

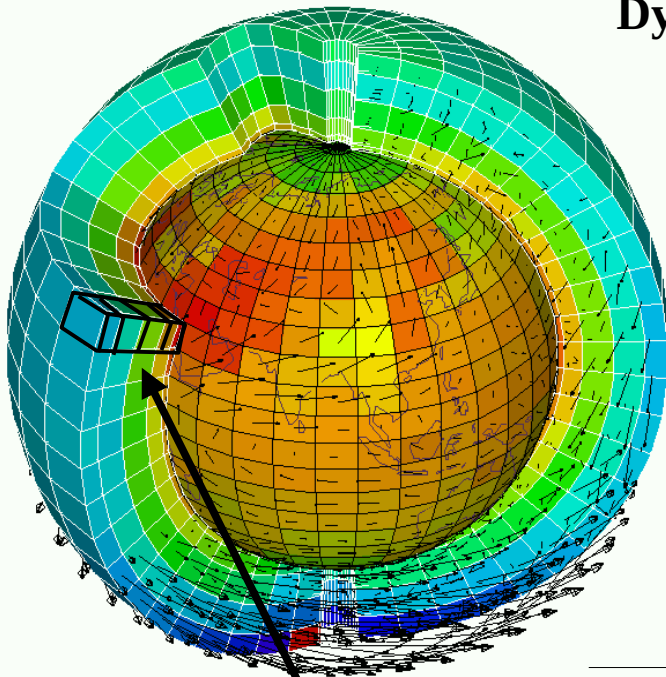
The physical parametrizations in LMDZ

LMDZ Team

Laboratoire de Météorologie Dynamique

January 2023

Dynamical core : primitive equations discretized on the sphere



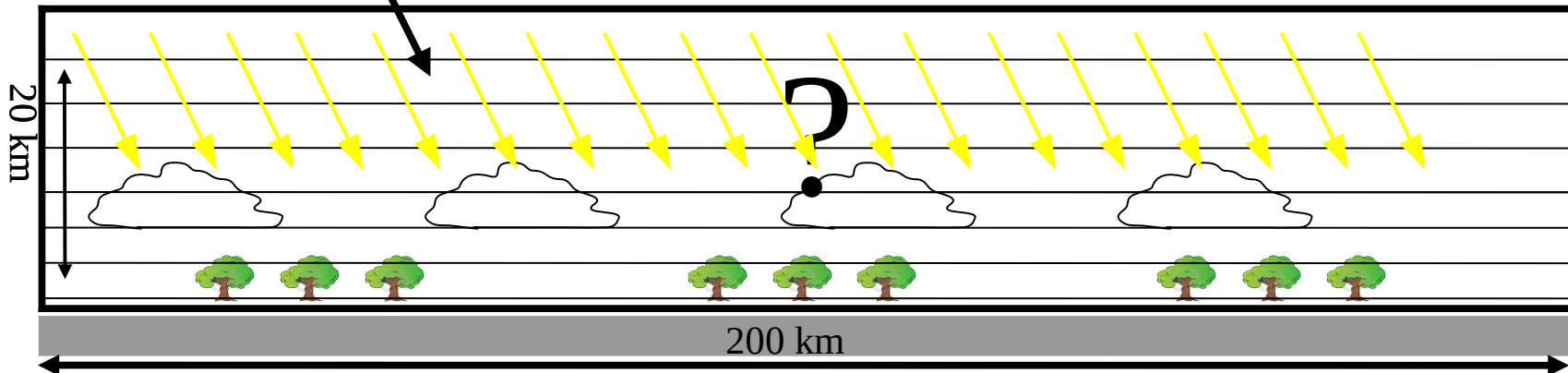
- Mass conservation

$$D\rho/Dt + \rho \operatorname{div}\underline{U} = 0$$
- Potential temperature conservation

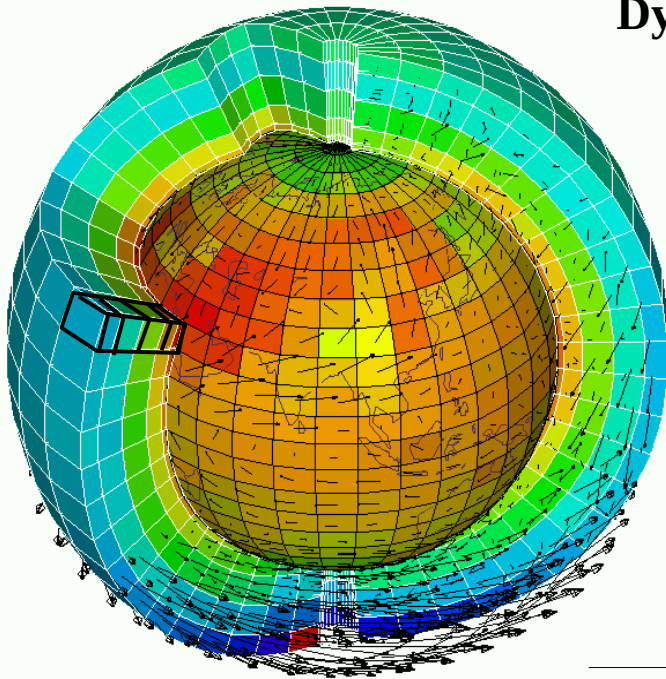
$$D\theta / Dt = Q / C_p (p_0/p)^\kappa$$
- Momentum conservation

$$D\underline{U}/Dt + (1/\rho) \operatorname{grad}p - g + 2 \underline{\Omega} \wedge \underline{U} = \underline{F}$$
- Secondary components conservation

$$Dq/Dt = Sq$$



Dynamical core : primitive equations discretized on the sphere



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- Momentum conservation
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- Secondary components conservation
 $Dq/Dt = Sq$

Parameterizations purpose : account for the effect of processes non resolved by the dynamical core

→ **Traditional « source » terms in the equations**

- Q : Heating by radiative exchanges, thermal conduction (neglected), condensation, sublimation, **subgrid-scale motions (turbulence, clouds, convection)**
- F : Molecular viscosity (neglected), **subgrid-scale motions (turbulence, clouds, convection)**
- Sq : condensation/sublimation (q = water vapor or condensed), chemical reactions, photo-dissociation (ozone, chemical species), micro physics and scavenging (pollution aerosols, dust, ...), **subgrid-scale motions (turbulence, clouds, convection)**

Tendencies

Model tendencies

The integration of a given prognostic variable X ($T, \vec{v}(u, v, w), p, \rho, q_{vap}$) can be written as :

$$X_{t+\Delta t} = X_t + \left(\frac{\partial X}{\partial t} \right)_{\text{dyn}} \Delta t \text{ (dynamical core)} \quad (1)$$

$$+ \left(\frac{\partial X}{\partial t} \right)_{\text{param}} \Delta t \text{ (parameterizations)} \quad (2)$$

From model outputs

$\text{temp}(t+\text{dtpphys})-\text{temp}(t)=\text{dtdyn}+\text{dtphy}$

$\text{ovap}(t+\text{dtpphys})-\text{ovap}(t)=\text{dqdyn}+\text{dqphy}$

$\text{vit}[u/v](t+\text{dtpphys})-\text{vit}[u/v](t)=\text{dudyn}+\text{duphy}$

Physics time-step :

$\text{dtpphys}=\text{daysec}*\text{iphysic}/(\text{day_step})$, $\text{day_sec}=86400$

Temperature tendencies

Basic facts about parametrizations I

- Each parametrization : (1) works almost independently of the others ; (2) depends on vertical profiles of u , v , w , T , q and on some interface variables with the other parametrizations ; (3) ignores the spatial heterogeneities associated with the other processes (except for some processes in the deep convection scheme).
- The total tendency due to sub-grid processes is the sum of the tendencies due to each process :

$$\begin{aligned} S_T = (\partial_t T)_\varphi = & (\partial_t T)_{eva} + (\partial_t T)_{lsc} + (\partial_t T)_{diff\ turb} + (\partial_t T)_{conv} \\ & + (\partial_t T)_{wk} + (\partial_t T)_{Th} + (\partial_t T)_{ajs} \\ & + (\partial_t T)_{rad} + (\partial_t T)_{oro} + (\partial_t T)_{dissip} \end{aligned}$$

In the model, the total tendency of T for example is $\partial_t T_{dyn} + \partial_t T_{param}$
 $= dt_{dyn} + dt_{phy}$, where :

$$\begin{aligned} dt_{phy} = & dt_{eva} + dt_{lsc} + dt_{vdf} + dt_{con} + \\ & dt_{wak} + dt_{the} + dt_{ajs} + \\ & (dt_{swr} + dt_{lwr}) + (dt_{oro} + dt_{lif}) + (dt_{dis} + dt_{ec}) \end{aligned}$$

Output names
→ **Not the same**
as their name in
the source code !
physiq_mod.f90

Specific humidity tendencies

Basic facts about parametrizations II

- Similarly, the total tendency of a given tracer q writes :

$$S_q = (\partial_t q)_\varphi = (\partial_t q)_{\text{eva}} + (\partial_t q)_{\text{lsc}} + (\partial_t q)_{\text{diff turb}} + (\partial_t q)_{\text{conv}} \\ + (\partial_t q)_{\text{wk}} + (\partial_t q)_{\text{Th}} + (\partial_t q)_{\text{ajs}}$$

In the model, the total tendency of q is therefore

$\partial_t q_{\text{dyn}} + \partial_t q_{\text{param}} = dq_{\text{dyn}} + dq_{\text{phy}}$, where :

$dq_{\text{phy}} = dq_{\text{eva}} + dq_{\text{lsc}} + dq_{\text{vdf}} + dq_{\text{con}} + dq_{\text{wak}} + dq_{\text{the}} + dq_{\text{ajs}}$

Subroutine structure

physiq_mod.F90 structure - I

Initialization (once) : *conf_phys*, *phyetat0*,
phys_output_open

Beginning *change_srf_frac*, *solarlong*

Cloud water evap. *reevap*

Vertical diffusion (turbulent mixing) *pbl_surface*

Deep convection *conflx* (Tiedtke) or *concvl* (Emanuel)

Deep convection clouds *clouds_gno*

Density currents (wakes) *calwake*

Strato-cumulus *stratocu_if*

Thermal plumes *calltherm* and *ajsec* (sec = dry)

Large scale clouds *calcratqs*

Large scale and cumulus condensation *fisrtilp*

Diagnostic clouds for Tiedtke *diagcld1*

Aerosols *readaerosol_optic*

Cloud optical parameters *newmicro* or *nuage*

Radiative processes *radlwsr*

In blue : subroutines and instructions modifying state variables

physiq_mod.F90 structure - II

Orographic processes : drag *drag_noro_strato* or
drag_noro

Orographic processes : lift *lift_noro_strato* or
lift_noro

Orographic processes : Gravity Waves *hines_gwd* or
GWD_rando

**Axial components of angular momentum and
mountain torque** : *aaam_bud*

Cosp simulator *phys_cosp*

Tracers *phytrac*

Tracers off-line *phystokenc*

Water and energy transport *transp*

Outputs

Statistics

Output of final state (for restart) *phyredem*

Subroutine structure

physiq_mod.F90 structure - I

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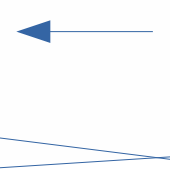
Effect of subrid-scale transport

Coupling with surface

Clouds and radiation

Today

Tomorrow



Radiation

Radiation I

Subroutine : radlsw

Tendencies :

dtswr, dtlwr Temperature tendencies due to solar radiation (SW = short wave) and thermal infra-red (LW = long wave)

The total radiative tendency is the sum of the SW and LW tendencies.

Other variables

- dtsw0 : clear sky SW tendency
- dtlw0 : clear sky LW tendency
- tops : net solar radiation at top of atmosphere (positive downward)
- topl : net infra-red radiation at top of atmosphere (positive upward)
- tops0, topl0 : same for clear sky
- sols : net solar radiation at surface (positive downward)
- soll : net infra-red radiation at surface (positive downward)
- sols0, soll0 : same for clear sky

New variables :

S[L]Wdn[up]TOA[SFC][clr] :

Short[Long]Wave

Downward[upward] radiative flux at

Top-Of-Atmosphere[Surface][clear-sky]

Cloud radiative effect (CRE) :

Old names : VAR - VAR0

New names : VAR - VARclr

ferret

xx use histhf.nc

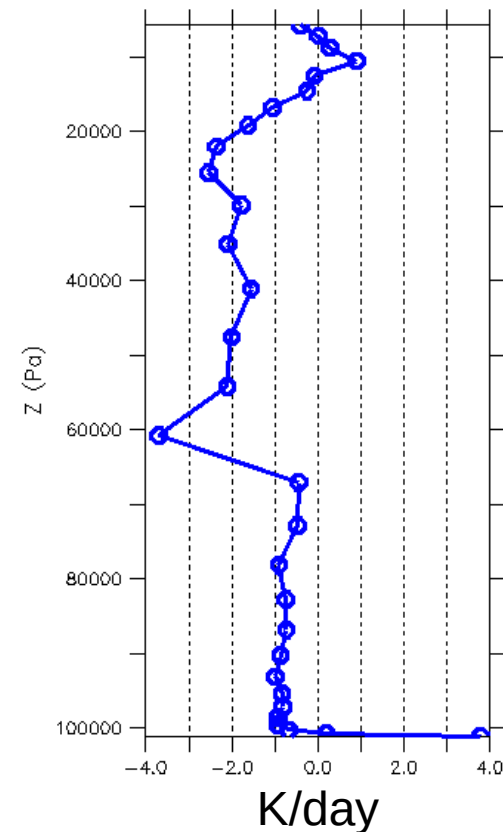
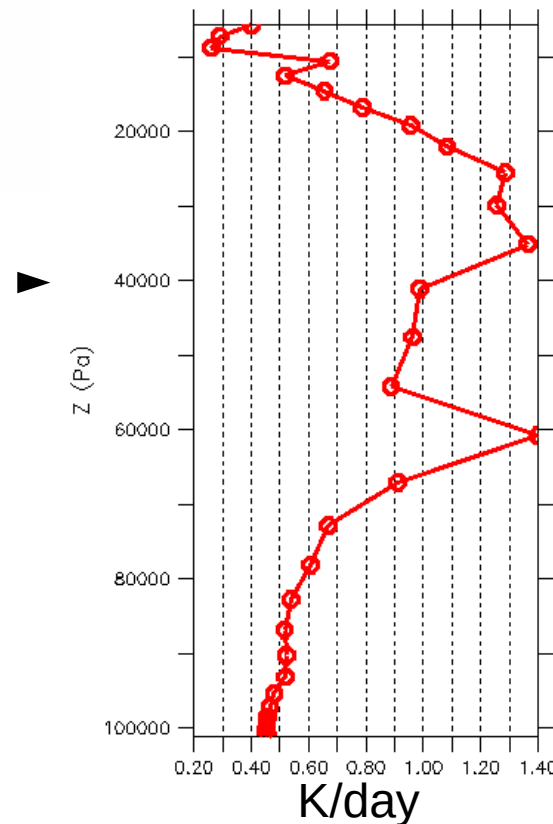
xx plot/thick=3/k=10:39 (dtswr[x=@ave,y=-30:30@ave,l=@ave])*86400

xx plot/thick=3/k=10:39 (dtlwr[x=@ave,y=-30:30@ave,l=@ave])*86400

TWPICE case

dtswr*86400

dtlwr*86400



In physiq.def (deepL translation)

```
#####  
#  
# Radiation  
#####  
#  
# activation of the new RRTM radiation code  
# 0: Old code and 1: RRTM (D=0)  
iflag_rrtm=1  
  
# Number of strips for SW. Set 2 if iflag_rrtm=0  
NSW=6
```

In config.def

```
#Radiative transfer code  
#*****  
# added this flag to activate/deactivate the radiation (MPL)  
# 0: no radiation. 1: radiation is activated (D=1).  
iflag_radia=1  
## Number of calls of radiation routines ( per day)  
nbapp_rad=24
```


Today : Parameterization of subgrid-scale motions

- Reynolds decomposition
- Turbulence
- Boundary layer convection
- Deep convection
- Subgrid-scale orography

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Based on the Reynolds decomposition between

- large-scale/resolved/explicit variables (dynamical core)
- subgrid-scale/unresolved/turbulent fluctuations (parameterizations)

Reynolds decomposition

\tilde{X} : "average" or "large scale" variable

$\bar{X} = \tilde{\rho} \mathbf{v} / \tilde{\rho}$: air mass weighted "average"

$X = \tilde{X} + X'$: X' , turbulent fluctuation

$$\begin{aligned} \Rightarrow \rho \tilde{\mathbf{v}} c &= \rho (\bar{\mathbf{v}} + \widetilde{\mathbf{v}'}) (\bar{c} + c') \\ &= \tilde{\rho} \bar{\mathbf{v}} \bar{c} + \tilde{\rho} \overline{\mathbf{v}' c'} \end{aligned}$$

$$\frac{\partial \rho c}{\partial t} + \text{div}(\rho \mathbf{v} c) = 0 \quad \Rightarrow \quad \frac{\partial \tilde{\rho} \bar{c}}{\partial t} + \text{div}(\tilde{\rho} \bar{\mathbf{v}} \bar{c}) + \text{div}(\tilde{\rho} \overline{\mathbf{v}' c'}) = 0$$

$$\frac{\partial \bar{c}}{\partial t} + \mathbf{v} \cdot \mathbf{grad} \bar{c} = -\frac{1}{\rho} \text{div}(\rho \overline{\mathbf{v}' c'}) = -\frac{1}{\rho} \frac{\partial \overline{\rho \mathbf{v}' c'}}{\partial z}$$

Today : Parameterization of subrid-scale motions

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- Turbulence
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Reynolds decomposition

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$$Dq/Dt = Sq$$

$$\frac{\partial c}{\partial t} + \mathbf{v} \cdot \mathbf{grad} c = -\frac{1}{\rho} \text{div}(\rho \overline{\mathbf{v}' c'}) = -\frac{1}{\rho} \frac{\partial \overline{\rho w' c'}}{\partial z}$$

Turbulent diffusion : Mellor et Yamada

I. Turbulent diffusion or eddy diffusion

**Boundary layer approximation (horizontal homogeneity)
+ eddy diffusion**

$$\overline{w'c'} = -K_z \frac{\partial c}{\partial z} \quad \longrightarrow \quad \frac{\partial c}{\partial t} = \frac{1}{\rho} \frac{\partial}{\partial z} \left(\rho K_z \frac{\partial c}{\partial z} \right)$$

- Analogy with molecular viscosity
(Brownian motion \leftrightarrow turbulence)
- Down-gradient fluxes.
- Turbulence acts as a "mixing"

Turbulent diffusion : Mellor et Yamada

Turbulent diffusivity K_z

- Prandtl (1925) mixing length : $K_z = l|\overline{w'}|$ or $K_z = l^2 \frac{\partial \|\mathbf{v}\|}{\partial z}$
- Accounting for static stability (Ex. Louis 1979)

$$K_z = f(Ri)l^2 \left| \frac{\partial \mathbf{v}}{\partial z} \right|, \text{ in } \quad \text{with } Ri = \frac{g}{\theta} \frac{\frac{\partial \theta}{\partial z}}{\left(\frac{\partial \mathbf{v}}{\partial z} \right)^2} \quad (1)$$

- Turbulent kinetic energy $\overline{w'^2} \simeq e = \frac{1}{2} \left[\overline{u'^2} + \overline{v'^2} + \overline{w'^2} \right]$

$$\frac{\partial e}{\partial t} = -\overline{w'u'} \frac{\partial u}{\partial z} - \overline{w'v'} \frac{\partial v}{\partial z} + \frac{g}{\theta} \overline{w'\theta'} - \frac{1}{\rho} \frac{\partial \overline{w'p'}}{\partial z} - \frac{\partial \overline{w'e}}{\partial z} - \epsilon$$

In LMDZ : Mellor and Yamada (Yamada 1983 version, see also Vignon et al. publications)

Turbulent diffusion : coupling with surface

$$\frac{\partial c}{\partial t} = -\frac{1}{\rho} \frac{\partial F_c(z)}{\partial z}$$

$$F_c(z > 0) = -K_z \rho \frac{\partial c}{\partial z}$$

At surface :

$F_c(z = 0)$: imposed or

$$F_c(z = 0) = \rho C_d ||V|| (c_s - c_1)$$

Where c_s and c_1 are values of c at the surface and in the first model layer respectively


```

#####
# Turbulent boundary layer                                     In physiq.def (deepL translation)
#####

# New version of Mellor and Yamada
new_yamada4=y

# Choice of numerical scheme for new_yamada4=y
# 1 MAR diagram. Good for stable CL but destroys the stratoculus.
# 5 MAR schema modified. Precaunise.
yamada4_num=5

# Stable boundary layer control flag
iflag_corr_sta=4

# min on the surface stability functions
f_ri_cd_min=0.01

# max of Ric for Kz. Larger decoupling for larger Ric.
yamada4_ric=0.18

# minimum mixing length for Kz
lmixmin=0

#shema of the surface layer (D:1, 1:LMD, 8:Mellor-Yamada)
iflag_pbl=12

# Thresholds for turbulent diffusion
ksta_ter=1e-07
ksta=1e-10

#ok_kzmin : Kzmin calculation in the surface CL (D: y)
ok_kzmin=n

```

Turbulent diffusion : practice

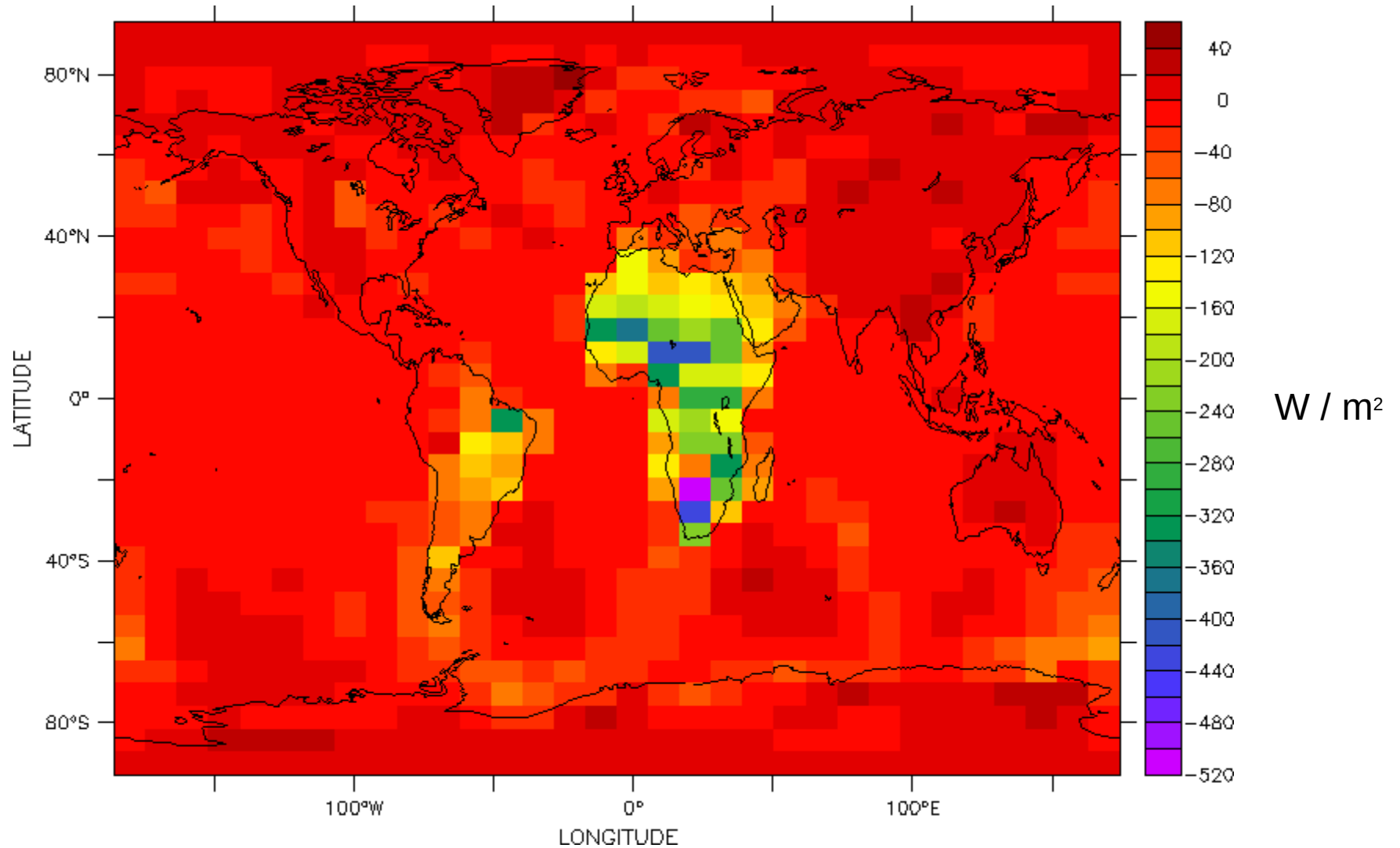
cd /LMDZ20211102.trunk/modipsl/modeles/LMDZ/BENCH32x32x39 ferret

xx use histhf.nc

xx shade/l=48 sens

xx go land 1

Sensible heat flux at 12h GMT on January 2nd



Turbulent diffusion : practice

Vertical diffusion

Subroutine : pbl_surface

Tendencies :

dtvdf, dqvdf, duvdf, dvvdf

Other variables

- sens : sensible heat flux at the surface (positive upward)
- evap : water vapour flux at the surface (positive upward)
- flat : latent heat flux at the surface (positive downward)
- tau_x, tau_y : wind stress at the surface

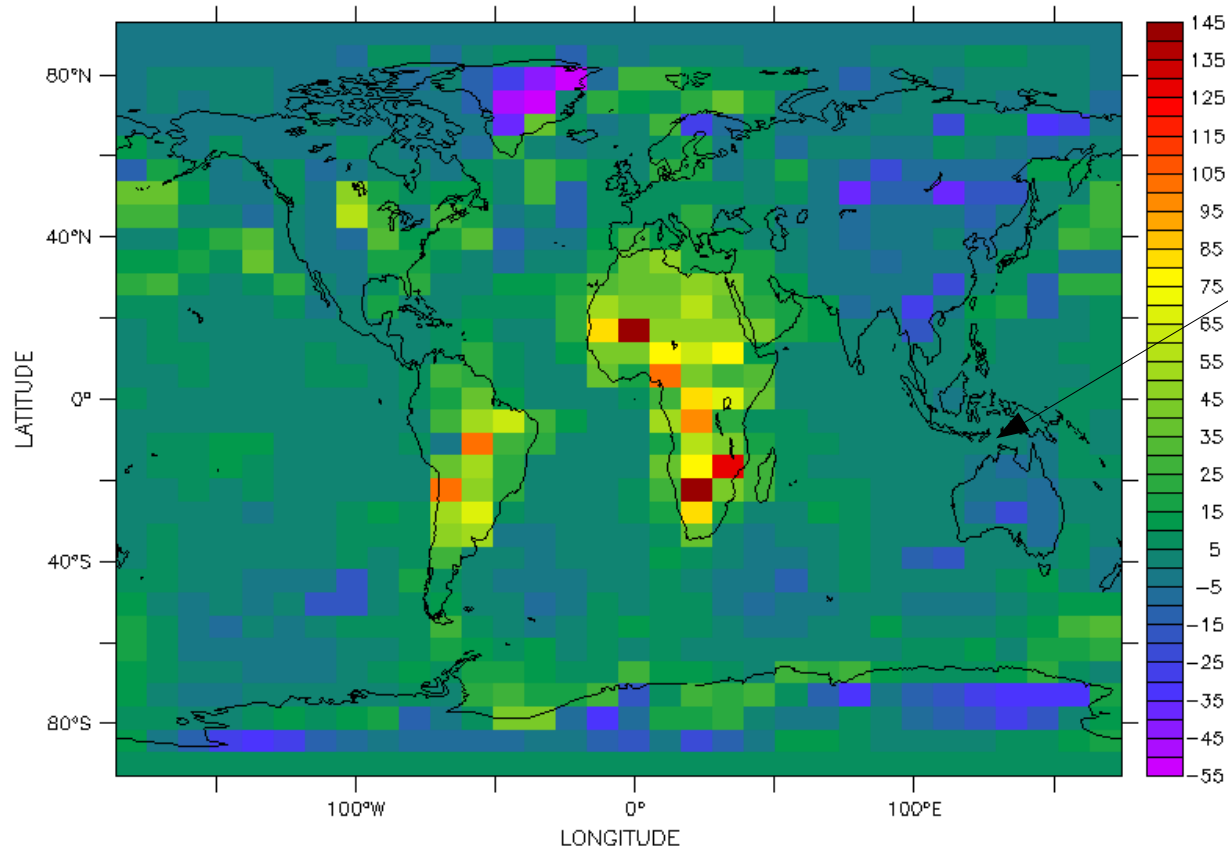
ferret

```
xx use histhf.ns
```

```
xx shade/l=48 dtvdf[k=@max]*86400
```

```
xx go land 1
```

Then choose a relevant location like for example :
x=20/y=-10



DTVDF*86400

1D case study
TWP-ICE

→ My plots in
the following

Turbulent diffusion : practice

Vertical diffusion

Subroutine : pbl_surface

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- sens : sensible heat flux at the surface (positive upward)
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ferret

xx use histhf.nc

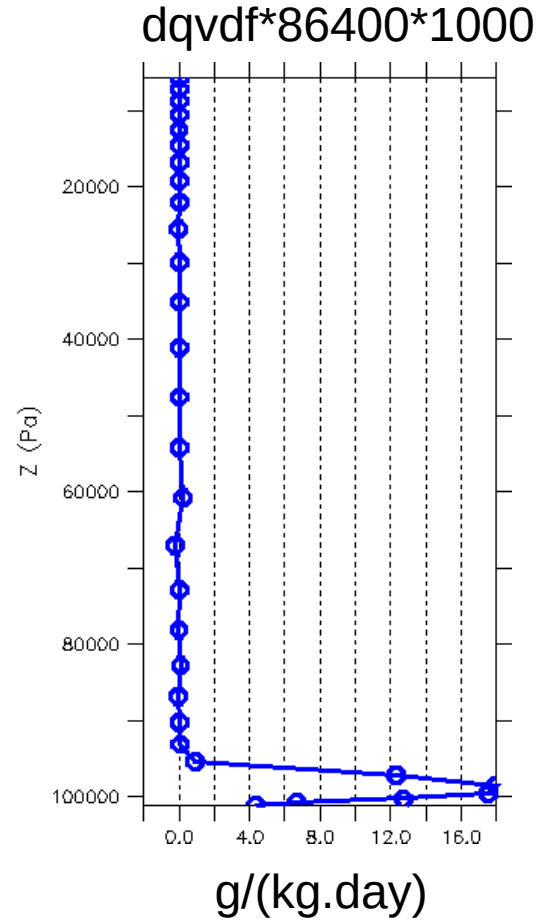
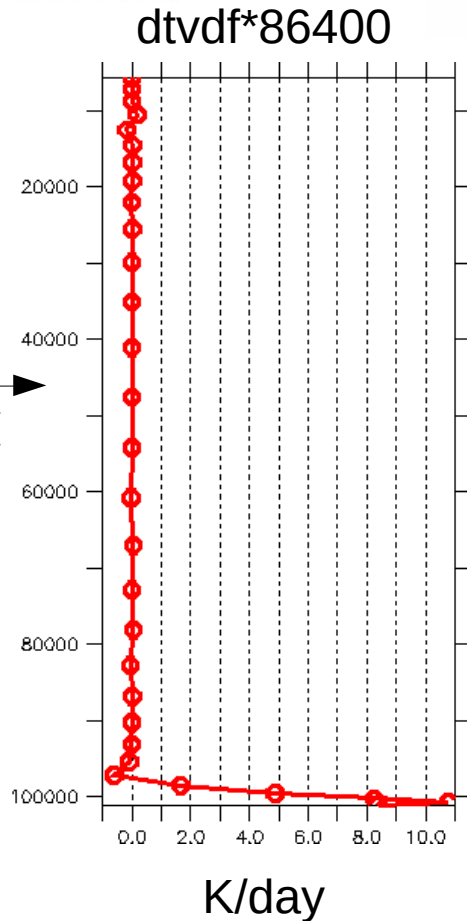
xx plot/l=48/thick=3/x=.../y=.../k=10:39

dtvdf*86400

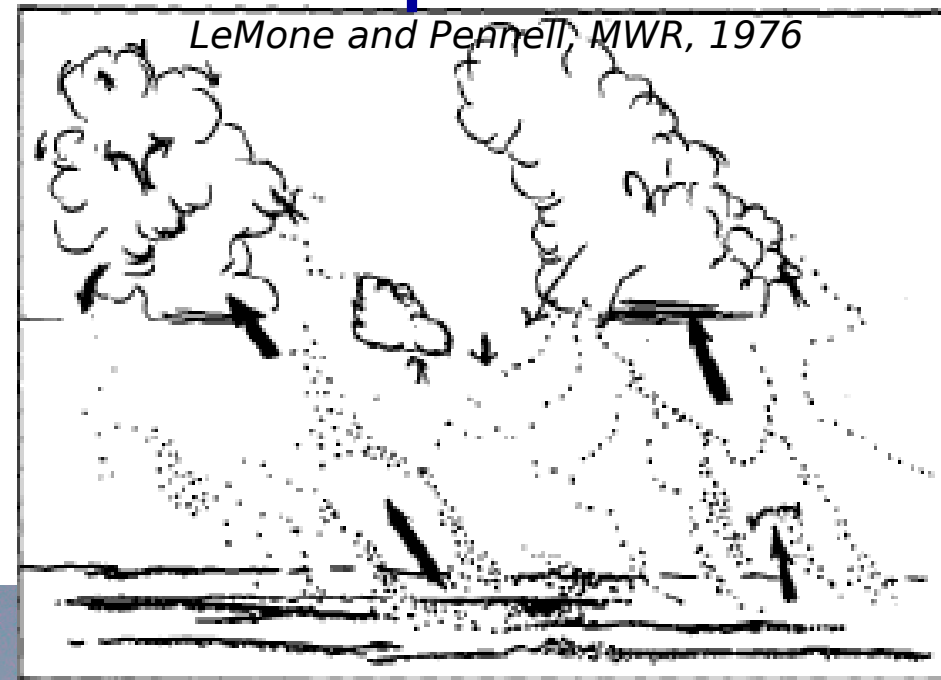
xx plot/l=48/thick=3/x=.../y=.../k=10:39

dqvdf*86400*1000

TWPICE case

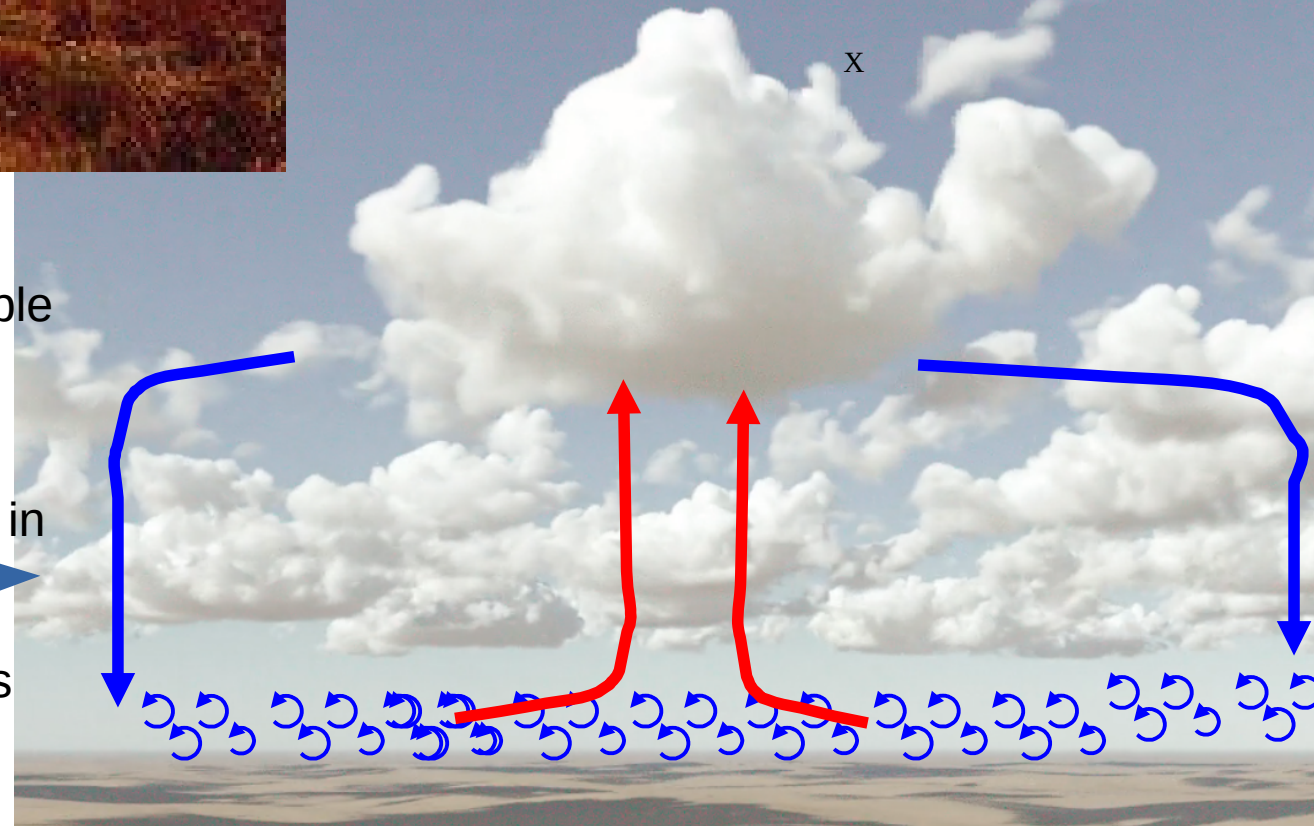


Boundary layer convection : the « thermal plume model »

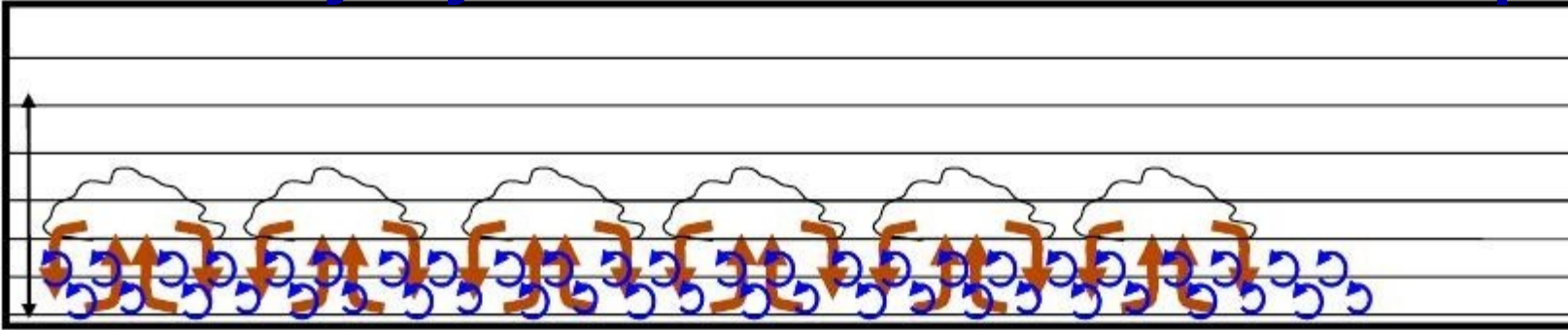


Organised turbulence/convection

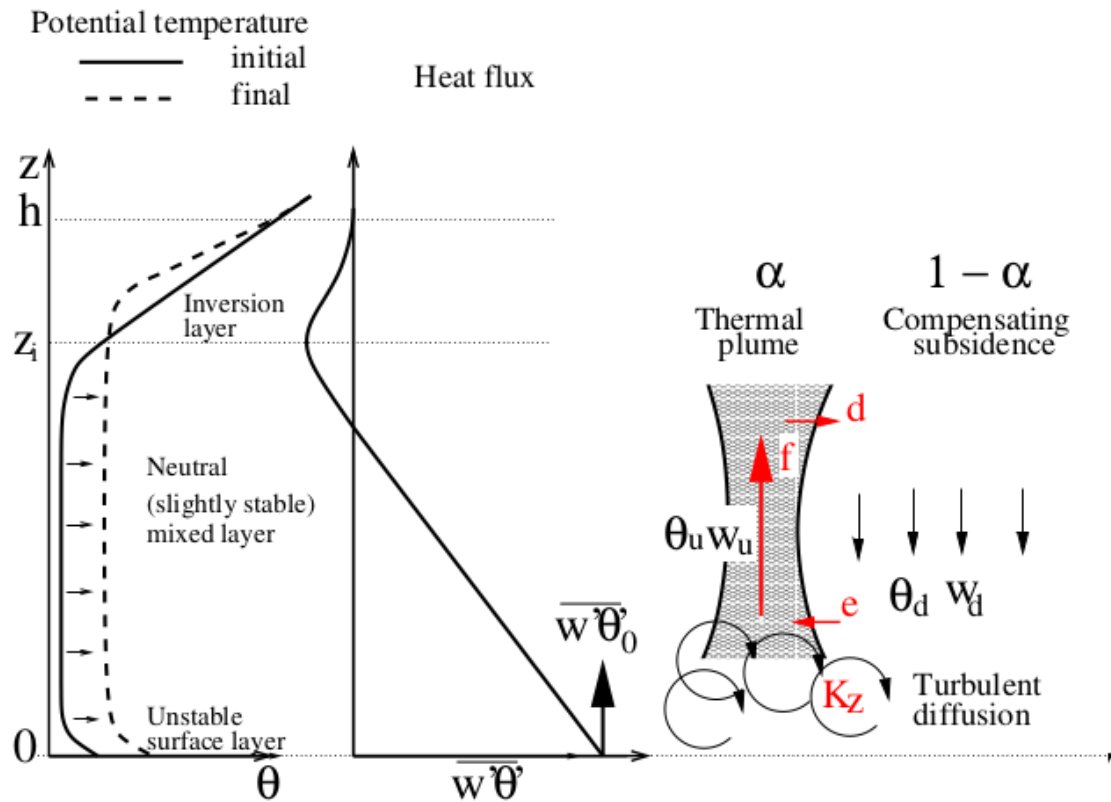
- When the boundary layer is unstable (upward > 0 sensible heat flux)
- Still in the « boundary layer »
- Above the « surface layer »
- Often dominates vertical transport in the « mixed layer »
- Often associated with cumulus
- Represented in explicit simulations (LES). Here at 8m resolution



Boundary layer convection : the « thermal plume model »



Combinaison of turbulent diffusion with a « mass flux scheme » representing a mean thermal plume or cell or roll



Separation into 2 sub-columns :

$$X = \alpha X_u + (1 - \alpha) X_d$$

ascending plume of mass flux

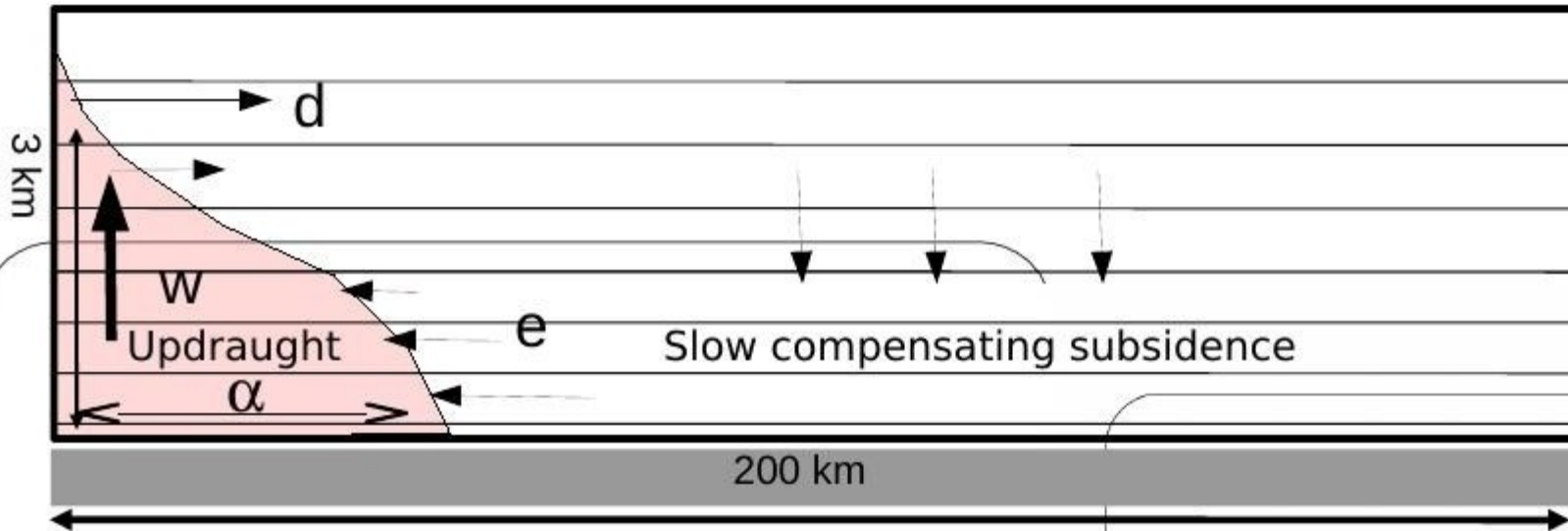
$$f = \alpha \rho w_u$$

$$\frac{\partial f}{\partial z} = e - d$$

$$\frac{\partial f c_u}{\partial z} = e c_d - d c_u$$

$$\overline{\rho w' c'} = -\rho K_z \frac{\partial c}{\partial z} + f (c_u - c_d) \quad (9)$$

Boundary layer convection : the « thermal plume model »



Internal variables of the parametrization :

- w = mean vertical velocity of ascending plumes
- α = fractionnal area covered by the updraughts
- e = lateral input rate of air into the plume (entrainment)
- d = output rate of air from the plume (detrainment)
- q_a = concentration of constituent q in the updraughts

Source term for the explicit equations :

$$S_q = -\frac{1}{\rho} \frac{\partial}{\partial z} \overline{\rho w' q'} = \frac{1}{\rho} \frac{\partial}{\partial z} \left[\rho K_z \frac{\partial q}{\partial z} \right] - \frac{1}{\rho} \frac{\partial}{\partial z} [f(q_a - q)]$$

Turbulent Diffusion

Transport by the thermal plume model

- Mass conservation

$$\frac{\partial f}{\partial z} = e - d \quad \text{where } f = \alpha \rho w$$

- Mass conservation of constituent q

$$\frac{\partial f q_a}{\partial z} = e q - d q_a$$

- Equation of movement

$$\frac{\partial f w}{\partial z} = -d w + \alpha \rho B$$

- where B is the buoyancy :

$$B = g \frac{\theta_{va} - \theta_v}{\theta_v}$$

- and the complex part lies in the expression of e and d :

$$e = f \max \left(0, \frac{\beta}{1+\beta} \left(a_1 \frac{B}{w^2} - b \right) \right)$$

$$d = \dots$$

Etc ...

```
#####  
# Convective boundary layer / thermal model      In physiq.def (deepL  
#####translation)#####
```

```
    # Dry convection (D:0, 0:dry adjustment,=>1:thermal model)  
iflag_thermals=18
```

```
    # no splitting time for thermals  
    # TURNS BUT POSES MORE PROBLEMS THAN IT SOLVES  
nsplit_thermals=1
```

```
    # tau_thermals to have a time constant on the thermals.  
    # invalid  
tau_thermals=0
```

```
    # Flag controlling training and practice  
iflag_thermals_ed=8
```

```
    # We will look for the air at  $z * (1 + \text{fact\_thermals\_ed\_dz})$  to  
compute  
    # training (A. Jam)  
fact_thermals_ed_dz=0.07
```

Boundary layer convection : practice

Thermals and dry adjustment

Subroutine : calltherm

Tendencies :

dtthe, dqthe, duthe, dvthe

Other variables

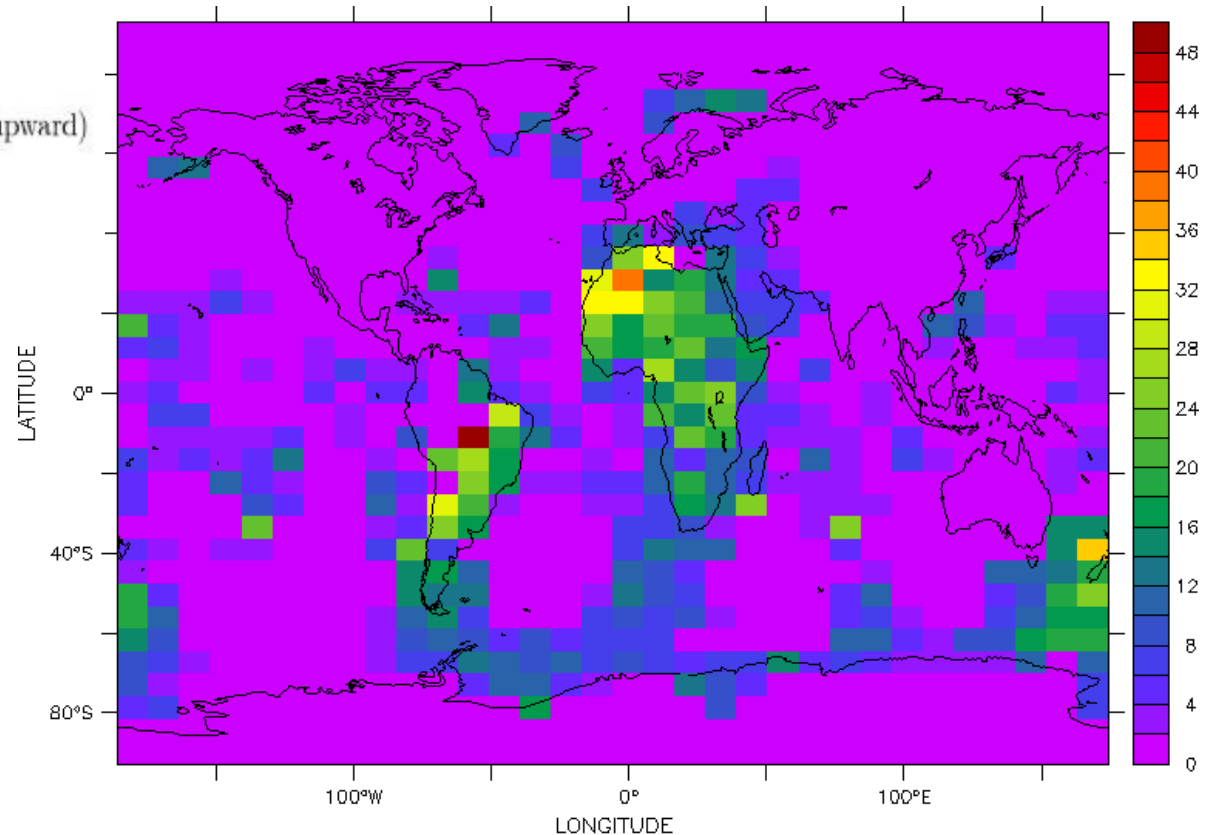
- dtajs : temperature tendency due to the sole dry adjustment
- dqajs : humidity tendency due to the sole dry adjustment
- a_th : fractional area of thermal plumes
- d_th : detrainment
- e_th : entrainment
- f_th : mass flux
- w_th : vertical velocity in the thermal plume (m/s, positive upward)
- q_th : total water content in the thermal plume
- zmax_th : altitude of the top of the thermal plume (m)
- f0_th : Thermal closure mass flux (kg/m².s)

ferret

xx use histhf.ns

xx shade/l=48 dtthe[k=@max]*86400

xx go land 1



DTTHE[K=@MAX]*86400

Boundary layer convection : practice

Thermals and dry adjustment

Subroutine : calltherm

Tendencies :

dtthe, dqthe, duthe, dvthe

Other variables

- dtajs : temperature tendency due to the sole dry adjustment
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- zmax_th : altitude of the top of the thermal plume (m)
- f0_th : Thermal closure mass flux (kg/m².s)

TWICE case

ferret

xx use histhf.nc

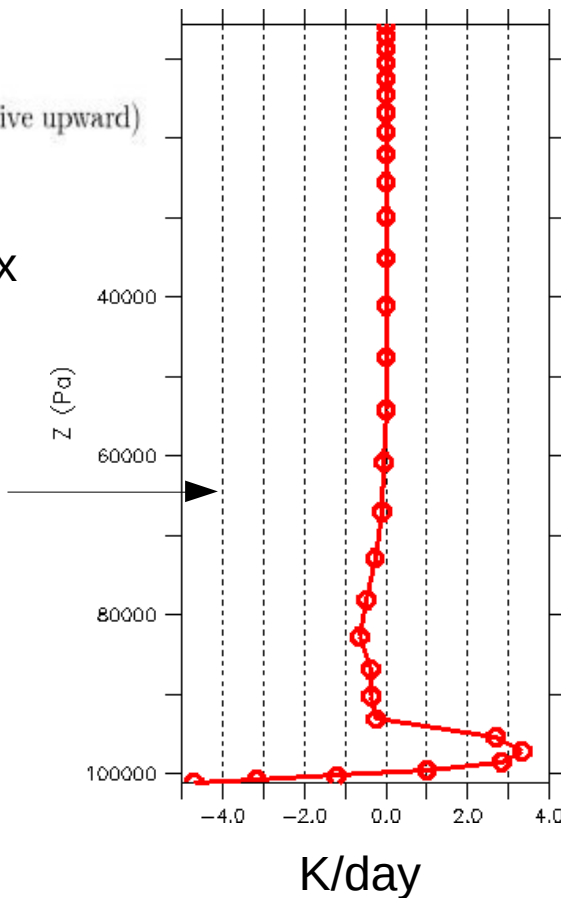
xx plot/l=48/thick=3/x=.../y=.../k=10:39

dtthe*86400

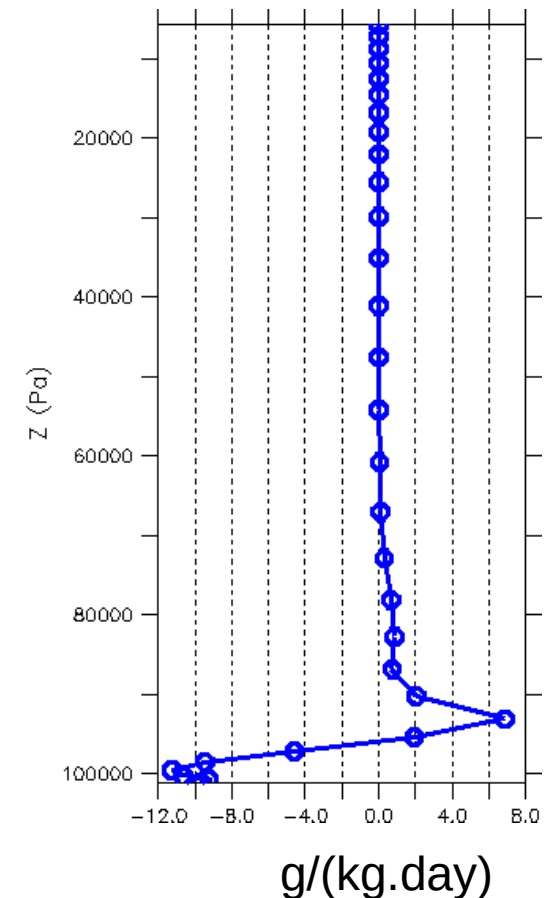
xx plot/l=48/thick=3/x=.../y=.../k=10:39

dqthe*86400*1000

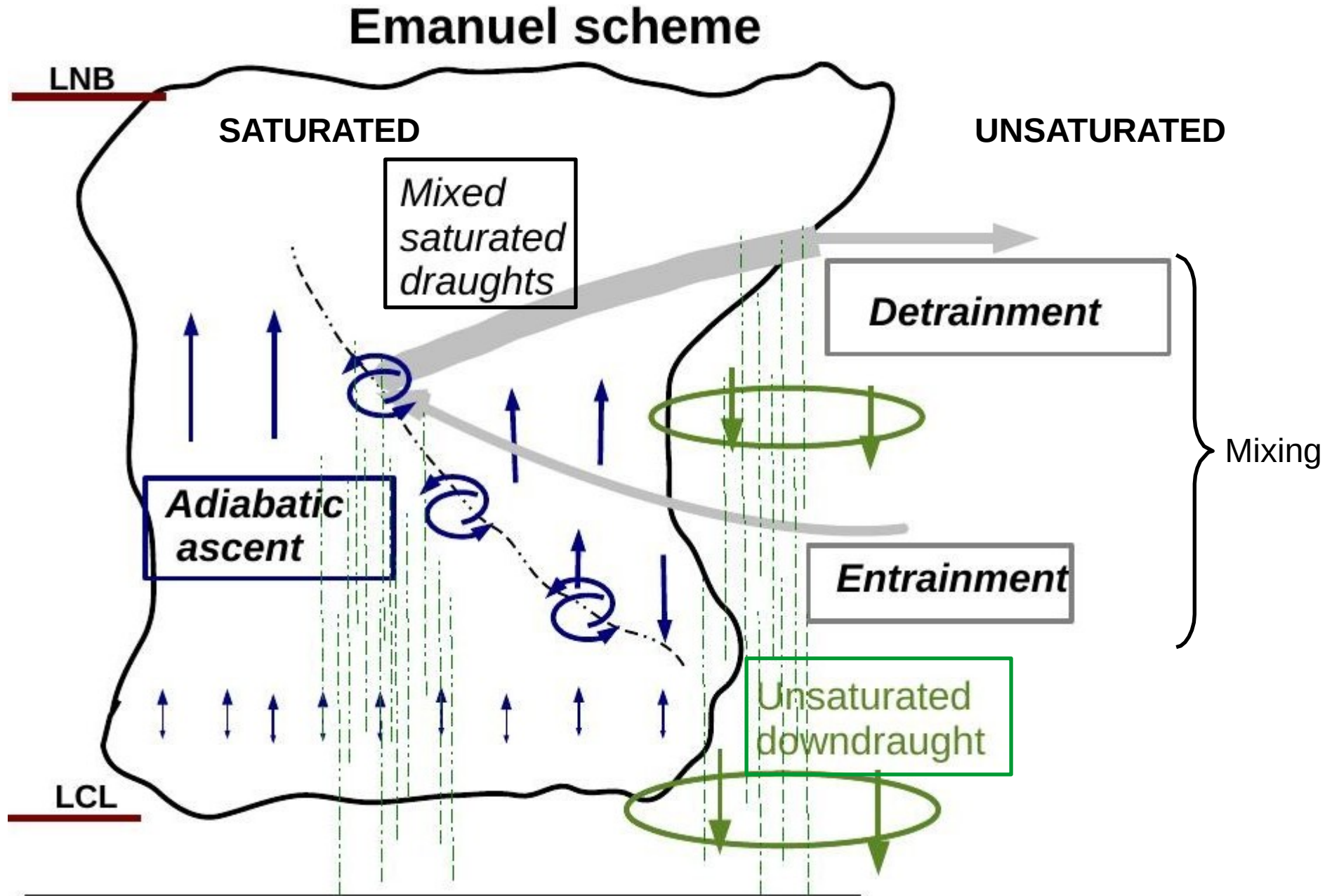
dtthe*86400



dqthe*86400*1000



Deep convection : Emanuel scheme



Deep convection : practice

Deep convection

Subroutine : concvl

Tendencies :

dtcon, dqcon, ducon, dvcon

Other variables

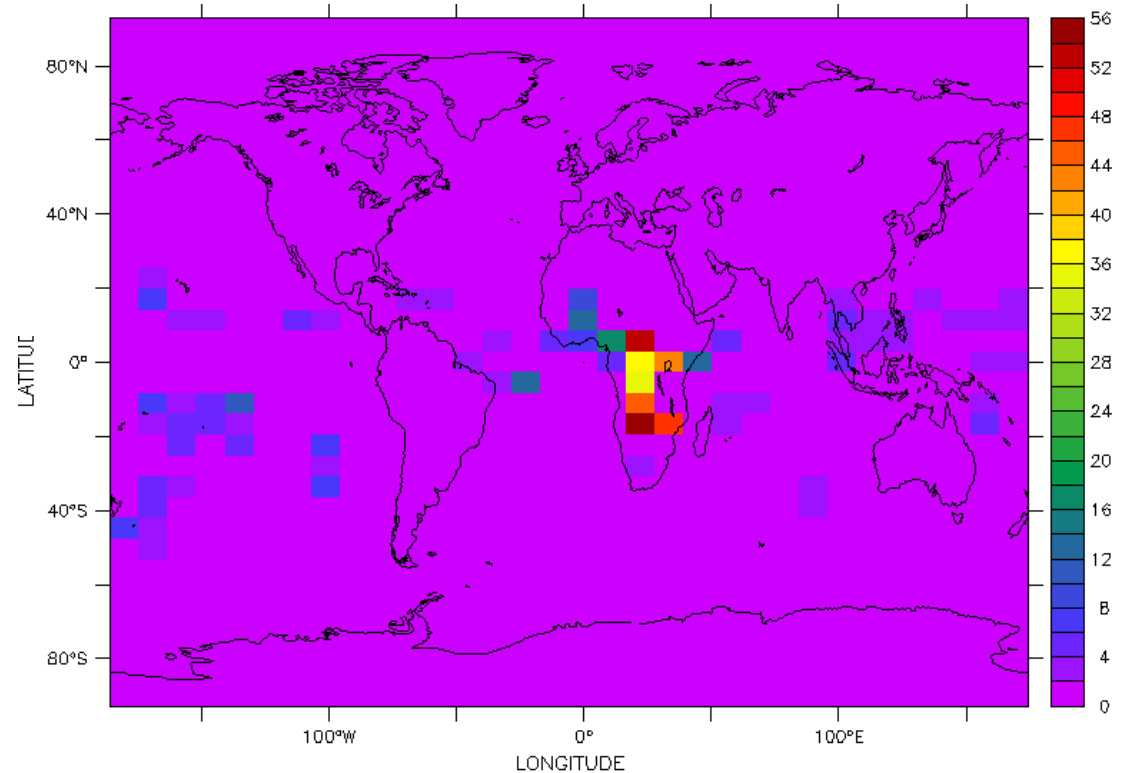
- pluc : convective precipitation at the surface
- ftd : temperature tendency due to the sole unsaturated downdraughts
- fqd : moisture tendency due to the sole unsaturated downdraughts
- clwcon : condensed water of convective clouds
("in cloud" condensed water content)
- Ma : mass flux of the adiabatic ascent
- upwd : mass flux of the saturated updraughts
- dnwd : mass flux of the saturated downdraughts
- dnwd0 : mass flux of the unsaturated downdraught (precipitating downdraught)
- pr_con_l : vertical profile of convective liquid precipitation
- pr_con_i : vertical profile of convective ice precipitation

ferret

```
xx use histf.ns
```

```
xx shade/l=48 dtcon[k=@max]*86400
```

```
xx go land 1
```



DTCON[K=@MAX]*86400

Large scale condensation & evaporation : practice

Large scale condensation (evap & lsc)

Subroutines : reevap & fisrtlp

Tendencies :

dteva, dqeva : tendencies due to cloud water evaporation

dtlsc, dqlsc : tendencies due to cloud water condensation

Total tendencies are the sums of the evaporation and condensation tendencies.

Other variables

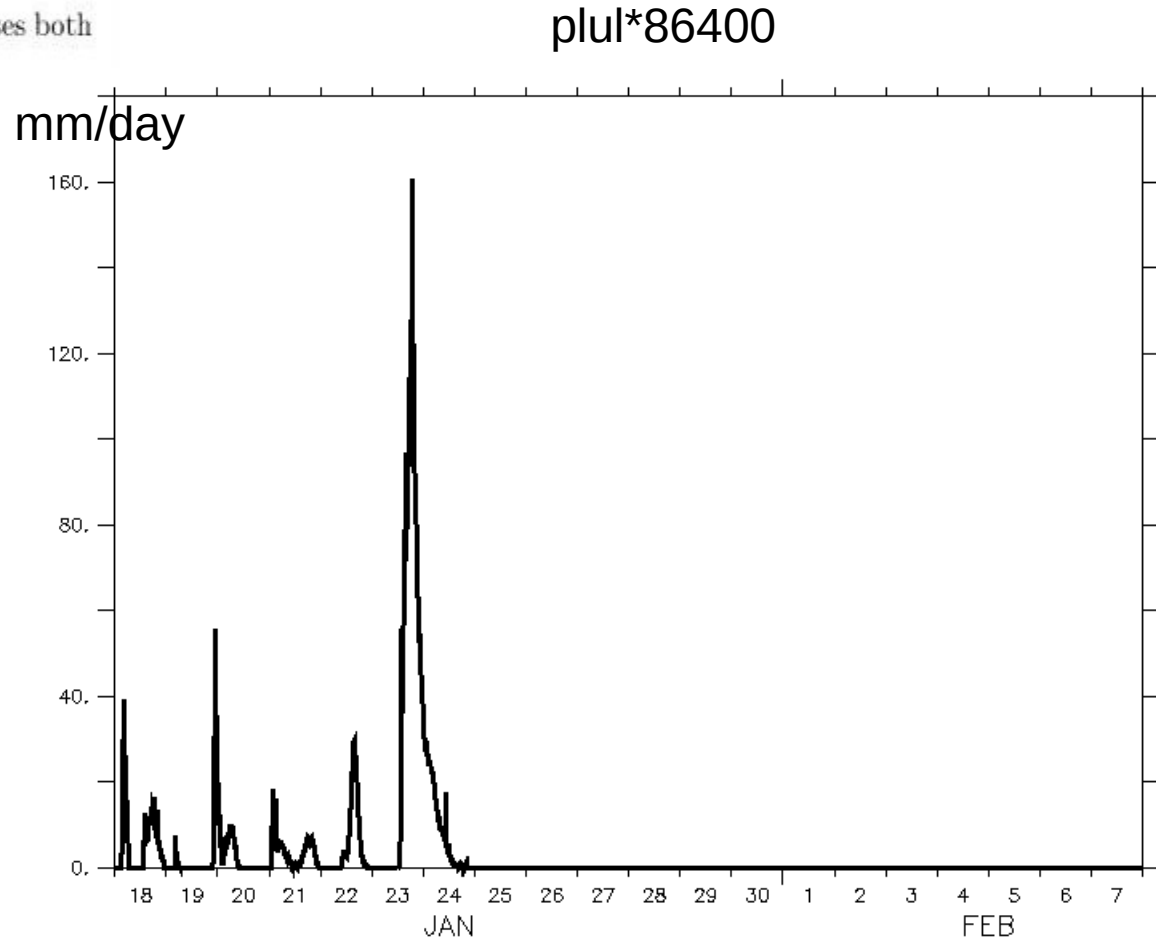
- plul : so called "large scale" or "stratiform" precipitation ; encompasses both stratiform precipitation and boundary layer cumulus precipitation.
- rneb : cloud cover
- pr_lsc_l : vertical profile of large scale liquid precipitation
- pr_lsc_i : vertical profile of large scale ice precipitation

ferret

xx use histhf.nc

xx plot/l=48/thick=3/x=.../y=... plul*86400

TWPICE case →



```
#####  
# Convection In physiq.def  
#####  
#Convection scheme switch  
# (D:2, 1:LMD, 2:Tiedtke, 3:KE New Physics, 30:KE AR4)  
iflag_con=3  
  
#output level of energy conservation diagnostics  
if_ebil=0  
  
#maximum efficiency of cld water->precipitation conversion (D: 0.993)  
epmax=0.999  
  
#Convective entrainment mixing law (D:1, 0:AR4=flat PDF, 1=PDF)  
iflag_mix=1  
  
#weights of the bell shaped and flat PDF (used only if iflag_mix=1) (D: 1 0)  
qqa1=1  
qqa2=0  
  
#reference fractional area of precipitating downdraughts,  
# def = original: 0.01  
sigdz=0.003  
  
#flag for wb (= vert velocity at LFC);  
# 0->wb=wbmax, 1->wb=f(plfc) bounded, 2->wb=f(plfc) linear, D=1  
# Si iflag_wb>=10 : wbeff_min=iflag_wb*0.1  
# wbmax : assymptotic value  
flag_wb=50  
wbmax=2.8
```

Deep convection : practice

Deep convection

Subroutine : concvl

Tendencies :

dtcon, dqcon, ducon, dvcon

Other variables

- pluc : convective precipitation at the surface
- ftd : temperature tendency due to the sole unsaturated downdraughts
- fqd : moisture tendency due to the sole unsaturated downdraughts
- clwcon : condensed water of convective clouds ("in cloud" condensed water content)
- Ma : mass flux of the adiabatic ascent
- upwd : mass flux of the saturated updraughts
- dnwd : mass flux of the saturated downdraughts
- dnwd0 : mass flux of the unsaturated downdraught (precipitation downdraught)
- pr_con_l : vertical profile of convective liquid precipitation
- pr_con_i : vertical profile of convective ice precipitation

TWPICE case →

ferret

xx use histhf.nc

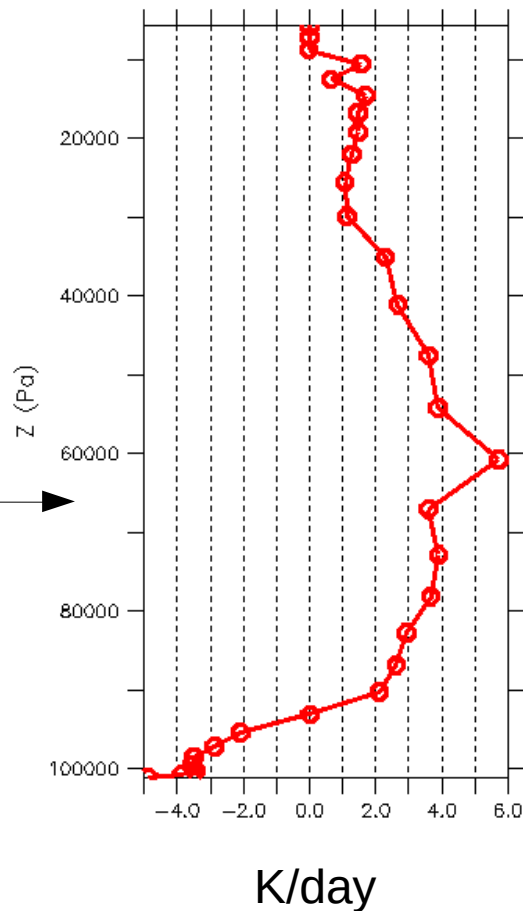
xx plot/l=48/thick=3/x=.../y=.../k=10:39

dtcon*86400

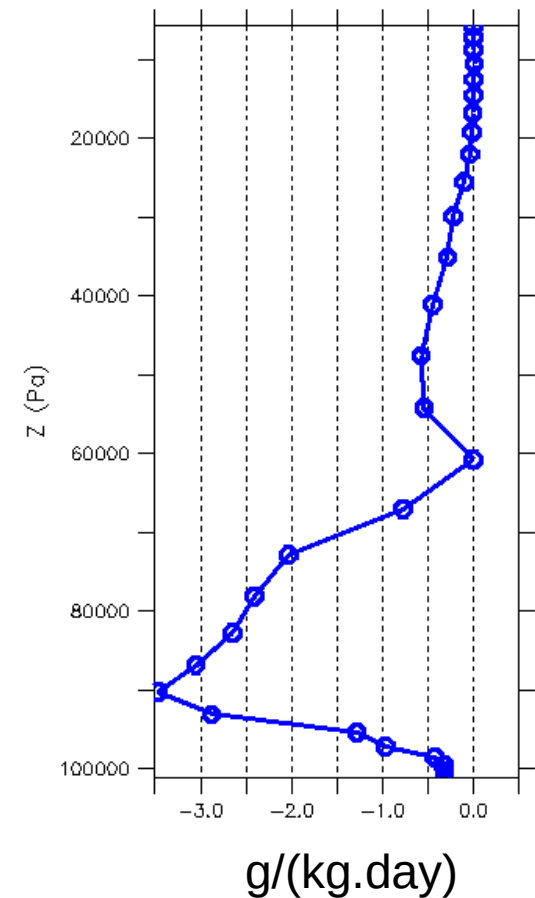
xx plot/l=48/thick=3/x=.../y=.../k=10:39

dqcon*86400*1000

dtcon*86400



dqcon*86400*1000



Deep convection : practice

Deep convection

Subroutine : concvl

Tendencies :

dtcon, dqcon, ducon, dvcon

Other variables

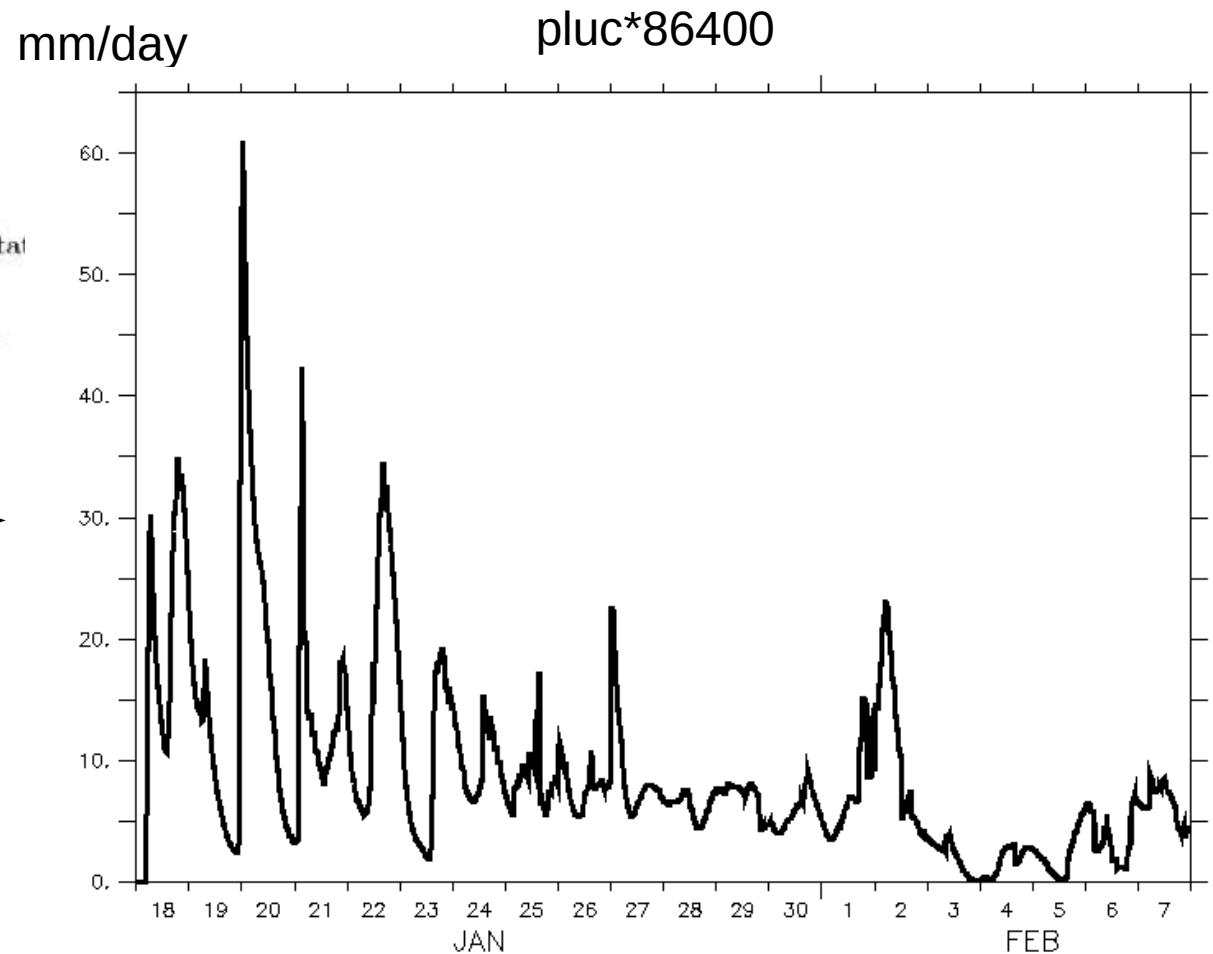
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- ftd : temperature tendency due to the sole unsaturated downdraughts
- fqd : moisture tendency due to the sole unsaturated downdraughts
- clwcon : condensed water of convective clouds ("in cloud" condensed water content)
- Ma : mass flux of the adiabatic ascent
- upwd : mass flux of the saturated updraughts
- dnwd : mass flux of the saturated downdraughts
- dnwd0 : mass flux of the unsaturated downdraught (precipitation downdraught)
- pr_con_l : vertical profile of convective liquid precipitation
- pr_con_i : vertical profile of convective ice precipitation

TWIPICE case →

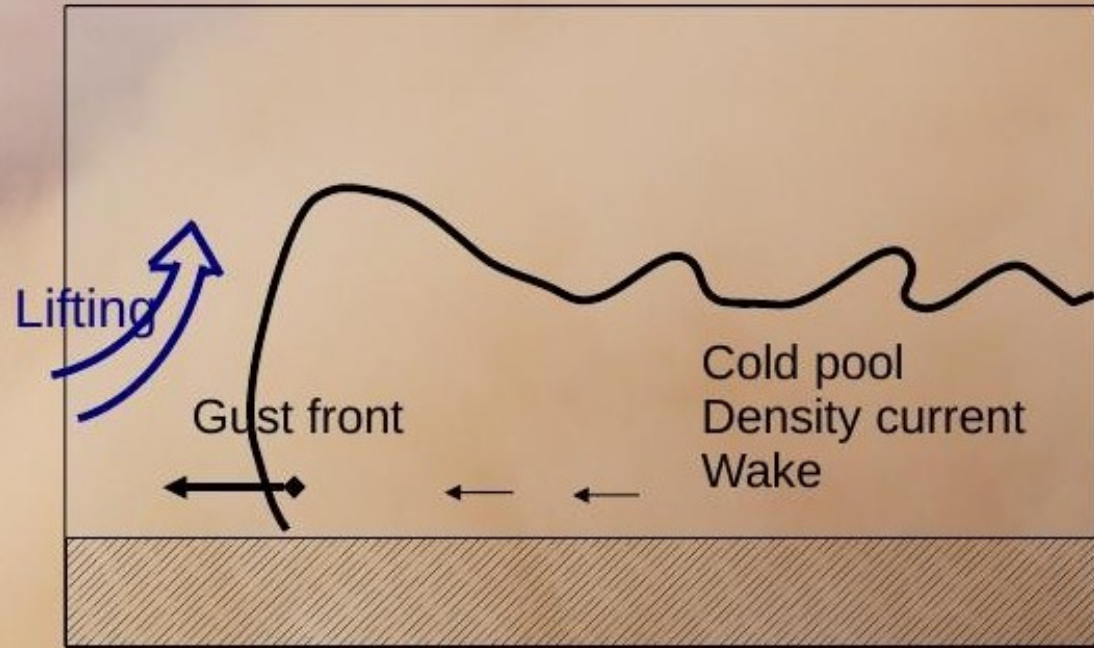
ferret

xx use histf.nc

xx plot/thick=3/x=.../y=... pluc*86400

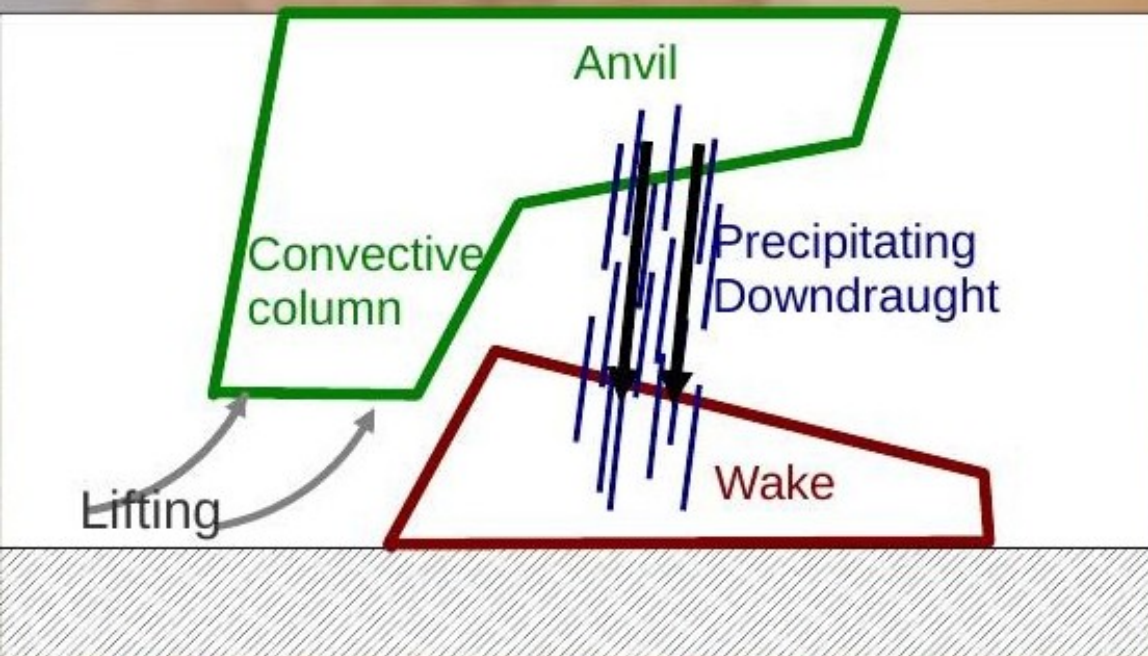


Density currents / cold pools / wakes



Created by reevaporation of convective rainfall

Trigger new convective cells by lifting air

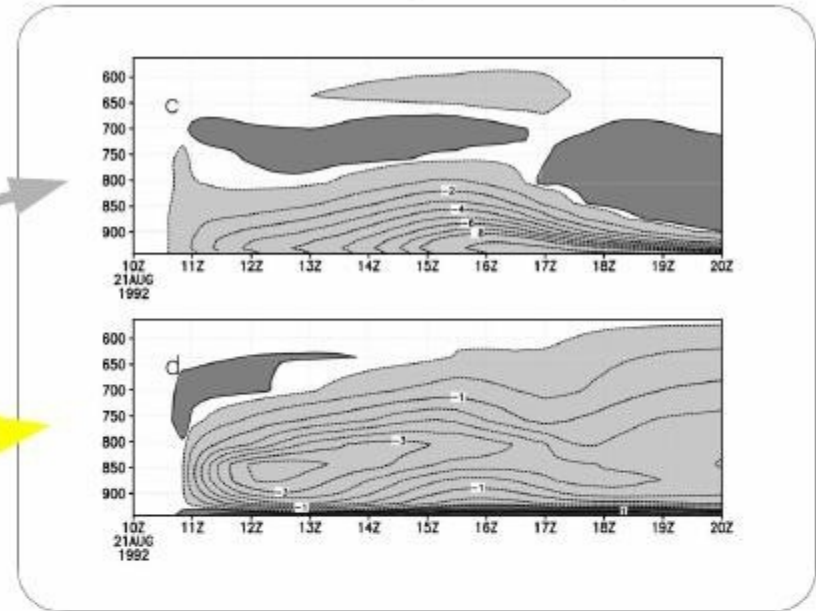


Mali, August 2004
F. Guichard, L. Kergoat

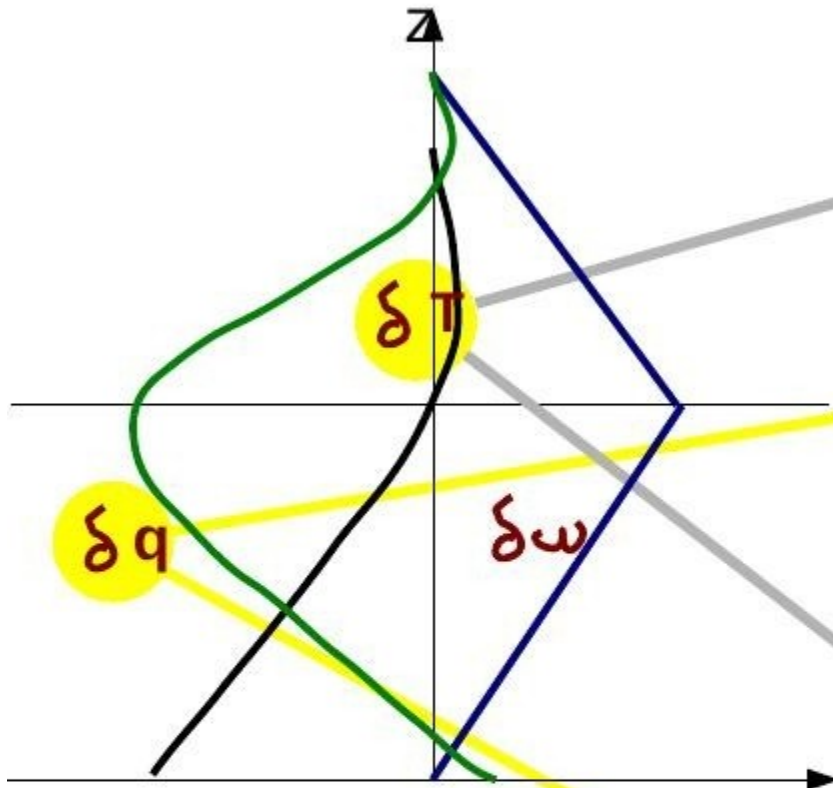
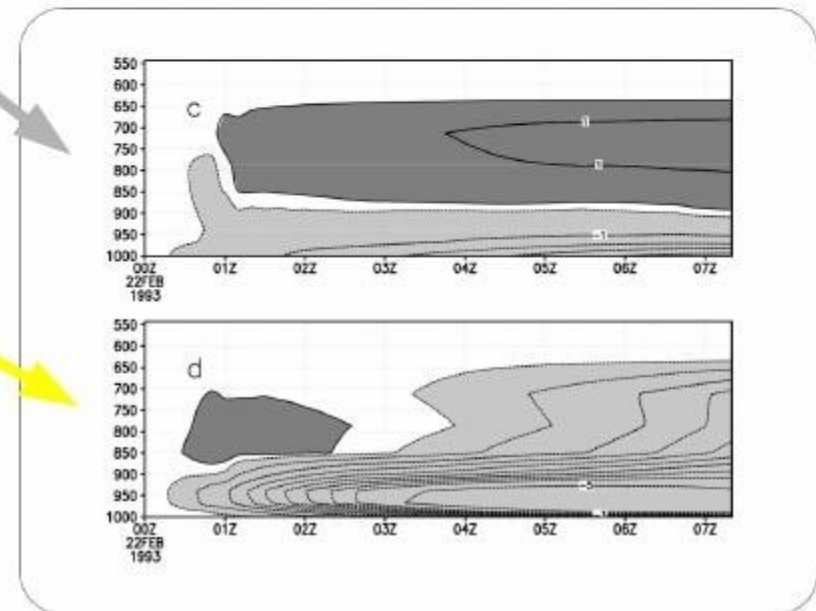
Density currents / cold pools / wakes

Simulated wake properties

HAPEX92: 21 Aug 1992 squall line case



TOGA-COARE: 22 Feb 1993 squall line case



Prognostic variables
expressed like this :

$$\Delta A = A_w - A_x$$

Density currents : practice

Cold pools (wakes)

Subroutine : calwake

Tendencies :

dtwak, dqwak

Other variables

- Alp_wk : lifting power due to cold pools
- Ale_wk : lifting energy due to cold pools
- wake_s : fractional area of cold pools
- wake_h : cold pool height
- wape : WAKE Potential Energy
- wake_deltat : vertical profile of temperature difference $T_w - T_x$
- wake_deltaq : vertical profile of humidity difference $q_w - q_x$
- wake_omg : vertical profile of vertical velocity difference $\omega_w - \omega_x$

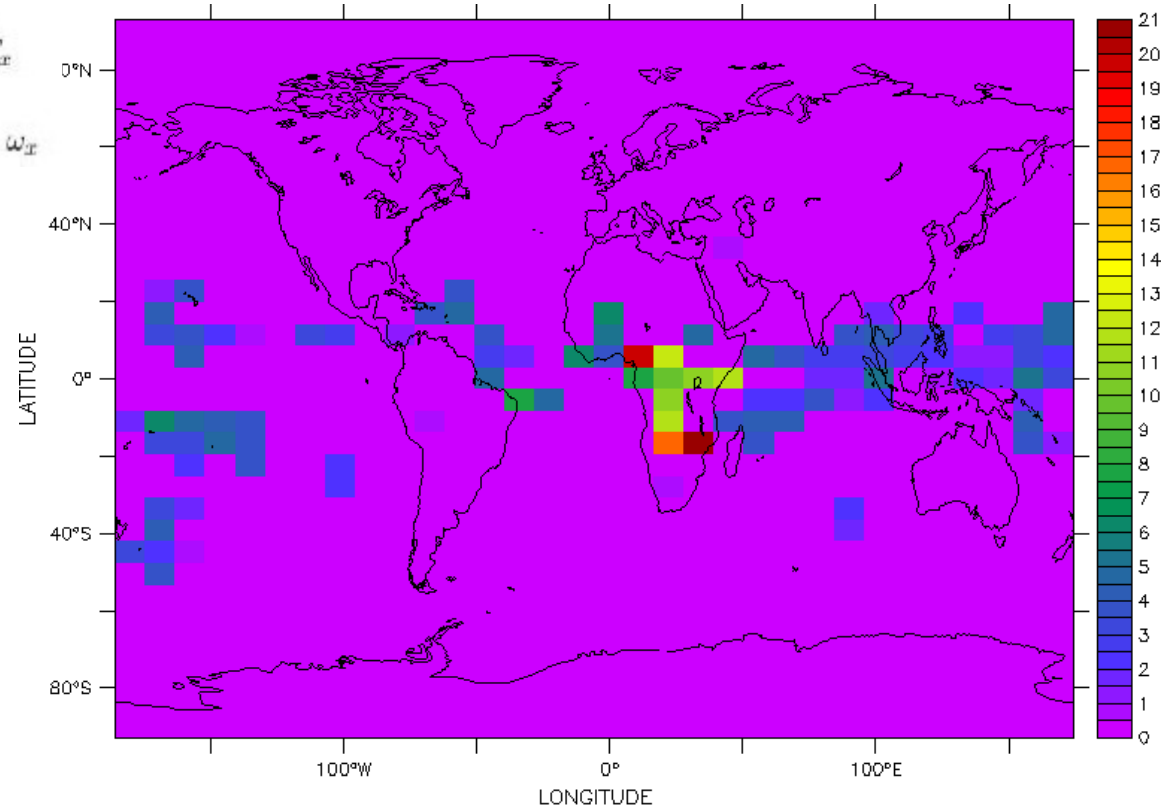
wk for « wakes »

ferret

xx use histf.ns

xx shade/l=48 dtwak[k=@max]*86400

xx go land 1



DTWAK[K=@MAX]*86400

Density currents : practice

Cold pools (wakes)

Subroutine : calwake

Tendencies :

dtwak, dqwak

Other variables

- Alp_wk : lifting power due to cold pools
- Ale_wk : lifting energy due to cold pools
- wake_s : fractional area of cold pools
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- wake_deltat : vertical profile of temperature difference $T_w - T_x$
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- wake_omg : vertical profile of vertical velocity difference $\omega_w - \omega_x$

ferret

xx use histhf.nc

xx plot/l=48/thick=3/x=.../y=.../k=10:39

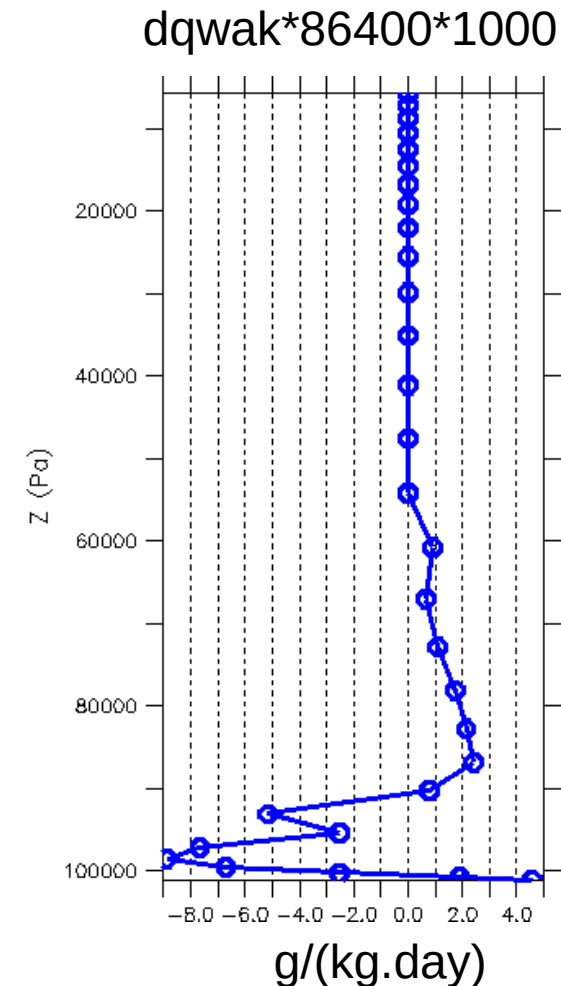
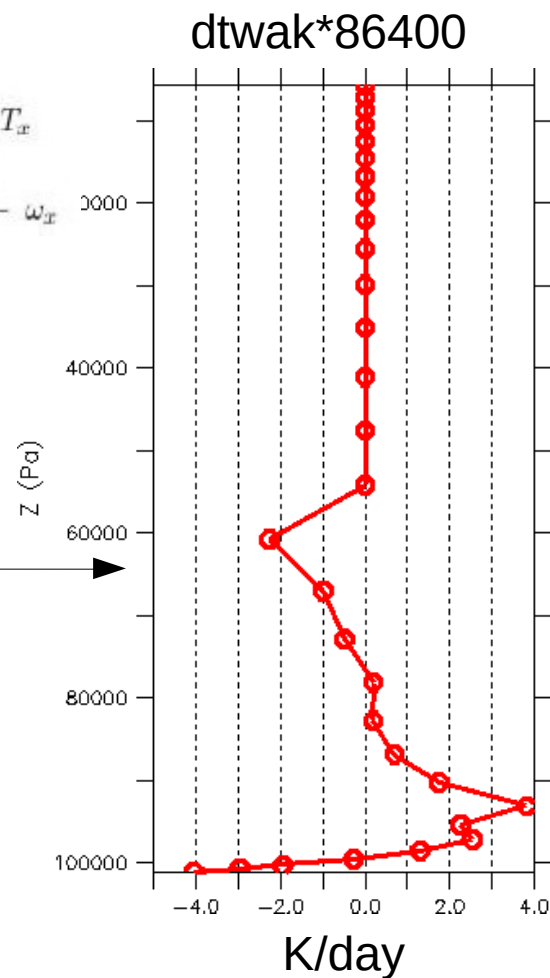
dtwak*86400

xx plot/l=48/thick=3/x=.../y=.../k=10:39

dqwak*86400*1000

wk for « wakes »

TWIPICE case



Density currents : practice

Cold pools (wakes)

Subroutine : calwake

Tendencies :

dtwak, dqwak

Other variables

- Alp_wk : lifting power due to cold pools
- Ale_wk : lifting energy due to cold pools
- wake_s : fractional area of cold pools
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- wake_deltaq : vertical profile of humidity difference $q_w - q_x$
- wake_omg : vertical profile of vertical velocity difference $\omega_w - \omega_x$

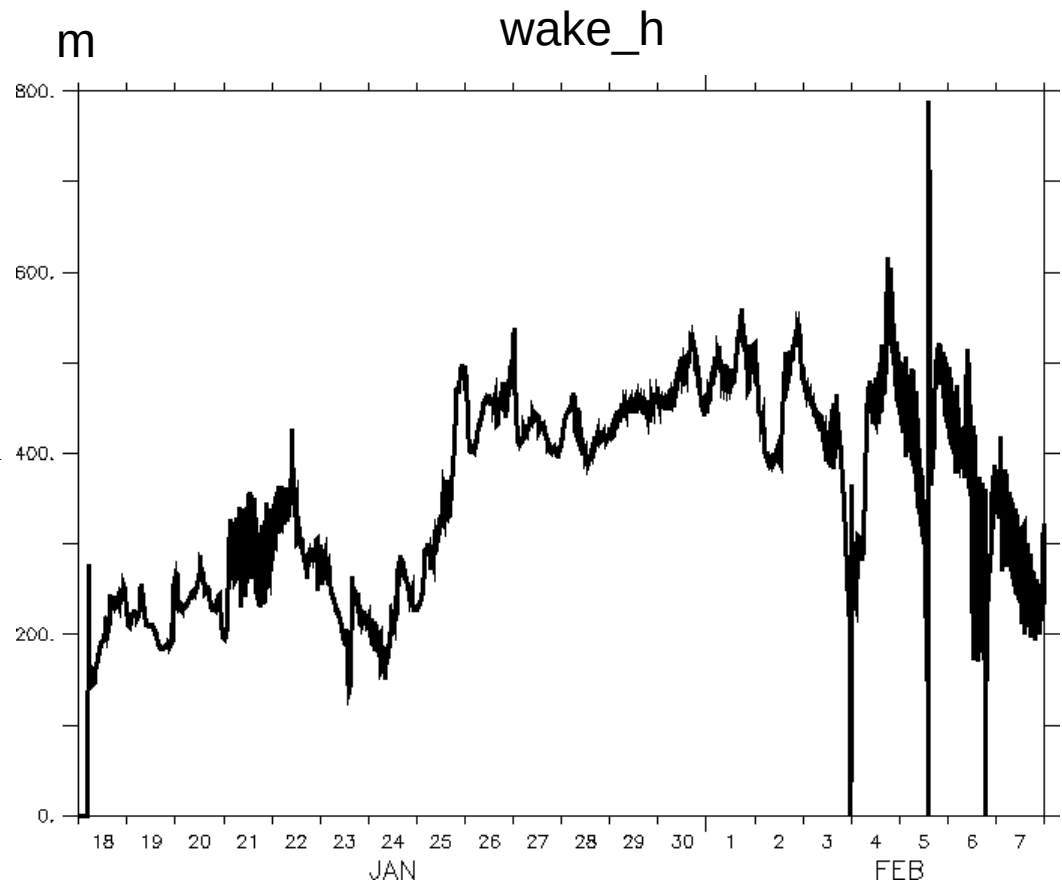
ferret

xx use histf.nc

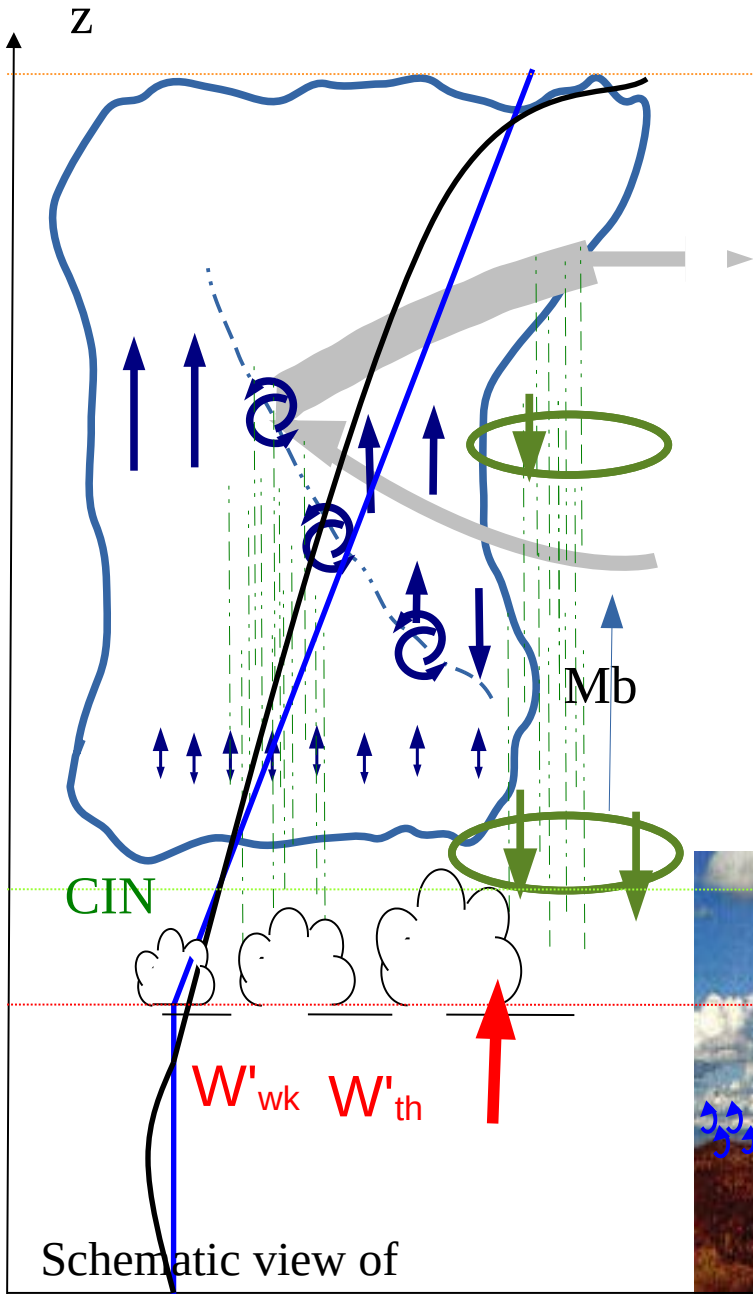
xx plot/thick=3/x=.../y=... wake_h

wk for « wakes »

TWPICE case →



What drives deep convection : triggering and closure



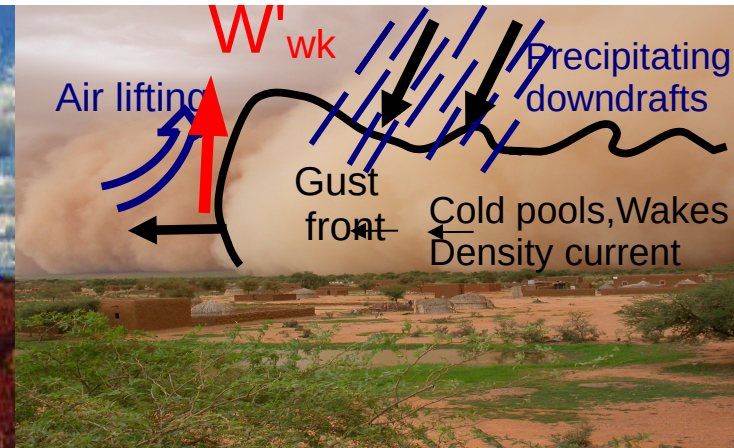
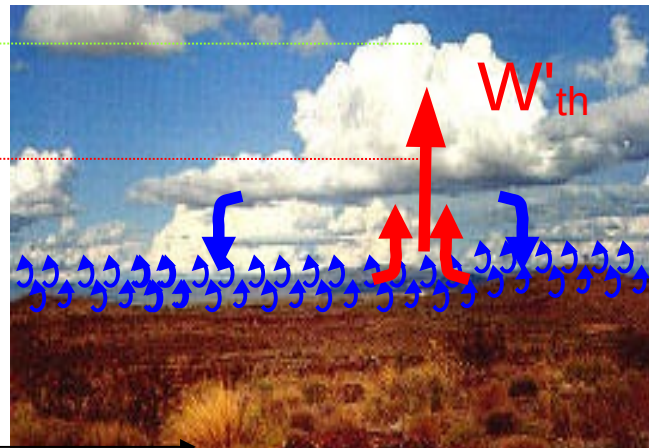
Triggering (is convection active?) and closure (with which intensity?) are based on sub cloud processes in LMDZ
 It uses estimations of subgrid scale vertical velocity provided by the Thermal plume model and the cold pool scheme
 (Catherine Rio's PhD)

Available lifting energy
ALE (J/kg) scaling with w'^2 .

→ Triggering: $\max(ALE_{th}, ALE_{wk}) > |CIN|$

Available lifting power
ALP (W/m²) scaling with w'^3 .

→ Closure : $MB = f(ALP_{th} + ALP_{wk})$



θ_v

Schematic view of Emanuel (1993) scheme Deep convection

What drives deep convection : triggering and closure

Deep convection

Subroutine : conevl

Tendencies :

dteon, dqcon, ducon, dvcon

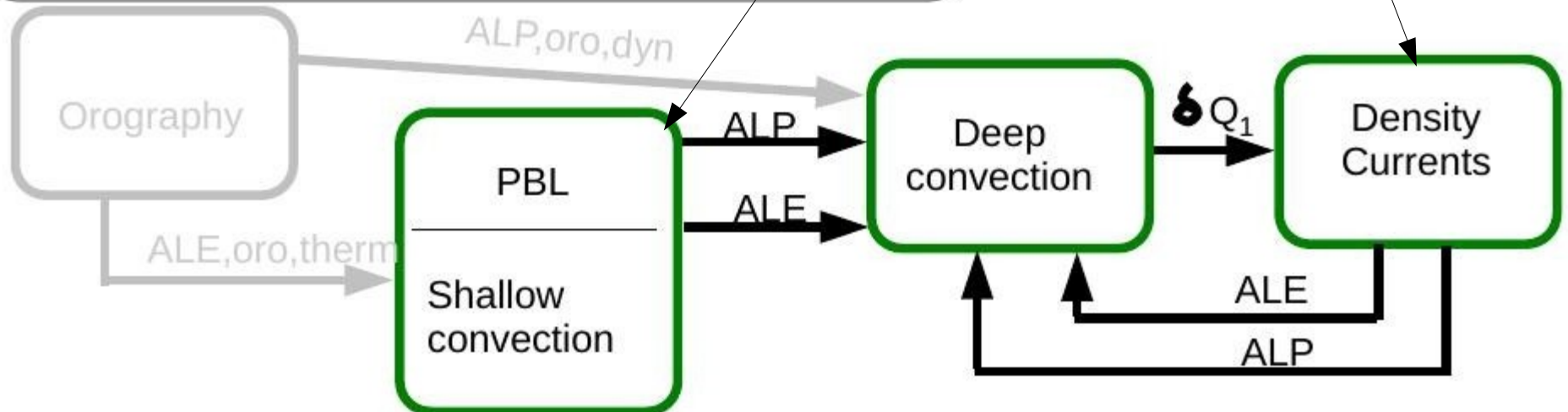
Other variables

- pluc : convective precipitation at the surface
- ftd : temperature tendency due to the sole unsaturated downdraughts
- fqd : moisture tendency due to the sole unsaturated downdraughts
- clwcon : condensed water of convective clouds ("in cloud" condensed water content)
- Ma : mass flux of the adiabatic ascent
- upwd : mass flux of the saturated updraughts
- dnwd : mass flux of the saturated downdraughts
- dnwd0 : mass flux of the unsaturated downdraught (precipitating downdraught)
- pr_con_l : vertical profile of convective liquid precipitation
- pr_con_i : vertical profile of convective ice precipitation

The deep convection scheme is then coupled to 2 PBL processes :

1. Thermals

2. Density currents (or wakes or cold pools)



In physiq.def (deepL translation)

```
#####
```

```
# Flags wakes
```

```
#####
```

```
#Wake scheme switch (D:0, 0:AR4, 1:New Physics)
```

```
iflag_wake=1
```

```
#multiplicative factor of the damping by gravity waves, def: 4.
```

```
coefgw=4
```

```
#wake density = number of wake centers per m2, def: 8.E-12
```

```
#wdens_ref=8.E-12
```

```
wdens_ref_o=1e-09
```

```
wdens_ref_l=8e-12
```

```
# Ajustement convectif prealable au calcul des poches
```

```
ok_adjwk=y
```

```
# Prevent some crashes
```

```
# Filter out bad wakes
```

```
flag_wk_check_trgl=n
```

```
iflag_wk_check_trgl=2
```

```
iflag_alp_wk_cond=1
```

Energy budgets

Radiation II : Energy budget

Energy budget at the top of the atmosphere :

$$\text{nettop} = \text{tops-topl} = (\text{SWdn-SWup}) - (\text{LWup-LWdn})$$

Energy input (received solar energy minus reflected solar and emitted LW energy)

Positive in the tropics, negative at the poles

Surface energy budget (from the atmosphere to the surface) :

$$\text{bils} = \text{soll} + \text{sols} + \text{sens} + \text{flat}$$

$$\text{soll} = \text{ldnsfc-lwpsfc} \text{ (same for sols)}$$

flat : latent heat flux (from the atmosphere to the surface)

Negative when there is surface evaporation

sens : sensible heat flux (from the atmosphere to the surface)

Positive when the atmosphere heats the surface (polar regions)

Negative when the atmosphere is heated by the surface (continents & oceans)

Try to do it !

PARTIE RAYONNEMENT NUAGES → JB

Large scale condensation & evaporation

Représentation des nuages

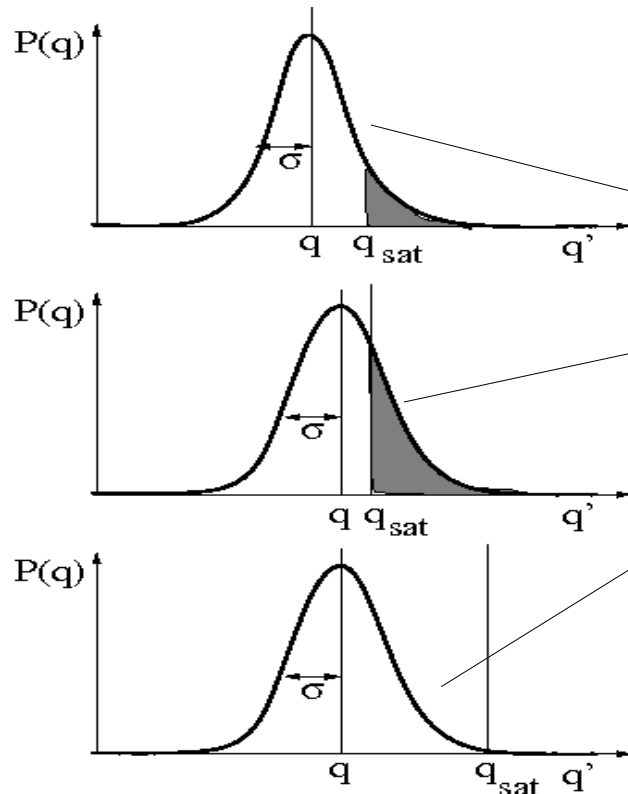
q : concentration en vapeur d'eau
 q_{sat} : concentration maximum à saturation

Si $q > q_{sat}$:

→ la vapeur d'eau condense = nuage

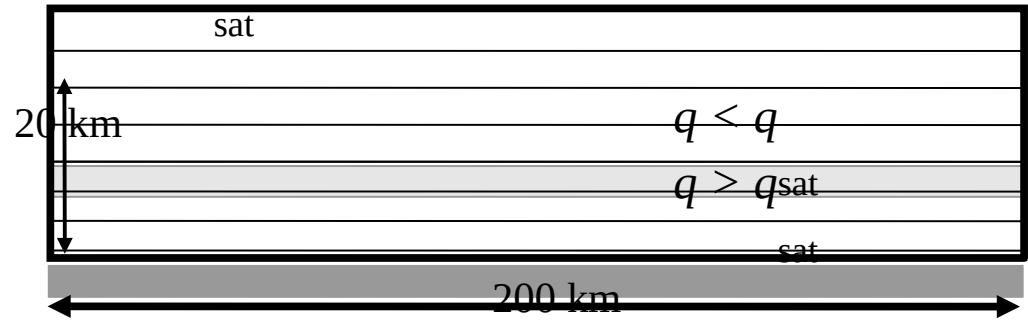
On connaît q et q_{sat} à l'échelle de la maille

→ Fraction de la maille couverte de nuages ?



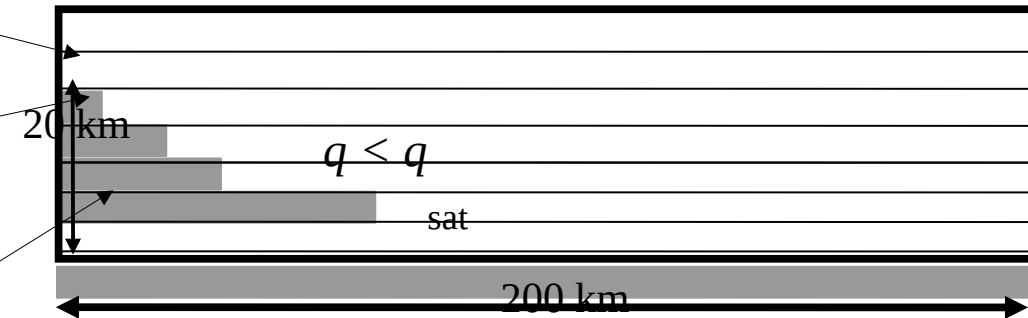
Modèle « tout ou rien » :

Si $q > q_{sat}$ maille nuageuse, sinon ciel clair.



Modèle « statistique » :

On suppose une distribution statistique de q' dans la maille autour de q



Intervient dans Q

→ condensation

→ prise en compte des nuages dans le code radiatifs

Paramétrisation simple : gaussienne $\sigma / q = 20\%$

2. Couche limite convective

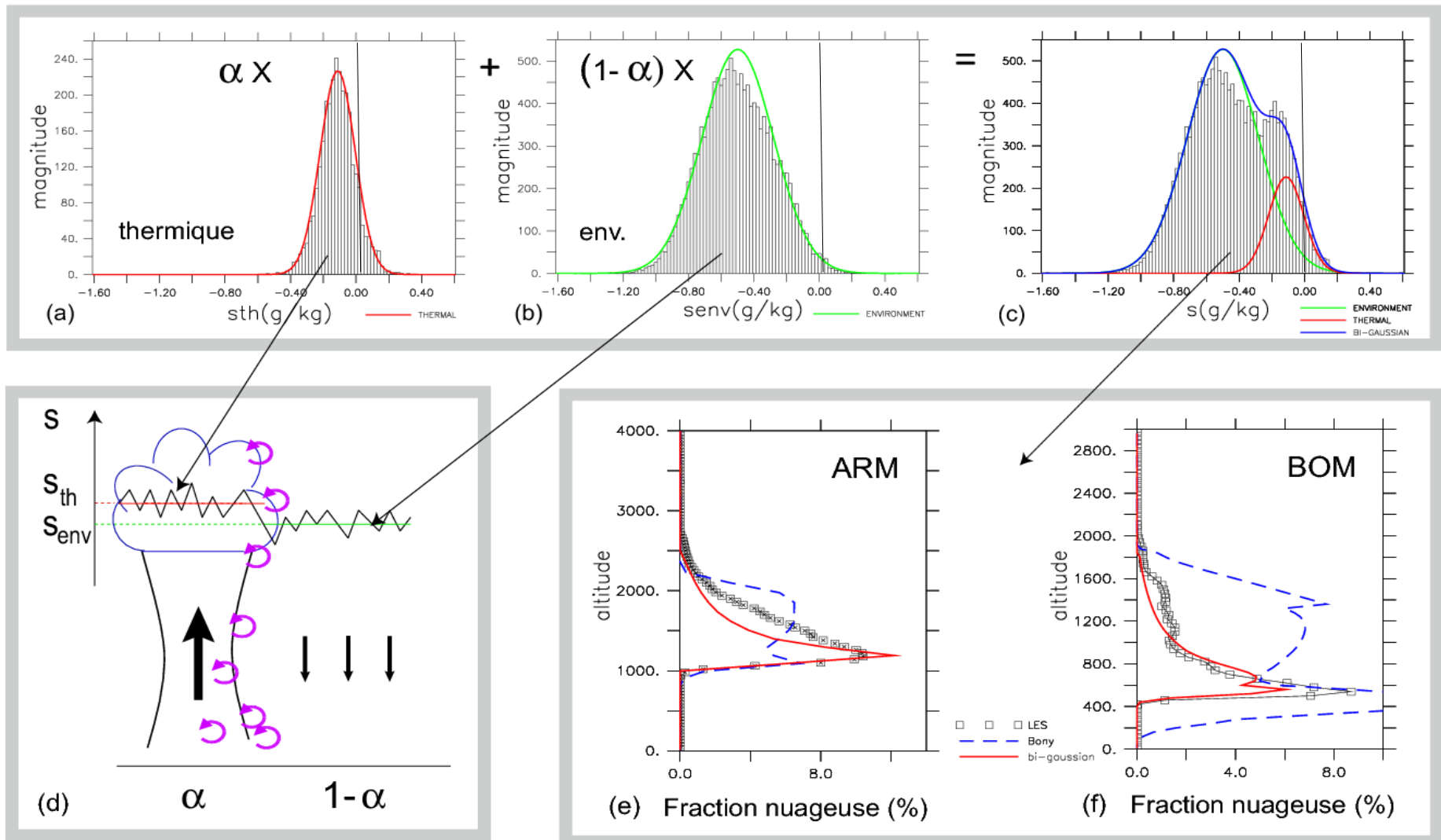
Large scale condensation & evaporation

Nouvelle paramétrisation de nuages couplée aux thermiques :

Utilisation d'une PDF bi-gaussienne pour la distribution d'eau totale sous nuageuse

Une gaussienne pour les panaches thermiques et une pour l'environnement

Comparaison des distributions prédites par ce schéma avec les distributions des LES



Cloud parameters

**In physiq.def (deepL
translation)**
#####

```
#precipitation thresholds for stratum clouds (D: 2.6e-4 2.6e-4)
cld_lc_lsc=0.00065
cld_lc_con=0.00065

#time constant to remove water lsc and convective water
# (D: 3600. 3600.)
cld_tau_lsc=900
cld_tau_con=900

#corrective factors on the speed of ice crystals falling (D: 1 1)
ffallv_lsc=0.8
ffallv_con=0.8

# coefficient on the evaporation of rain (D: 2.e-5 n)
# rule a 3.e-5 on cases of cumulus in 1D
coef_eva=0.0001

# flag for rain evaporation
# 0: nothing
# 1: old-fashioned
# 2: takes into account the maximum cloud surface above to calculate
# the maximum reevaporation, as a deviation from saturation. TIP
iflag_evap_prec=2

# Modification of the temperature range for the mixed phase
# cloud liquid/ice
# Controlled by t_glance_min/max, exponent_ice,
# iflag_t_glance (D=0)
t_glance_min=243.15
t_glance_max=273.15
```

Large scale condensation & evaporation : practice

Large scale condensation (evap & lsc)

Subroutines : reevap & firtilp

Tendencies :

dteva, dqeva : tendencies due to cloud water evaporation

dtlsc, dqlsc : tendencies due to cloud water condensation

Total tendencies are the sums of the evaporation and condensation tendencies.

Other variables

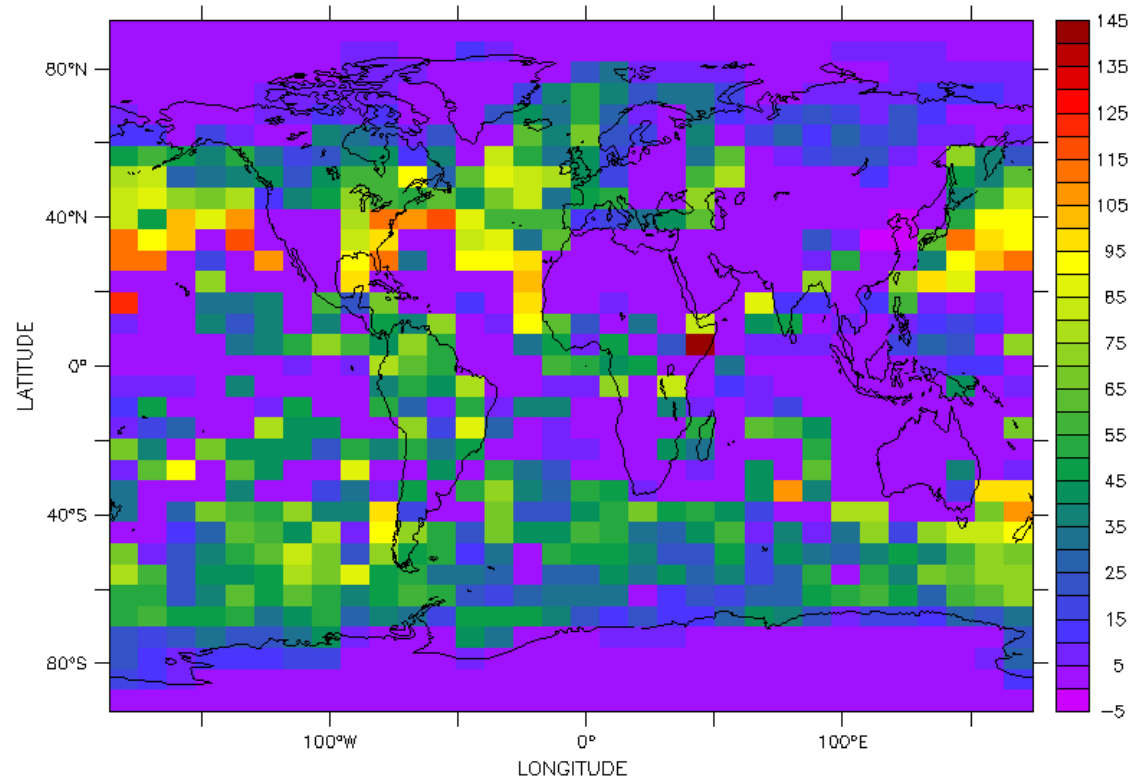
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- rneb : cloud cover
- pr_lsc_l : vertical profile of large scale liquid precipitation
- pr_lsc_i : vertical profile of large scale ice precipitation

ferret

xx use histhf.ns

xx shade/l=48 dtlsc[k=@max]*86400

xx go land 1



$DTLSC[K=@MAX]*86400 + DTEVA[K=@MAX]*86400$

Large scale condensation & evaporation : practice

Large scale condensation (evap & lsc)

Subroutines : reevap & fisrtlp

Tendencies :

dteva, dqeva : tendencies due to cloud water evaporation

dtlsc, dqlsc : tendencies due to cloud water condensation

Total tendencies are the sums of the evaporation and condensation tendencies.

Other variables

- plul : so called "large scale" or "stratiform" precipitation ; encompasses both stratiform precipitation and boundary layer cumulus precipitatic
- rneb : cloud cover
- pr_lsc_l : vertical profile of large scale liquid precipitation
- pr_lsc_i : vertical profile of large scale ice precipitation

TWIPICE case

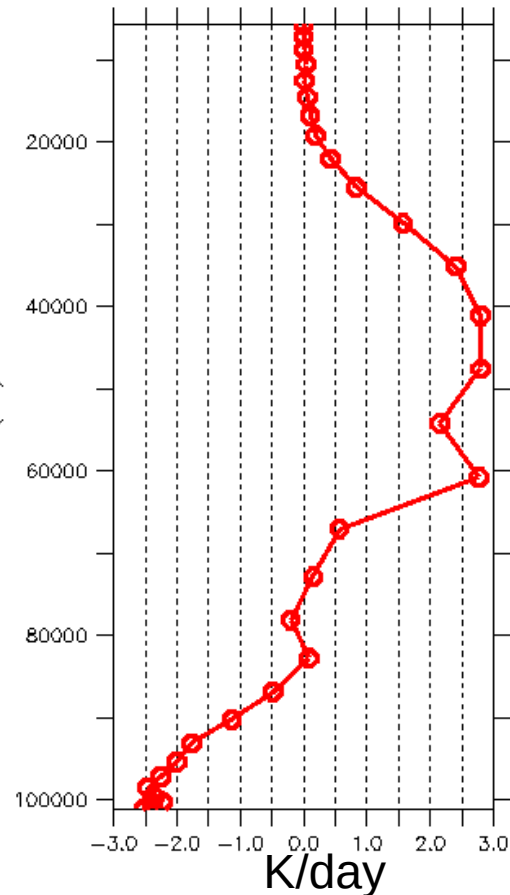
ferret

xx use histhf.nc

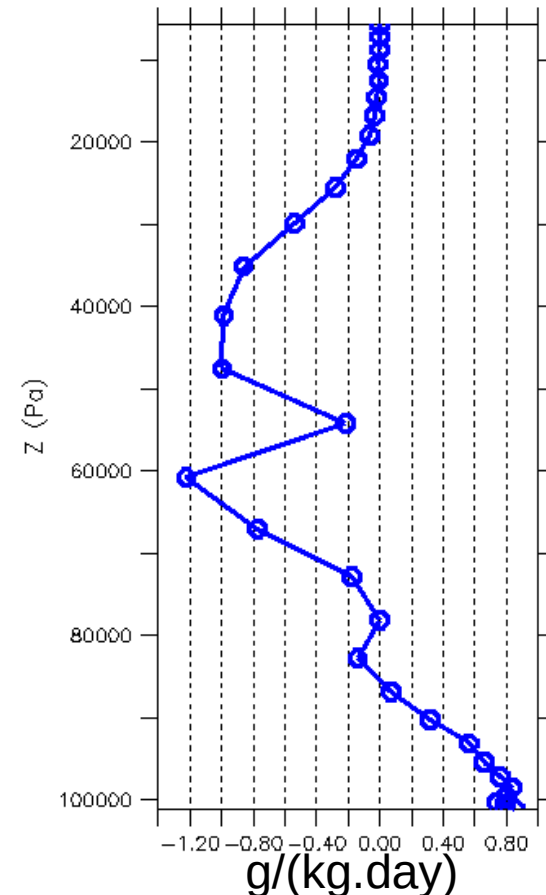
xx plot/l=48/thick=3/x=.../y=.../k=10:39
(dtlsc+dteva)*86400

xx plot/l=48/thick=3/x=.../y=.../k=10:39
(dqlsc+dqeva)*86400*1000

(dtlsc+dteva)*
86400



(dqlsc+dqeva)
*86400*1000



PARTIE PBL numérique → Frédérique

Turbulent diffusion

Turbulent diffusion

- Turbulent diffusion or "**turbulent mixing**" : transport by small random movements. Similar to molecular diffusion.

$$Dq/Dt = S_q \quad \text{où} \quad S_q = \frac{1}{\rho} \frac{\partial}{\partial z} \left(\rho K_z \frac{\partial q}{\partial z} \right) \quad \leftarrow \text{Downgradient flux}$$

- **Prandtl mixing length** : $K_z = l |w|$
 l : characteristic length of the small movements
 w : characteristic velocity
- **Turbulent kinetic energy (TKE)** : $K_z = l \sqrt{e}$

$$De/Dt = f(dU/dz, d\theta/dz, e, \dots)$$

$$Dl/Dt = \dots$$

Shear

Bouyancy

In LMDZ : TKE computed with Mellor and Yamada scheme

Turbulent diffusion

Turbulent diffusion : numerics

Process : Turbulent mixing of moisture (q in kg/kg) and potential enthalpy ($H = C_p\theta$).

$$\left\{ \begin{array}{l} \frac{dq}{dt} = -\partial_z \phi_q \\ \phi_q = -K_z \partial_z q \\ \phi_q|_{\text{srf}} = -\text{Evap} \end{array} \right. \left\{ \begin{array}{l} \frac{dH}{dt} = -\partial_z \phi_\theta \\ \phi_\theta = -K_z \partial_z H \\ \phi_\theta|_{\text{srf}} = \phi_{\text{sens}} \left(\frac{p_0}{p_{\text{srf}}} \right)^\kappa \end{array} \right. \quad \begin{array}{l} \leftarrow \\ \leftarrow \text{positive} \\ \leftarrow \end{array} \quad \begin{array}{l} \text{(Fluxes} \\ \text{downward)} \\ \text{Surface fluxes} \end{array} \quad (3)$$

Spatial discretization : (moisture)

$$\left\{ \begin{array}{l} m_i \partial_t q_i = \phi_{q,i+1} - \phi_{q,i} \\ \phi_{q,i} = K_i (q_i - q_{i-1}) \\ \phi_{q,1} = -\text{Evap} \end{array} \right. \quad (4)$$

Implicit scheme, yields for the first atmospheric layer :

$$\begin{array}{l} q_{1,t+\delta t} = A + B\phi_{q,1}\delta t \\ \phi_{q,1} = K_1(q_{1,t+\delta t} - q_{\text{srf}}) \end{array} \quad \leftarrow (5)$$

A and B are coefficient resulting from solving Eq. (4) over the whole atmosphere.

Eqs. (5) are the mixed boundary conditions for the sub-surface model.

$H = C_p T + gz =$ Dry static energy , here conserved

Water (left) and energy (right) conservation Diffusion

(Fluxes positive (downgradient flux)

downward)

Turbulent diffusion is the only one parameterization which « see » the surface

First atmospheric layer

Turbulent diffusion

Turbulent diffusion : numerics

Process : Turbulent mixing of moisture (q in kg/kg) and potential enthalpy ($H = C_p\theta$).

$$\left\{ \begin{array}{l} \frac{dq}{dt} = \partial_z \phi_q \\ \phi_q = K_z \partial_z q \\ \phi_q|_{\text{srf}} = -\text{Evap} \end{array} \right. \left\{ \begin{array}{l} \frac{dH}{dt} = \partial_z \phi_\theta \\ \phi_\theta = K_z \partial_z H \\ \phi_\theta|_{\text{srf}} = \phi_{\text{sens}} \left(\frac{p_0}{p_{\text{srf}}} \right)^\kappa \end{array} \right. \quad \begin{array}{l} \text{(Fluxes} \\ \text{positive} \\ \text{downward)} \end{array} \quad (3)$$

Spatial discretization : (moisture)

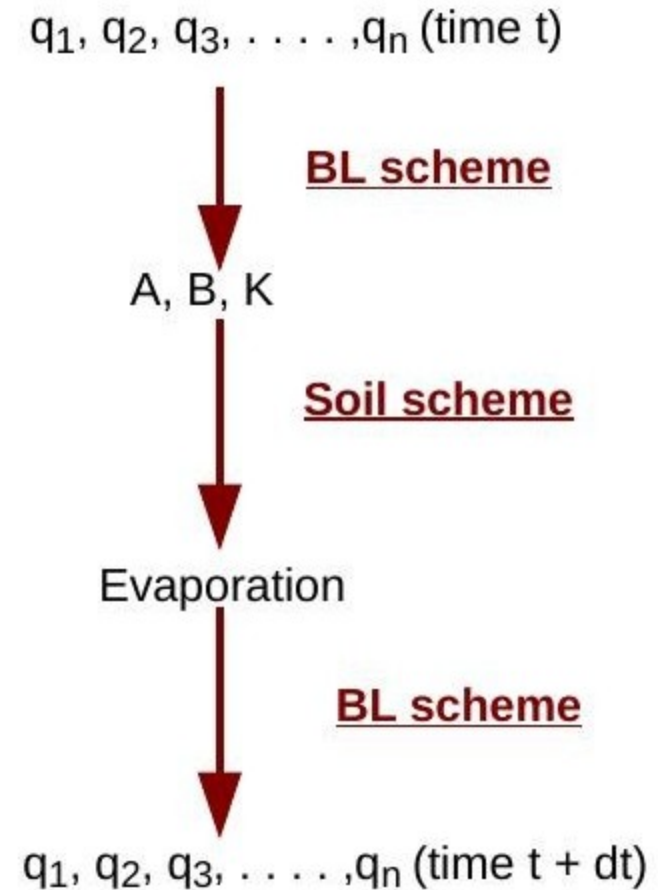
$$\left\{ \begin{array}{l} m_i \partial_t q_i = \phi_{q,i+1} - \phi_{q,i} \\ \phi_{q,i} = K_i (q_i - q_{i-1}) \\ \phi_{q,1} = -\text{Evap} \end{array} \right. \quad (4)$$

Implicit scheme, yields for the first atmospheric layer :

$$\begin{aligned} q_{1,t+\delta t} &= A + B\phi_{q,1}\delta t \\ \phi_{q,1} &= K_1(q_{1,t+\delta t} - q_{\text{srf}}) \end{aligned} \quad (5)$$

A and B are coefficient resulting from solving Eq. (4) over the whole atmosphere.

Eqs. (5) are the mixed boundary conditions for the sub-surface model.



ELIMINE

Boundary layer convection : practice

Thermals and dry adjustment

Subroutine : calltherm

Tendencies :

dtthe, dqthe, duthe, dvthe

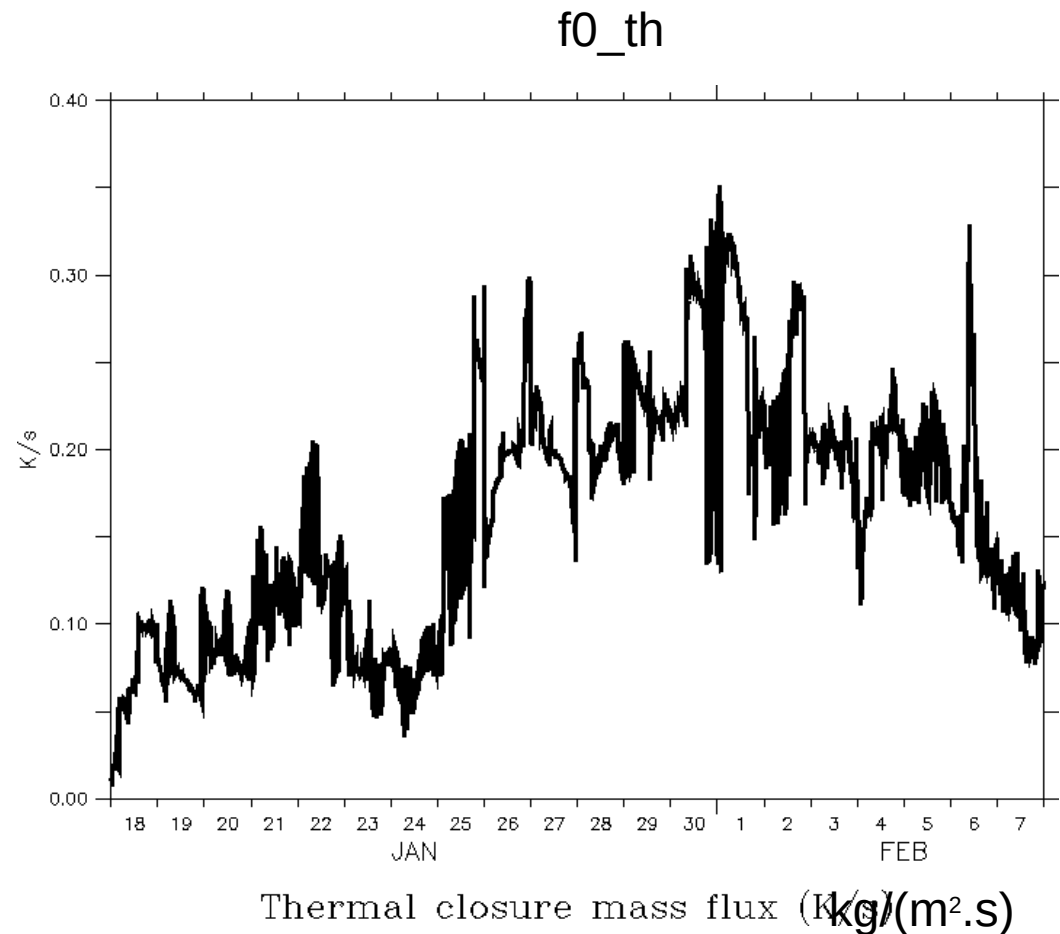
Other variables

- dtajs : temperature tendency due to the sole dry adjustment
- dqajs : humidity tendency due to the sole dry adjustment
- a_th : fractional area of thermal plumes
- d_th : detrainment
- e_th : entrainment
- f_th : mass flux
- w_th : vertical velocity in the thermal plume (m/s, positive upward)
- q_th : total water content in the thermal plume
- zmax_th : altitude of the top of the thermal plume (m)
- f0_th : Thermal closure mass flux (kg/m².s)

TWIPICE case



```
ferret
xx use histhf.nc
xx plot/thick=3/x=.../y=... f0_th
```



Parameterization = source terms

Atmospheric GCM equations

Primitive equations in pressure coordinates

Momentum equation :

$$\partial_t \vec{v} + \underbrace{(\vec{v} \cdot \vec{\nabla}_p) \vec{v}}_{\text{transport}} + \omega \partial_p \vec{v} + \underbrace{f \vec{k} \times \vec{v}}_{\text{Coriolis}} + \underbrace{\vec{\nabla}_p \Phi}_{\text{gravity}} = \vec{S}_v$$

Continuity equation :

$$\vec{\nabla}_p \cdot \vec{v} + \partial_p \omega = 0$$

Component conservation :

$$\partial_t q + \vec{v} \cdot \vec{\nabla}_p q + \omega \partial_p q = S_q$$

Thermodynamic equation :

$$\partial_t \theta + \vec{v} \cdot \vec{\nabla}_p \theta + \omega \partial_p \theta = \frac{\theta}{c_p T} \dot{Q}_{net}$$

$\Phi = gz$ geopotential
 $\omega = \partial_t p$ vert. velocity
 $q =$ specific humidity
 $\dot{Q}_{net} =$ heating rate
 from all diabatic sources

Sources

\vec{S}_v , S_q and \dot{Q}_{net} : source terms determined by the **physical parametrizations**

- planetary boundary layer, shallow and deep convection
- scattering and absorption by cloud droplets and crystals
- drag due to topography...