



Towards a more correct and relevant explanation of the greenhouse effect

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Presenting the greenhouse effect as an atmosphere that warms the surface by emitting infrared radiation towards the surface:

- Is inconsistent (false) with the definition of its measure: $G = F_s F_e$
- Logically leads one to question the role of CO₂ in the greenhouse effect (saturation effect), to fail to understand why high clouds have a greater greenhouse effect than low clouds, etc.
- Doesn't allow for an answer to these legitimate questions.

Programme d'enseignement scientifique de Terminale (section 2.2, p.9)

"Lorsque la concentration des GES augmente, l'atmosphère absorbe davantage le rayonnement thermique infrarouge émis par la surface de la Terre. Il en résulte une augmentation de la puissance radiative reçue par la surface terrestre de l'atmosphère. Cette puissance additionnelle entraîne une perturbation de l'équilibre radiatif qui existait à l'ère préindustrielle [...] ce qui se traduit par une augmentation de la température moyenne à la surface de la Terre [...]" (MEN 2023, p.9) Towards a more correct and relevant explanation of the greenhouse effect

- I. Conceptual framework
- II. Principle of the greenhouse effect
- III. Gaz absorption, emission height and the greenhouse effect
- IV. Focus on the CO₂ greenhouse effect
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Emergence of climate physics

J. Fourier, 1824: Mémoire sur les températures du globe terrestre et des espaces planétaires

(https://www.academie-sciences.fr/pdf/dossiers/Fourier/Fourier_pdf/Mem1827_p569_604.pdf) *English traduction in* American Journal of Science, Vol. 32, N°1, 1837.

+ R. Pierrehumbert https://geosci.uchicago.edu/~rtp1/papers/Fourier1827Trans.pdf

> He consider the Earth like any other planet

>The energy balance equation drives the temperature of all the planets

- > The major heat transfers are
 - 1. Solar radiation
 - 2. Infra-red radiation
 - 3. Diffusion with the interior of Earth
- The heat diffusion with the interior of Earth has a negligible impact on the surface temperature
- Contradicts the thermal death of Earth



Joseph Fourier



He formulated what would later be called the 'greenhouse effect'. «C'est ainsi que la température est augmentée par l'interposition de l'atmosphère, parce que la chaleur trouve moins d'obstacle pour pénétrer l'air, étant à l'état de lumière, qu'elle n'en trouve pour repasser dans l'air lorsqu'elle est convertie en chaleur obscure »

"it is thus that the temperature is augmented by the interposition of the atmosphere, because the heat has less trouble penetrating the air when it is in the form of light, than it has exiting back through the air after it has been converted to dark heat."

Emergence of climate physics

J. Fourier, 1824: Mémoire sur les températures du globe terrestre et des espaces planétaires

(https://www.academie-sciences.fr/pdf/dossiers/Fourier/Fourier_pdf/Mem1827_p569_604.pdf) *English traduction in* American Journal of Science, Vol. 32, N°1, 1837.

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He **envisages the importance of any change of the sun.** «Les moindres variations de la distance de cet astre à la Terre occasionneraient des changements très considérables dans les températures, l'excentricité de l'orbite terrestre donnerait naissance à diverses saisons. »

"The least variation of the distance of the Earth from this star would lead to considerable changes in the temperature, and the eccentricity of the Earth's orbit would give rise to new forms of seasonal variations"

He refuted this possibility, which led him to assume the existence of a "temperature of space", which he took to be equal to that of the poles in winter.

He **envisages that climate may change**: « L'établissement et le progrès des sociétés humaines, l'action des forces naturelles peuvent changer notablement, et dans de vastes contrées, l'état de la surface du sol, la distribution des eaux et les grands mouvements de l'air. De tels effets sont propres à faire varier, dans le cours de plusieurs siècles, le degré de la chaleur moyenne; car les expressions analytiques comprennent des coefficients qui se rapportent à l'état superficiel et qui influent beaucoup sur la valeur de la température.»

"The establishment and progress of human societies, and the action of natural forces, can notably change the state of the ground surface over vast regions, as well as the distribution of waters and the great movements of the air. Such effects have the ability to make the mean degree of heat vary over the course of several centuries, for the analytic expressions contain coefficients which depend on the state of the surface, and which greatly influence the temperature."

Energy budget at the surface or at the top of atmosphere?



Steady state (energy equilibrium): the energy balance is zero at both interfaces.

• The Earth (and other planets) is an open system with the rest of the universe

• Incoming solar radiation is independent of the radiation emitted by the Earth

- Atmosphere and surface are two open systems
- Strong energy coupling between surface and atmosphe

Single column model (from the 60's)



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opposite direction to that of the stratosphere

[[]Manabe and Wetherald, 1967]

Vertical profile of the atmosphere

Stratosphere:

- Radiative equilibrium
- •Temperature driven by radiation

Troposphere:

- Radiative-convective equilibrium
- •Temperature profile driven by the thermodynamic



Fraction of the total mass of air below this altitude

99.9%

80-90%

Impact of clouds on LW radiative flux

Simplification: Clouds ≈ blackbody in the LW ; no absorption in the SW No LW absorption by the atmosphere



Observation from Meteosat satellite

Visible (0.5-0.9µm)



http://www.meteo-spatiale.fr/src/autres_sources.php



Emission (brightness) temperature: White: warm. Black: cold

Impact of clouds on LW radiative flux



• The relative impact of high and low level clouds on radiative flux is opposite at the TOA and at surface

• For climate, the radiative budget at the TOA is central (cf. [Manabe & Wetherald, 1967])

Equilibrium temperature of planet Earth

I₀=1364 W.m⁻²

A = 0.3

Greenhouse effect

G = F₂-F₂ ≈ 160 Wm⁻²

Average incoming solar radiation on a sphere: $I_s = I_0/4$

absorbed solar (shortwave) radiation: $F_a = (1-A) I_0/4 = 240W.m^{-2}$ We assume the surface temperature is uniform

emitted terrestrial (longwave) radiation: $F_e = \epsilon \sigma T_e^4$

Steady state: the heat power gained by absorption is equal to that lost by emission: $F_a = F_e$

 $\sigma \epsilon T_e^4 = (1 - A)I_0/4$

longwave radiation **emitted by the Earth** toward space: **F**_a = **240** W.m⁻²

longwave radiation **emitted by** surface: $F_{c} \approx 400 \text{ W.m}^{-2}$ **T**_e: Emission temperature

*T*_e= 255*K* (-18°*C*)

Global mean surface temperature $T_s \approx 16.5^{\circ}C$

Energy flows in the Earth atmosphere



[IPCC AR6, ch7, 2021; Trenberth & Fasullo, 2012]

Same, redesigned by Saint-Lu & Dufresne Also in Peixoto and Oort, 1992

Equilibrium temperature of planet Earth

The energy budget must be considered at the top of atmosphere, not at the surface

The link between the energy budget and the Earth's surface temperature will be decomposed into two parts:

- *how the flux emitted by the Earth towards space depends on Earth's state* (including greenhouse gas concentration, surface and atmosphere temperature)

- how the Earth's temperature depends on its energy balance

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Spontaneous emission of radiation



With $\sigma = 5,67 \ 10^{-8}$: Stefan-Boltzmann constant, *F* in W.m⁻², T in K

The flux emitted by a medium is an increasing function of temperature

Spontaneous emission of radiation

Planck law ("Black body" emission)

$$B_{\lambda}(T) = \frac{C_1 \,\lambda^{-5}}{\pi \,\left(e^{C_2/\lambda T} - 1\right)}$$

 B_{λ} in W.m⁻².µm⁻¹.sr⁻¹

T in K, C₁ et C₂ are constants

Semi-transparent media:

 $L_{\lambda}(T) = \varepsilon_{\lambda} B_{\lambda}(T)$ with ε_{λ} spectral emissivity

 $(0 \le \varepsilon_{\lambda} \le 1; \text{ black body: } \varepsilon_{\lambda}=1)$

Kirchhoff law: emissivity ε_{λ} = absorptivity α_{λ} at the spectral level

Stefan-Boltzmann law (integral of the Planck law over the whole spectrum and over an hemisphere).

Power *F* lost by emission of radiation by a body of temperature *T* : $F = \sigma T^4$

With $\sigma = 5,67 \ 10^{-8}$: Stefan-Boltzmann constant, *F* in W.m⁻², T in K

The flux emitted by a medium is an increasing function of temperature



Radiation absorption by the atmosphere



Spontaneous emission of radiation





The flux emitted by a medium is an increasing function of temperature

The camera indicates a temperature, but it actually measures the power of the infrared radiation it receives.

This radiation is partially reflected by a pane of glass, like visible radiation.

[Maron et al., 2025]



Forte puissance de rayonnement infrarouge

Faible puissance de rayonnement infrarouge

A : Plus la température d'un objet est élevée, plus la puissance de rayonnement infrarouge qu'il émet est grande.



A material can be transparent or opaque, and these properties depend on wavelength, can be different for visible and infrared radiation.



If the plates are heated, the wood and glass emit more radiation, while the plastics emit less. *A material that is a good absorber of infrared radiation is also a good emitter.* Kirchhoff law: absorptivity = emissivity ; $\alpha_{\lambda} = \varepsilon_{\lambda}$



high

ΝO

Infrared "CO₂" camera

background temperature : 20°C

balloons temperature (and gas temperature inside): 5°C





high

0€

Infrared "CO₂" camera

background temperature : 20°C

balloons temperature (and gas temperature inside): **30°C**

Observed LW radiative flux which balloon contains air? CO₂?

background temperature : 20°C



high

ΝO

balloons temperature (and gas temperature inside): **5°C**



[Maron et al., 2025]

The greenhouse effect



Same Warm surface Cool atmosphere

Measure of greenhouse effect:

$$\mathbf{G} = \mathbf{F}_{s} - \mathbf{F}_{e} = [\mathbf{B}(\mathbf{T}_{s}) - \mathbf{B}(\mathbf{T}_{e})] \mathbf{A}(\mathbf{0}, \infty)$$

The greenhouse effect depends on:

difference between surface temperature and atmosphere emission temperature via the Planck function

absorptivity of the whole atmosphere

The greenhouse effect is all the more important when:

- absorptivity of the atmosphere in the infrared range is high
- difference between atmosphere emission temperature and surface temperature is large.

The greenhouse effect

Clouds \approx blackbody in the LW



Magnitude of the greenhouse effect $G = F_s - F_e$ F_s : flux emitted by the surface

 F_e : flux emitted by the Earth toward space

The flux emitted by a medium is an **increasing function of temperature** (Planck law)

• High level clouds have a large greenhouse effect because their temperature is much lower than that of surface

When computing G, both flux $F_{\rm s}$ anf $F_{\rm e}$ need to be positive

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Absorption by gases



Absorption coefficient for an absorption line *i* at frequence *v*:

 $k_{v,i} = n S_i f_{v,i}$ with: *n* : molecular density (mol/kg) *S_i* : line instensity (m²/mol) *f_{v,i}* : line profile (-)

- Line emission and absorption by transition between states of different energy
- In the infra-red: level of energy correspond to change in vibration and vibration-rotation of molecules
- Complex molecules are better absorbing



Absorption by gases



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Typical radiative properties of the Earth atmosphere

Optical thickness:
$$\tau_{\nu}(\infty, 0) = \int_{\infty}^{0} k_{\nu}(z) \rho(z) dz$$

With k_{ν} extinction coef. (m²/kg) and ρ volume mass of absorbing gas (kg/m³)

Transmissivity: $T_{\nu}(\infty,0) = e^{-\tau_{\nu}(\infty,0)}$ Absorptivity: $A_{\nu}(\infty,0) = 1 - T_{\nu}(\infty,0)$

Assuming no scattering



Very wide range of optical thickness, of absorption intensity

Line-by-line radiative transfer model



The concept of emission height



Analogy with the visibility distance







[Dufresne et Treiner, 2011]

Greenhouse effect in a *stratified* atmosphere

dT/dz constrained by convection



FLW: outgoing infrared (LW) radiation Ze: emission height

Visible zone (photons emitted upwards reach the space)



Hidden zone (photons emitted upwards are absorbed and do not reach the space)

[Dufresne, Treiner, 2011]
Greenhouse effect in a *stratified* atmosphere

dT/dz constrained by convection



The concept of emission height



reaching space has been emitted at altitude z for different optical thicknesses of the atmosphere

[Dufresne et al., 2020]

The concept of emission height



[Dufresne et al., 2020]

Spectrum of the radiation emitted by the Earth as measured by satellites



The greenhouse effect

Measure of the **greenhouse effect** : *difference* between the radiative *flux emitted by the surface* and the radiative *flux emitted by the planet* (i.e. the outgoing flux at the top of atmosphere (TOA)

$$G = F_s - F_{TOA} = \int_{v} [F_{v,s} - F_{v,TOA}] dv$$
 both flux F being positive



The greenhouse effect



The greenhouse effect is all the more important when:

- absorptivity of the atmosphere in the infrared range is high, over a wide spectral domain
- difference between atmosphere emission temperature and surface temperature is large.

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The CO₂ saturation paradox $G=F_s-F_e=\int_{v} [B_v(T_s)-B_v(T_e)] A_v(0,\infty)dv$



when there is some H₂O?



Why does the greenhouse effect increase with CO_2 while absorptivity does not when there is some H₂O?

The CO₂ saturation paradox



The water vapor masks the CO_2 absorption by does not "mask" the radiative effect of CO_2 because:

1) Over a wide spectral range, the optical thickness of CO_2 is larger than that of $H_2O =>$ There, the emission temperature depends only on CO_2

2) This effect is amplified as most of the water vapor is close to the surface

The CO₂ saturation paradox

Absorptivity of the atmosphere between the TOA and

surface

an altitude of **5km**



Why CO₂ radiative forcing is a logaritmic in CO₂ concentration?



The greenhouse effect due to CO₂

Absorption by CO_2 is not saturated when CO_2 is the only absorbing gas

 H_2O does not mask the greenhouse effect of CO_2 because the emission height of CO_2 is greater than that of H_2O in the spectral range where both absorb

When increasing CO_2 concentration, the increase in the greenhouse effect is due to

- an increase in spectral absorptivity (when below 1)
- an increase in emission altitude and therefore a decrease in emission temperature in the troposphere



Presenting the greenhouse effect as an atmosphere that warms the surface by emitting infrared radiation towards the surface:

- Is inconsistent (false) with the definition of its measure: $G = F_s F_e$
- Logically leads one to question the role of CO_2 in the greenhouse effect (saturation effect, masking of CO_2 by H_2O), to fail to understand why high clouds have a greater greenhouse effect than low clouds, etc.
- Doesn't allow for an answer to these legitimate questions.

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From radiative forcing to temperature change

We analyze how the flux emitted by the Earth towards space depends on greenhouse gaz concentration **all other conditions being equal**. What about the Earth's surface temperature response ? Answering this question requires considering **the whole physics of climate, i.e. global climate models**

Radiative forcing and feedback framework

In response to an external forcing, the response ΔN of the net flux at the TOA, may be expressed as:



The *radiative forcing* ΔQ is the change in the net radiative flux N (W.m⁻²) at the top of atmosphere due to the external forcing without the surface temperature T_s adjusting to this perturbation. The radiative forcing aims to compare the magnitude of different perturbations that impact climate.

The *climate feedback parameter* λ (W m⁻² K⁻¹) is the **sensitivity of the net radiative flux N** at the top of atmosphere due to a change in the surface temperature T_s



CO₂ forcing with stratospheric adjustment



Emission height

Change in emission height for a doubling of co₂ concentration

Change in radiative flux at the top of the atmosphere

[Dufresne et al., 2020]

CO₂ forcing with stratospheric adjustment





(Dufresne & Bony, 2008)

Temperature response to a CO₂ doubling forcing



$$\Delta N = 0 \Rightarrow \Delta T_s = -\frac{\Delta Q}{\lambda} \qquad \lambda = \lambda_P + \lambda_w + \lambda_A + \lambda_C$$



(Dufresne & Bony, 2008)

Energy flows in the Earth atmosphere



[IPCC AR6, ch7, 2021; Trenberth & Fasullo, 2012]

Same, redesigned by Saint-Lu & Dufresne Also in Peixoto and Oort, 1992

After an increase in CO_2 , the power of the infrared radiation emitted by the atmosphere towards the surface increases mainly because of the increase in temperature and water vapour, not because of the increase in CO_2 .

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Would you like to

visit my lab?

https://www.grandiloquents.fr/en/chimat (pedagogical content to use it in class

Why is the CO2

balloon a darker

colour?

es fr pl pt If you are interested for a translation in your language,

contact me

woooh!

lt's a little more complicated for earth.

But not to worry ...

en ₩₩

CO

de

Any feedback

very welcome !

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Further readings

Greenhouse effect:

• V Maron, JL Dufresne, LP Pelissier, A Rabier, M. Cochepin, "Quelles expériences et quelles représentations pour construire le lien entre CO₂ et réchauffement climatique avec des non spécialistes ?", 2025,

https://hal.science/hal-04744461v1

• Dufresne J.-L., V. Eymet, C. Crevoisier, J-Y Grandeix; Greenhouse effect: the relative contributions of emission height and total absorption, J. of Climate, 33(9), 3827-3844, https://doi.org/10.1175/JCLI-D-19-0193.1

• Dufresne J.-L., J. Treiner (2011), L'effet de serre atmosphérique: plus subtil qu'on ne le croit!, La Météorologie, No. 72, pp. 31-41, http://dx.doi.org/10.4267/2042/39839

• Pierrehumbert R.T.; Infrared radiation and planetary temperature. Physics Today 1 January 2011; 64 (1): 33–38. https://doi.org/10.1063/1.3541943

• Benestad, R. E. (2017). "A mental picture of the greenhouse effect". Theor Appl Climatol. 128 (3–4): 679–688. doi:10.1007/s00704-016-1732-y

IPCC AR6 Technical Summary. In Climate Change 2021: The Physical Science Basis. Contribution of Working Group I to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change [Masson-Delmotte, V. et al. (eds.)]. Cambridge University Press, pp. 33–144. doi:10.1017/9781009157896.002

Vidéo:

• Science Etonnate: SATURATION de l'EFFET DE SERRE : Le réchauffement a-t-il atteint sa limite ? , par David Louapre: https://scienceetonnante.com/2023/10/06/la-saturation-de-leffet-de-serre/

• Sabine Hossenfelder: I Misunderstood the Greenhouse Effect. Here's How It Works. https://www.youtube.com/watch?v=oqu5DjzOBF8



[NASA]

Solar radiation dominates Earth energy inputs

Rayonnement électromagnétique reçu du Soleil (principalement visible et IR)	1,7 10 ¹⁷ W
Géothermie (radioactivités à période longue : ²³⁸ U, ²³⁵ U, ²³² Th, ⁴⁰ K)	~ 4,4 10 ¹³ W
Civilisation en 2010 (~10 ⁹ humains consommant 10 t de pétrole/an)	1,6 10 ¹³ W
Énergie rotative dissipée par les marées	2,8 10 ¹² W
Vent solaire (pour « cible magnétosphérique » de 25 $R_{Terre} \sim 10^{14} \text{ W}$)	~ 2 10 ¹¹ W
Rayonnement du fond cosmologique (corps noir* à 2,7 K)	1,6 10 ⁹ W
Rayonnement électromagnétique reçu des étoiles (visible, IR)	~ 1,3 10 ⁹ W
Rayonnement cosmique (protons, alphas)	9 10 ⁸ W
Météorites (~ 30000 tonnes par an, supposant $v_{impact} \approx$ 20 km/s)	~ 2 10 ⁸ W

Surface of the Earth: 510 10^{12} m² 1 PW = 10^{15} W

Source : P. von Balmoos in Le Climat à Découvert, CNRS éditions, 2011

1.4 Vertical Structure of Planetary Atmospheres



[Stamnes, 2008]

Spectrum of the radiation emitted by the Earth as measured by satellites



Gaz absorption in the atmosphere

Optical thickness:

Absorptivity:



Gaz absorption in the atmosphere

Optical thickness:

Absorptivity:



LW flux at the TOA



$$\frac{d L_{v}}{d z} = k_{v} \rho(B_{v}(T) - L_{v})$$

$$_{\nu}(\Omega) \longrightarrow \overset{dz}{\longrightarrow} \overset{L_{\nu}(\Omega)}{\longrightarrow} \overset{L_{\nu}(\Omega)}{\longrightarrow} \overset{dz}{\longrightarrow} \overset{L_{\nu}(\Omega)}{\longrightarrow} \overset{L_{\nu$$

spectral radiance L_{ν} z

distance

k_v **absorption coefficient** per unit of mass $\mathbf{B}_{v}(\mathbf{T})$ black-body emission (Planck function) ρ

L

volumic mass of absorbing gaz

$$\frac{d L_{\nu}}{d \tau} = (B_{\nu}(T) - L_{\nu}) \text{ with } d \tau = k_{\nu} \rho d z \qquad \tau, \text{ optical thickness}$$

Optical thickness between z_1 and z_2 : $\tau_v(z_1, z_2) = |\int_{z_1}^{z_2} k_v(z)\rho(z) dz|$ $z = \infty$: top of atmosphere z = 0: surface

Upward LW radiation at altitude z for an atmosphere at uniform temperature T_a with a black surface at temperature T_s:

$$L_{\nu}(z) = B_{\nu}(T_{s})e^{-\tau_{\nu}(0,z)} + B_{\nu}(T_{a})(1-e^{-\tau_{\nu}(0,z)})$$
$$L_{\nu}(z) = B_{\nu}(T_{s})[1-A_{\nu}(0,z)] + B_{\nu}(T_{a})A_{\nu}(0,z)$$

transmittivitv = 1-absorptivity

LW flux at the TOA and emission height

Upward LW spectral flux at the top of the atmosphere (TOA) *for an isothermal atmosphere* at uniform temperature T_a with a black surface at temperature T_s:

$$F_{\nu}(\infty) = B_{\nu}(T_{s})[1 - A_{\nu}(0, \infty)] + B_{\nu}(T_{a})A_{\nu}(0, \infty)$$

transmittivity absorptivity

$$\mathbf{A}_{\nu}(\mathbf{0},\infty) = 1 - \mathrm{e}^{-\tau_{\nu}(\mathbf{0},\infty)}$$

For a non isothermal atmosphere:

$$F_{v}(\infty) = B_{v}(T_{s})[1 - A_{v}(0, \infty)]$$

+ $\int_{\infty}^{0} B_{v}(T) \frac{\partial A_{v}(z,\infty)}{\partial z} dz$

 $A_{\nu}(z,\infty)=1-e^{-\tau_{\nu}(z,\infty)}$

Radiation emitted by the surface toward space

Radiation emitted by the atmosphere toward space

Which we rewrite as:

$$F_{v}(\infty) = B_{v}(T_{s})[1 - A_{v}(0, \infty)] + B_{v}(T_{e})A_{v}(0, \infty)$$

with:
$$B_{v}(T_{e}) = \frac{1}{A_{v}(0, \infty)} \int_{\infty}^{0} B_{v}(T) \frac{\partial A_{v}(z, \infty)}{\partial z} dz$$
$$T_{e}: \text{ emission temperature of the atmosphere}$$

A common approximation is: $T_e \approx T(z_e)$ where $Z_e(emissionheight)$ is defined as $\tau(Z_e, \infty) = 1$

Vertical profiles of gas contribution



Vertical profiles of gas contribution



CO2 Emission height

[Lebrun, 2023]



	solar	far IR
absorption	UV: O ₂ , O ₃ Visible: no Near IR: H ₂ O (gas)	H ₂ O (gas), CO ₂ , CH ₄ , O ₃ , etc.
scattering	UV: gases (Rayleigh) [+ clouds, aerosols]	Negligible for gases [small for clouds and aerosols]

Observation from Meteosat satellite



Brightness temperature: White: warm. Black: cold