δT profile in the RCE case (Fig. 10a). The δq and δw profiles also remain well represented

for this case (Fig. 10b,c). Fig. 11b and Fig. 11d also illustrate a significant improvement in the humidity profiles for the RCE and AMMA cases. However, a humid bias persists in the boundary layer for the AMMA case (Fig. 11d), accompanied by a slight cooling in this same layer (Fig. 11c). A slight increase in the temperature of the cold pool and a drying at their top are also observed in AMMA after tuning (Fig. 10d,c). However, the fact to obtain a better representation of the humidity profiles in both cases, while improving the representation of the cold pools, particularly in the RCE case, constitutes a satisfactory result. The values of the optimized parameters resulting from this tuning can now be used in the 3D version of the LMDZ model.

7 Conclusions

Although the cold pool model proposed by Grandpeix and Lafore (2010) has improved the representation of convection in the LMDZ climate model Rio et al. (2009), its internal variables and physical properties have never been evaluated. This work proposes, for the first time, a detailed evaluation of the cold pool model, based on ~~explicit simulations called~~ LES. We evaluate both the physics of the model, its internal variables and those involved in the coupling with deep convection, based on two oceanic LES in the RCE regime and a continental LES of the AMMA case. ~~For this, we first performed sampling in the LES, separating the interior and exterior of cold pools on the RCE and AMMA cases by surface temperature anomalies lower than~~ We introduced a sampling of the cold pools in the LES based on a threshold of the 10 m temperature anomaly of -0.2 K for the RCE case and -1 K ~~respectively, in order to calculate the targeted variables. The internal variables analyzed include the profiles of temperature (δT), humidity (δq) and vertical velocity ($\delta \omega$) differences between the inside and outside of cold pools, the collaspe energy ($WAPE$), the spreading speed (C_*), as well as the Available Liftting Energy (ALE_{wk}) and Power (ALP_{wk}) variables related to cold pools for the coupling with deep convection~~for AMMA.

We ~~first validated the physics of the cold pool model for calculations of ALE_{wk}, C_* and ALP_{wk} based on the $WAPE$. For this, these three variables were recalculated in the LES using the $WAPE$, derived from the sampled $\delta\theta_v$ profiles, according to the parameterization. The values obtained were then compared to those calculated from the divergence of wind at 10 m inside cold pools (for C_*) and the vertical velocities (w_{bgust}) at the cloud base at the gust fronts (for ALE_{wk} and ALP_{wk}), also sampled in the same~~ started by validating relationship internal to the parameterizations, by diagnostics of the LES. The results show that the ALE_{wk} calculated from the $WAPE$ (computed from the vertical profile of the temperature anomaly between the cold pool and its environment) is comparable to that estimated from the vertical velocity in gust fronts w_{bgust}. This result is consistent with the model hypothesis, which estimates an equality between ALE_{wk} and $WAPE$. The spreading speed ~~(C_*)~~, determined from the mean of divergence of wind at 10 m inside cold pools, is consistent with the estimate based on the square root of $WAPE$~~. The proportionality~~ , if

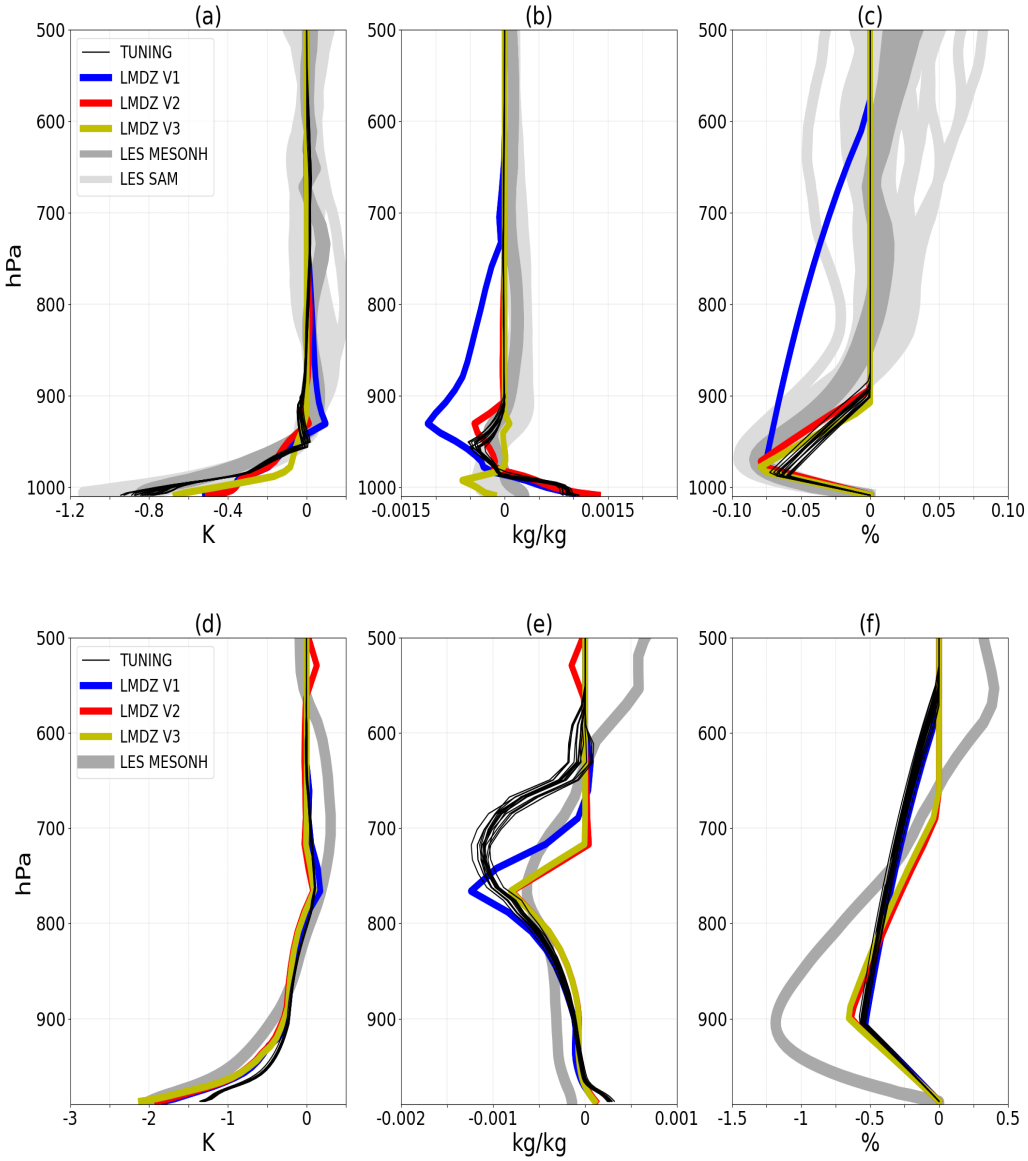

Figure 10: Vertical profiles of δT, δq and δw calculated in the LES and simulated in LMDZ TUNING, LMDZ with the adjustment of the coefficient k to 0.66 (V1), LMDZ with the drop in altitude (h_m) at which the subsidence of the air masses in cold pools is zero (V2) and LMDZ with the activation of thermals in the entire domain (V3) on the RCE case (a, b, c) and on the AMMA case (d, e, f).

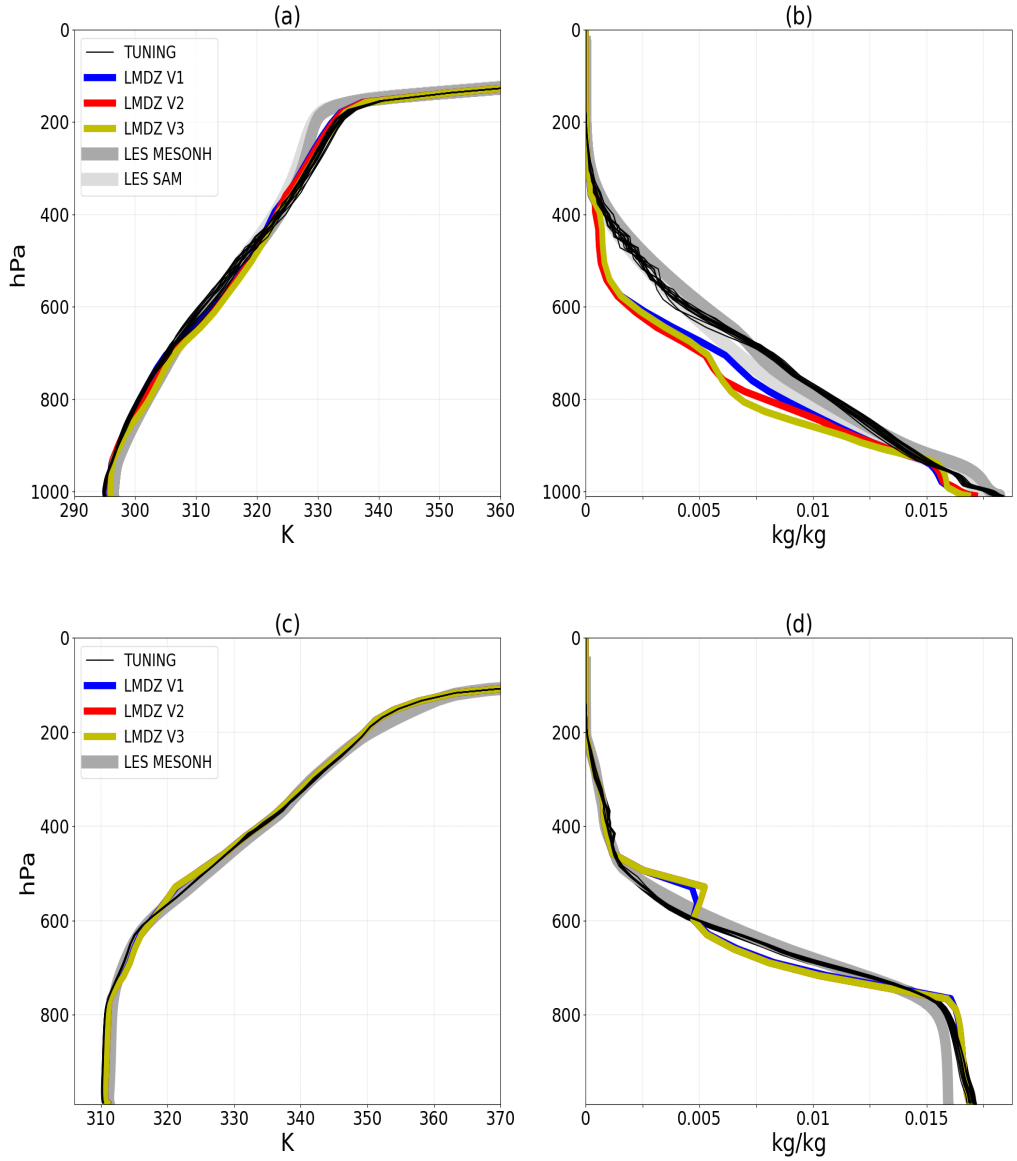

Figure 11: Vertical profiles of potential temperature (θ) and specific humidity (~~qv~~q_v) calculated in the LES and simulated in LMDZ TUNING, with the adjustment of the coefficient k to 0.66 (V1), LMDZ with the drop in altitude (h_m) at which the subsidence of the air masses in cold pools is zero (V2) and LMDZ with the activation of thermals in the entire domain (V3) on the RCE case (a, b, c) and on the AMMA case (d, e, f).

coefficient k ~~, evaluated here at~~ entering (2) is fixed to 0.66~~.~~. This value is consistent with the work of Lafore and Moncrieff (1998), and differs from the initially assumed value of 0.33 in the model. ALP_{wk}, calculated using C_* (computed from the $WAPE$ ~~(~~with $k = 0.66$), is close to the estimate derived directly from ~~the~~ w_{bgust}. This result is compatible with the model hypothesis according to which a quarter of the cold pool Avaliable Potential Power, ALP_{wk} ~~translates a transformation of the horizontal power of the pockets into a vertical power, with a conversion coefficient of 25%~~, feed deep convection, the remaining being dissipated. All of these results show the overall consistency of the model hypotheses with the three LES (RCE and AMMA) used in this study.

We then ~~compared the variables simulated by the model to those calculated in the LES by performing a simulation with a version single-column of LMDZ~~ compare with LES simulations performed with the SCM version of LMDZ LMDZ for the RCE and AMMA cases~~, using the same initial and boundary conditions as the LES.~~ .

The results show that the initial version of the parameterization represents the cold pool properties well to first order, ~~even if some biases could be identified.~~ but with a cold pool dry anomaly much too strong for the RCE case above the cold pool top, and a general tendency for both cases to underestimate the cold anomaly within cold pools and in turns $WAPE$, C_*, ALE_{wk} and ALE_{wk}.

The dry bias observed at the top of ~~the pockets in~~ cold pools the model is attributed to ~~a~~ the maximum subsidence altitude (h_m) ~~imposed at a too high level in the initial parameterization (above 600 hPa, both on the ocean and on the continent). In the LES, h_m is observed at lower altitudes: below 800 hPa for the RCE case , and below~~ which was imposed a fixed value of 600 ~~hPa for the AMMA case~~ hPa. ~~By making~~ This value which was inspired from continental situations is well suited for the AMMA case but much to small for the RCE case for which the LES indicate a value of about 800 hPa. Making h_m dependent on h_{wk} ~~to account for its regional variation, and lowering it to a level consistent with that observed in LES~~, we significantly improve the simulated humidity at the top of cold pools for both cases. These results highlight the significant impact of descending air masses in cold pools on the vertical humidity anomaly profile. They also confirm the relevance of the ~~physical model , which postulates impermeability of cold pools below the top and penetration of dry air only above this level, canceling out at a certain altitude. The differences observed in the profiles of δ_w below~~ transport model with lateral entrainment between h_m and h_{wk} ~~in the RCE case between the model and the LES are corrected when we impose, in the model, a value of the~~ feeding the maximum subsidence at h_{wk}.

Increasing the value of coefficient k ~~equal~~ ((2)) from 0.33 to 0.66~~instead of 0.33~~, as suggested by the ~~LES. This change significantly improves the representation~~ analysis of the LES, almost doubles the estimation of C_* ~~, which directly influences the profile of δ_w, depending of this speed below h_{wk}. This modification of k also significantly improved the representation of~~ for both the RCE and AMMA cases and multiplies the value of ALP_{wk} ~~in the model.~~ by 6 for AMMA and more than 10 for the RCE case, without affecting much the vertical mean and anomaly profiles. However, despite this improvements, C_* and ALP_{wk} remain underestimated in both cases.

A wet bias is also noted at the surface of cold pools in the RCE and AMMA cases. Our

analyses show that this bias is linked to the absence, in the model, of the effect of thermals on the variation of humidity at the surface of cold pools. The evaporation flux plays a weak role in this variation, which seems to be mainly controlled by thermals. To account for the effect of thermals on humidity variation in cold pools, we propose to introduce a parameterization of shallow thermals (not producing clouds) inside cold pools. ~~We also find that, in the RCE case, cold pools are warmer in the model than those in the LES. Given the coupling between the cold pools model and the deep convectionmodel, it is likely that the cold pools temperature is influenced by convective processes. To correct for this warm bias~~

Despite all the improvements, the cold pools remain not cool enough in the RCE case, inducing an underestimation of C_* by about 25% and ALP_{wk} by a factor of 6 (V2) to 9 (V3). In order to check whether this underestimation may come from a coupling with the other model parameterizations, and in particular that of deep convection, we conducted a calibration experiment using the HighTune ~~tool~~ explorer software to jointly adjust the free parameters of the cold pools and deep convection models. This tuning procedure also aimed to correct the dry and wet biases still present in the potential temperature and specific humidity profiles~~, despite the improvements made to the cold pools model~~. These adjustments led to a significant improvement in the representation of cold pool temperature in the RCE case, as well as specific humidity for the RCE and AMMA cases, even if a humid bias persists in the boundary layer for the AMMA case.

The above mentioned changes have been adopted in the new version of the LMDZ global model, used as the atmospheric component of the IPSL-CM7 coupled model under development for the forthcoming CMIP7 Fast-Trac exercise. Changes to the cold ~~pocket~~ pool model are now incorporated into the 3D version of LMDZ. Calibrated values of the free parameters for cold pools and convection can also be incorporated into the 3D version of LMDZ.

Although significant progress has been made in recent years in modeling cold pools, due to their important role in convection, challenges remain. ~~For example, the life cycle of cold pools, including their birth, death or collisions, needs to be addressed. After highlighting the impact of thermals on humidity variations within cold pools, we encourage the development of a parameterization of thermals capable of taking into account their influence without leading to cloud formation. The~~ First a simple parameterization of boundary layer convective transport, based for instance on a simplified version of the thermal plume model, could be included to better represent vertical mixing within the cold pools without activating the thermal plume model uniformly over the grid cell. The cold pool number density should become an internal variable of the model since we know it presents very different values when considering popcorn like convection over ocean or continents, or well organized long live system such as squall lines. A parameterization of this number density, based on a population dynamic model is presently under test. To end with, the issue of the propagation of cold pools from grid cell to grid cell needs to be also integrated into GCMs~~, as well as the wind gusts associated with their spreading~~.

References

Böing, S. J., Jonker, H. J., Siebesma, A. P., and Grabowski, W. W. (2012). Influence of the subcloud layer on the development of a deep convective ensemble. *Journal of the Atmospheric Sciences*, 69(9):2682–2698.

Boucher, O., Denvil, S., Levavasseur, G., Cozic, A., Caubel, A., Foujols, M.-A., Meurdesoif, Y., Balkanski, Y., Checa-Garcia, R., Hauglustaine, D., et al. (2020). Ipsl ipsl-cm6a-lr-inca model output prepared for cmip6 rfmip piclim-aer.

Brown, A., Cederwall, R. T., Chlond, A., Duynkerke, P. G., Golaz, J.-C., Khairoutdinov, M., Lewellen, D., Lock, A., MacVean, M., Moeng, C.-H., et al. (2002). Large-eddy simulation of the diurnal cycle of shallow cumulus convection over land. *Quarterly Journal of the Royal Meteorological Society: A journal of the atmospheric sciences, applied meteorology and physical oceanography*, 128(582):1075–1093.

Bryan, G. H. (2005). Spurious convective organization in simulated squall lines owing to moist absolutely unstable layers. *Monthly weather review*, 133(7):1978–1997.

Couvreux, F., Hourdin, F., Williamson, D., Roehrig, R., Volodina, V., Villefranque, N., Rio, C., Audouin, O., Salter, J., Bazile, E., et al. (2021). Process-based climate model development harnessing machine learning: I. a calibration tool for parameterization improvement. *Journal of Advances in Modeling Earth Systems*, 13(3):e2020MS002217.

Couvreux, F., Rio, C., Guichard, F., Lothon, M., Canut, G., Bouniol, D., and Gounou, A. (2012). Initiation of daytime local convection in a semi-arid region analysed with high-resolution simulations and amma observations. *Quarterly Journal of the Royal Meteorological Society*, 138(662):56–71.

Daleu, C. L., Plant, R., Woolnough, S. J., Sessions, S., Herman, M., Sobel, A., Wang, S., Kim, D., Cheng, A., Bellon, G., et al. (2015). Intercomparison of methods of coupling between convection and large-scale circulation: 1. comparison over uniform surface conditions. *Journal of Advances in Modeling Earth Systems*, 7(4):1576–1601.

Diallo, F., Hourdin, F., Rio, C., Traore, A.-K., Mellul, L., Guichard, F., and Kergoat, L. (2017). The surface energy budget computed at the grid-scale of a climate model challenged by station data in west africa. *Journal of Advances in Modeling Earth Systems*, 9(7):2710–2738.

Dirmeyer, P. A., Cash, B. A., Kinter, J. L., Jung, T., Marx, L., Satoh, M., Stan, C., Tomita, H., Towers, P., Wedi, N., et al. (2012). Simulating the diurnal cycle of rainfall in global climate models: Resolution versus parameterization. *Climate dynamics*, 39:399–418.

Dorrestijn, J., Crommelin, D. T., Siebesma, A. P., and Jonker, H. J. (2013). Stochastic parameterization of shallow cumulus convection estimated from high-resolution model data. *Theoretical and Computational Fluid Dynamics*, 27:133–148.

Emanuel, K. A. (1991). A scheme for representing cumulus convection in large-scale models. *Journal of Atmospheric Sciences*, 48(21):2313–2329.

Feng, Z., Hagos, S., Rowe, A. K., Burleyson, C. D., Martini, M. N., and de Szoeke, S. P. (2015). Mechanisms of convective cloud organization by cold pools over tropical warm ocean during the amie/dynamo field campaign. *Journal of Advances in Modeling Earth Systems*, 7(2):357–381.

Grandpeix, J.-Y. and Lafore, J.-P. (2010). A density current parameterization coupled with emanuel's convection scheme. part i: The models. *Journal of the Atmospheric Sciences*, 67(4):881–897.

Grandpeix, J.-Y., Lafore, J.-P., and Cheruy, F. (2010). A density current parameterization coupled with emanuel's convection scheme. part ii: 1d simulations. *Journal of the Atmospheric Sciences*, 67(4):898–922.

Grandpeix, J.-Y., Phillips, V., and Tailleux, R. (2004). Improved mixing representation in emanuel's convection scheme. *Quarterly Journal of the Royal Meteorological Society: A journal of the atmospheric sciences, applied meteorology and physical oceanography*, 130(604):3207–3222.

Grant, L. D., Lane, T. P., and van den Heever, S. C. (2018). The role of cold pools in tropical oceanic convective systems. *Journal of the Atmospheric Sciences*, 75(8):2615–2634.

Guichard, F., Petch, J., Redelsperger, J.-L., Bechtold, P., Chaboureau, J.-P., Cheinet, S., Grabowski, W., Grenier, H., Jones, C., Köhler, M., et al. (2004). Modelling the diurnal cycle of deep precipitating convection over land with cloud-resolving models and single-column models. *Quarterly Journal of the Royal Meteorological Society: A journal of the atmospheric sciences, applied meteorology and physical oceanography*, 130(604):3139–3172.

Haerter, J. O. and Schlemmer, L. (2018). Intensified cold pool dynamics under stronger surface heating. *Geophysical Research Letters*, 45(12):6299–6310.

Hourdin, F., Couvreux, F., and Menut, L. (2002). Parameterisation of the dry convective boundary layer based on a mass flux representation of thermals. *Journal of the Atmospheric Sciences*, 59:1105–1123.

Hourdin, F., Foujols, M.-A., Codron, F., Guemas, V., Dufresne, J.-L., Bony, S., Denvil, S., Guez, L., Lott, F., Ghattas, J., et al. (2013). Impact of the lmdz atmospheric grid configuration on the climate and sensitivity of the ipsl-cm5a coupled model. *Climate Dynamics*, 40:2167–2192.

Hourdin, F., Jam, A., Rio, C., Couvreux, F., Sandu, I., Lefebvre, M.-P., Brient, F., and Idelkadi, A. (2019). Unified Parameterization of Convective Boundary Layer Transport and Clouds With the Thermal Plume Model.

Hourdin, F., Musat, I., Bony, S., Braconnot, P., Codron, F., Dufresne, J.-L., Fairhead, L., Filiberti, M.-A., Friedlingstein, P., Grandpeix, J.-Y., et al. (2006). The lmdz4 general circulation model: climate performance and sensitivity to parametrized physics with emphasis on tropical convection. *Climate Dynamics*, 27:787–813.

Hourdin, F., Rio, C., Grandpeix, J.-Y., Madeleine, J.-B., Cheruy, F., Rochetin, N., Jam, A., Musat, I., Idelkadi, A., Fairhead, L., et al. (2020). Lmdz6a: The atmospheric component of the ipsl climate model with improved and better tuned physics. *Journal of Advances in Modeling Earth Systems*, 12(7):e2019MS001892.

Hourdin, F., Rio, C., Jam, A., Traore, A.-K., and Musat, I. (2020). Convective Boundary Layer Control of the Sea Surface Temperature in the Tropics. *J. of Adv. in Modeling Earth Systems*, 12(6):e01988.

Hourdin, F., Williamson, D., Rio, C., Couvreux, F., Roehrig, R., Villefranque, N., Musat, I., Fairhead, L., Diallo, F. B., and Volodina, V. (2021). Process-based climate model development harnessing machine learning: Ii. model calibration from single column to global. *Journal of Advances in Modeling Earth Systems*, 13(6):e2020MS002225.

Jam, A., Hourdin, F., Rio, C., and Couvreux, F. (2013). Resolved Versus Parametrized Boundary-Layer Plumes. Part III: Derivation of a Statistical Scheme for Cumulus Clouds. 147:421–441.

Jeevanjee, N. and Romps, D. M. (2013). Convective self-aggregation, cold pools, and domain size. *Geophysical Research Letters*, 40(5):994–998.

Kendon, E. J., Roberts, N. M., Senior, C. A., and Roberts, M. J. (2012). Realism of rainfall in a very high-resolution regional climate model. *Journal of Climate*, 25(17):5791–5806.

Khairoutdinov, M. and Randall, D. (2006). High-resolution simulation of shallow-to-deep convection transition over land. *Journal of the atmospheric sciences*, 63(12):3421–3436.

Khairoutdinov, M. F. and Randall, D. A. (2003). Cloud resolving modeling of the arm summer 1997 iop: Model formulation, results, uncertainties, and sensitivities. *Journal of the Atmospheric Sciences*, 60(4):607–625.

Kurowski, M. J., Suselj, K., Grabowski, W. W., and Teixeira, J. (2018). Shallow-to-deep transition of continental moist convection: Cold pools, surface fluxes, and mesoscale organization. *Journal of the Atmospheric Sciences*, 75(12):4071–4090.

Lac, C., Chaboureau, J.-P., Masson, V., Pinty, J.-P., Tulet, P., Escobar, J., Leriche, M., Barthe, C., Aouizerats, B., Augros, C., et al. (2018). Overview of the meso-nh model version 5.4 and its applications. *Geoscientific Model Development*, 11(5):1929–1969.

Lafore, J.-P. and Moncrieff, M. W. (1989). A numerical investigation of the organization and interaction of the convective and stratiform regions of tropical squall lines. *Journal of Atmospheric Sciences*, 46(4):521–544.

Legay, A., Deremble, B., and Burchard, H. (2025). Derivation and implementation of a non-local term to improve the oceanic convection representation within the k–ϵ parameterization. *Journal of Advances in Modeling Earth Systems*, 17(1):e2024MS004243.

Lothon, M., Campistron, B., Chong, M., Couvreux, F., Guichard, F., Rio, C., and Williams, E. (2011). Life cycle of a mesoscale circular gust front observed by a c-band doppler radar in west africa. *Monthly weather review*, 139(5):1370–1388.

Meyer, B. and Haerter, J. O. (2020). Mechanical forcing of convection by cold pools: Collisions and energy scaling. *Journal of Advances in Modeling Earth Systems*, 12(11):e2020MS002281.

Pantillon, F., Knippertz, P., Marsham, J. H., and Birch, C. E. (2015). A parameterization of convective dust storms for models with mass-flux convection schemes. *Journal of the Atmospheric Sciences*, 72(6):2545–2561.

Provod, M., Marsham, J., Parker, D., and Birch, C. (2016). A characterization of cold pools in the west african sahel. *Monthly Weather Review*, 144(5):1923–1934.

Qian, L., Young, G. S., and Frank, W. M. (1998). A convective wake parameterization scheme for use in general circulation models. *Monthly weather review*, 126(2):456–469.

Randall, D., Khairoutdinov, M., Arakawa, A., and Grabowski, W. (2003). Breaking the cloud parameterization deadlock. *Bulletin of the American Meteorological Society*, 84(11):1547–1564.

Redelsperger, J.-L., Diedhiou, A., Flamant, C., Janicot, S., Lafore, J.-P., Lebel, T., Polcher, J., Bourlès, B., Caniaux, G., de Rosnay, P., et al. (2006). Amma, une étude multidisciplinaire de la mousson ouest-africaine. *La meteorologie*, 54:22–32.

Rio, C. and Hourdin, F. (2008). A thermal plume model for the convective boundary layer: Representation of cumulus clouds. *Journal of the atmospheric sciences*, 65(2):407–425.

Rio, C., Hourdin, F., Couvreux, F., and Jam, A. (2010). Resolved versus parametrized boundary-layer plumes. part ii: continuous formulations of mixing rates for mass-flux schemes. *Boundary-layer meteorology*, 135:469–483.

Rio, C., Hourdin, F., Grandpeix, J.-Y., and Lafore, J.-P. (2009). Shifting the diurnal cycle of parameterized deep convection over land. *Geophysical Research Letters*, 36(7).

Rochetin, N., Grandpeix, J.-Y., Rio, C., and Couvreux, F. (2014). Deep convection triggering by boundary layer thermals. part ii: Stochastic triggering parameterization for the lmdz gcm. *Journal of the Atmospheric Sciences*, 71(2):515–538.

Rochetin, N., Hohenegger, C., Touzé-Peiffer, L., and Villefranque, N. (2021). A physically based definition of convectively generated density currents: Detection and characterization in convection-permitting simulations. *Journal of Advances in Modeling Earth Systems*, 13(7):e2020MS002402.

Rotunno, R., Klemp, J. B., and Weisman, M. L. (1988). A theory for strong, long-lived squall lines. *Journal of Atmospheric Sciences*, 45(3):463–485.

Sadourny, R. (1984). January and july performances of the lmd general circulation model. *New perspectives in climate modeling*.

Siebesma, A. P., Bretherton, C. S., Brown, A., Chlond, A., Cuxart, J., Duynkerke, P. G., Jiang, H., Khairoutdinov, M., Lewellen, D., Moeng, C.-H., et al. (2003). A large eddy simulation intercomparison study of shallow cumulus convection. *Journal of the Atmospheric Sciences*, 60(10):1201–1219.

Stephens, G. L., L'Ecuyer, T., Forbes, R., Gettelmen, A., Golaz, J.-C., Bodas-Salcedo, A., Suzuki, K., Gabriel, P., and Haynes, J. (2010). Dreary state of precipitation in global models. *Journal of Geophysical Research: Atmospheres*, 115(D24).

Strauss, C., Ricard, D., Lac, C., and Verrelle, A. (2019). Evaluation of turbulence parametrizations in convective clouds and their environment based on a large-eddy simulation. *Quarterly Journal of the Royal Meteorological Society*, 145(724):3195–3217.

Tan, J., Oreopoulos, L., Jakob, C., and Jin, D. (2018). Evaluating rainfall errors in global climate models through cloud regimes. *Climate Dynamics*, 50:3301–3314.

Tompkins, A. M. (2001). Organization of tropical convection in low vertical wind shears: The role of cold pools. *Journal of the atmospheric sciences*, 58(13):1650–1672.

Torri, G. and Kuang, Z. (2019). On cold pool collisions in tropical boundary layers. *Geophysical Research Letters*, 46(1):399–407.

Touzé-Peiffer, L., Vogel, R., and Rochetin, N. (2022). Cold pools observed during eurec 4 a: Detection and characterization from atmospheric soundings. *Journal of Applied Meteorology and Climatology*, 61(5):593–610.

Vogel, R., Konow, H., Schulz, H., and Zuidema, P. (2021). A climatology of trade-wind cumulus cold pools and their link to mesoscale cloud organization. *Atmospheric Chemistry and Physics*, 21(21):16609–16630.

Weisman, M. L. and Rotunno, R. (2004). "a theory for strong long-lived squall lines" revisited. *Journal of the Atmospheric Sciences*, 61(4):361–382.

Williamson, D., Goldstein, M., Allison, L., Blaker, A., Challenor, P., Jackson, L., and Yamazaki, K. (2013). History matching for exploring and reducing climate model parameter space using observations and a large perturbed physics ensemble. *Climate dynamics*, 41:1703–1729.

Yamada, T. (1983). Simulations of nocturnal drainage flows by a q^2l turbulence closure model. 40:91–106.

Young, G. S., Perugini, S. M., and Fairall, C. (1995). Convective wakes in the equatorial western pacific during toga. *Monthly Weather Review*, 123(1):110–123.

Zuidema, P., Torri, G., Muller, C., and Chandra, A. (2017). A survey of precipitation-induced atmospheric cold pools over oceans and their interactions with the larger-scale environment. *Surveys in Geophysics*, 38(6):1283–1305.

A Tungin experiment

A.1 High-Tune Explorer (HTExplo) tool

General circulation models, used for global warming projections, are essentially based on a separation between the dynamical core, which manages large-scale air movements, and the physical parameterizations, enabling the impact of subgrid processes on the large scale to be represented. Progress in improving these models has been slow in recent years, not only because of the difficulties of integrating these processes into the parameterizations, but also because of the complex tuning of the many free parameters involved in their formulation. This is the background to the development of the High-Tune Explorer (HTExplo) tool.

HTExplo has been developed in collaboration between the LMD (Paris), the Centre National de Recherche Météorologiques (CNRM/Météo-France) and the University of Exeter (UK). It is an automatic calibration tool for free parameters, based on machine learning techniques from the uncertainty quantification community (Williamson et al., 2013). This approach proposes a new calibration paradigm: instead of optimizing parameter values, it aims to identify the subset of parameters that enables the model to reproduce certain observables to a certain accuracy. The main steps involved in using the tool, as well as its mathematical foundations, are well described in Couvreux et al. (2021). The HTExplo tool was used for the first time in a SCM/LES comparison on several boundary layer cases of the LMDZ model, in order to characterize the subspace of free parameter values for which SCM simulations are consistent with LES for certain metrics and a given tolerance (Couvreux et al., 2021). This information was then used by Hourdin et al. (2021) to calibrate the 3D configuration. These authors demonstrated how reducing the parameter space using this method significantly saves computing and human resources. They also pointed out that this approach eases the burden on the modeler, enabling him or her to concentrate more on understanding and improving the physical parameterizations of the model.